- 1 Technical Note: Rapid multi-exponential curve fitting algorithm for voxel-based targeted radionuclide
- 2 dosimetry
- 3 Key words: Radionuclide dosimetry, pharmacokinetics, image processing

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- 18 Short Title: Tri-exponential kinetics Algorithm
- 19 Abstract:

Background: Dosimetry in nuclear medicine often relies on estimating pharmacokinetics based on sparse temporal data. As analysis methods move toward image-based 3-dimensional computation, it becomes important to interpolate and extrapolate these data without requiring manual intervention; that is, in a manner that is highly efficient and reproducible. Iterative least-squares solvers are poorly suited to this task because of the computational overhead and potential to optimise to local minima without applying tight constraints at the outset.

Methodology: This work describes a fully-analytical method for solving three-phase exponential timeactivity curves based on three measured time points in a manner that may be readily employed by

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image-based dosimetry tools. The methodology uses a series of conditional statements and a piecewise approach for solving exponential slope directly through measured values in most instances. The proposed algorithm is tested against a purpose-designed iterative fitting technique and linear piecewise method followed by single exponential in a cohort of 10 patients receiving <sup>177</sup>Lu-DOTA-Octreotate therapy.

33 Results: Tri-exponential time-integrated values are shown to be comparable to previously-published 34 methods with an average difference between organs when computed at the voxel level of 9.8±14.2% 35 and -3.6±10.4% compared to iterative and interpolated methods, respectively. Of the three methods, 36 the proposed tri-exponential algorithm was most consistent when regional time-integrated activity was 37 evaluated at both voxel- and whole-organ levels. For whole-body SPECT imaging, it is possible to 38 compute 3D time-integrated activity maps in less than 5 minutes processing time. Further, the technique 39 is able to predictably and reproducibly handle artefactual measurements due to noise or spatial 40 misalignment over multiple image times.

Conclusions: An efficient, analytical algorithm for solving multi-phase exponential pharmacokinetics is
 reported. The method may be readily incorporated into voxel-dose routines by combining with widely
 available image registration and radiation transport tools.

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45 Keywords: radionuclide dosimetry, pharmacokinetics, image processing

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48 Main Text:

49 Background:

50 Driven by increasing recognition of the clinical benefits of radionuclide therapy, particularly in neuroendocrine tumors and prostate cancer<sup>1,2</sup>, image-based dosimetry in nuclear medicine has been a 51 focus of physics and computational development. The MIRD committee has published coefficients for 52 estimating radiation transport from sources at the voxel level<sup>3</sup> and other groups have supplemented 53 54 these tables for a variety of cubic dimensions and common therapeutic isotopes<sup>4,5</sup>. This has been 55 extended to patient-specific Monte Carlo calculations, which may now be performed in a clinically-56 achievable timeframe<sup>6,7</sup>. There has been consideration of the spatial effects of ionisation relative to 57 source location with respect to the resolution of the imaging systems used to infer that source distribution<sup>8</sup>. There has also been work extending dose metrics to infer radiobiological effect according 58 59 to dose-rate and spatial heterogeneity<sup>9</sup>.

While much focus has been applied to computation of radiation physics, research in pharmacokinetic
 interpolation is relatively limited. Inferring the input time-integrated activity map—a 3-dimensional grid

of the number of disintegrations per voxel—represents a comparably challenging task both in terms of complexity and potential to introduce errors in the predicted dose-volume. In the ideal instance, this is performed entirely in the image space allowing dosimetry to be appreciated at the level of detail attained by a SPECT imaging system. Typically, this workflow involves serial acquisition of multiple quantitative SPECT images<sup>10</sup> with pharmacokinetic time-activity curves (TACs) derived independently for each position in the aligned image sequence<sup>11</sup>.

68 One of the primary challenges in computing voxelized TACs is employing a routine that is 69 generalizable-that is, one that can be applied uniformly throughout the variety of tissues in the body-70 while operating without manual oversight and at minimal concession to fitting accuracy. Sarrut et al. 71 described an algorithm that places voxels into different classes to simplify the optimisation challenge and penalise models based on their complexity<sup>12</sup>. This, in principle, yields more reproducible results 72 73 than an unconstrained least-squares method. A similar approach had previously been employed by 74 Kletting et al. to enable users to designate between a variety of fitting functions based on the shape of 75 pharmacokinetic measurements, however, in requiring user input would not be appropriate for voxel 76 level dose estimation<sup>13</sup>. In this work a general three-phase exponential model is applied which offers 77 the flexibility to characterise components of uptake as well as a mixture of slow and fast tissue clearance 78 components.

79 An analytical pharmacokinetic estimation technique is reported in detail including the sequence of 80 computational operations and methods for handling noisy or otherwise irregular data. The technique 81 provides the basis for a previously-published voxel dosimetry software package<sup>14</sup> and has been shown 82 to be reliable across a variety of clinical trial datasets<sup>15</sup>. Given that all phases of the pharmacokinetic 83 curves—even those of uptake—may be described by equations of exponential decay, it is possible to 84 approach the problem as a piecewise operation. By solving for the slope between the final two 85 measurements, the preceding phases can be solved in sequence moving to earlier times based on the 86 difference between measured values and the trajectory of the previously predicted phase as a simplified 87 curve-stripping process<sup>16</sup>. Depending on the data conditions, where measurement values lie within 88 respective reference lines, the most appropriate order of solving may vary. In some instances, for 89 example when activity continues to increase beyond the second image time, the curve is best 90 approximated by only two phases using sustained uptake from injection to the final measurement, 91 followed by physical decay in the period beyond. This facilitates simplification of a highly unconstrained problem—six variables with only three data points—using only a few straightforward assumptions and 92 93 computational logic operations. With judicious selection of acquisition times, this form of curve 94 generation may be applied in a manner that is representative, and without systematic bias, for a wide 95 variety of pharmacokinetic models.

96 Methods:

97 With the aim to solve parameters that define a three-phase exponential curve described by Equation 1, 98  $A_{1-3}/k_{1-3}$ , the ideal case includes a single phase of tissue uptake and up to two phases of clearance.

- 99 This model may describe periods of rapid washout and long-term retention; each with a variable half-100 life and relative proportion as represented across a variety of pharmacokinetic tissue types.
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Region Activity =  $A_1e^{k_1t} + A_2e^{k_2t} + A_3e^{k_3t}$ 

102 Equation 1

[Figure 1]

Three activity concentration values are described as  $c_{1-3}$  and time points as  $t_{1-3}$ . As a preliminary step, 104 the convention is taken to decay-correct all image data,  $c_{i_{1-3}} \rightarrow c_{1-3}$ , as illustrated in Figure 1. This 105 106 handles concentration values in pharmacological terms during fitting. The decay-correction is 107 straightforward to reverse when taking the final integral calculation and offers practical advantage to 108 ensure that the pharmacological concentration does not continue to increase beyond the final imaging 109 time point. This should be a reasonable assumption given judicious selection of imaging time points<sup>17</sup>. 110 Specifically, it prevents the final integral from exceeding a value that would exceed the physical half-life of the isotope; curves which deplete more slowly than the half-life of the radionuclide. If the highest 111 112 activity measurement is detected at the final time point, fitting a slope very near zero,  $k_{3} \approx -\infty$ , equates to 113 only physical decay. Secondly, this provides a simple mechanism to adapt the algorithm for other 114 isotope or diagnostic/therapeutic pairs, for example using sequential <sup>124</sup>I PET/CT imaging to predict radiation dose from <sup>131</sup>I radioactive iodine. The user only needs to provide the physical half-life of each 115 tracer and the same algorithm may be applied to compute local time-integrated activity concentration 116 (decays per unit volume) for the given quantity of activity administered. 117

118 [Figure 2]

The ideal case can be described by a transient uptake phase between t=0 and  $t_1$  followed by distinct periods of rapid and delayed washout in the  $t_{1\rightarrow 2}$  and  $t_{2\rightarrow 3}$  time spans, respectively, as shown in Figure 2. In clinical use of long half-life therapeutic isotopes, after initial uptake, one or two exponential clearance phases of activity from organs and tumors are widely described<sup>18</sup>. It is possible to fit a curve of exponential decay between two points as shown in Figure 3 with the form:

124  $A = A_0 e^{kt}$ 

125 Equation 2

Solving for the linear fit, y = mx + b, by log transform of the activity values starting with the final phase, the kinetic parameter,  $k_3$ , is determined by:

128 
$$k_3 = m = \frac{\ln(c_3) - \ln(c_2)}{t_3 - t_2}$$

129 Equation 3:

130 And the amplitude parameter,  $A_3$ , is then:

$$A_3 = e^b = e^{\ln(c_2) - k_3 t_2}$$

132 Equation 4:

133 [Figure 3]

As a first instance, this method provides the slope of the line representing the long-term retention phase. 134 135 The preceding phase can be described as the difference between the slope described by the  $A_3, k_3$ curve and the value at  $c_1$  using another exponential decay equation that depletes as it approaches  $t_2$ . 136 137 This very nearly builds a piecewise function from exponential terms. Solving by log transform requires 138 non-zero values, so, for simplicity, we adjust the latter activity value, delta  $c_2$ , to be in the range of 1-139 3% of the measured value  $c_2$ . Some discussion of the special conditions which warrant the variability is 140 provided in later sections. The process may be more clearly illustrated by the mixture of curves in Figure 141 4. The residual of the curve,  $\Delta c_1$ , is the difference between the slope of the late phase and the first measured activity value,  $c_1$ : 142

143  $\Delta c_1 = c_1 - A_3 e^{k_3 t_1}$ 144 Equation 5:

145 The sign of the delta value is evaluated:  $\Delta c_2 = 0.01 * c_2$  if  $\Delta c_1$  is greater than zero. If not, the sign is 146 reversed to  $\Delta c_2 = -0.01 * c_2$ . That is, both delta values should be positive or negative. There are 147 conditions when a negative  $A_2$  provides the most appropriate fit based on the measured data. Curve 148 approximation then follows the previous method of solving for exponential slope to generate a phase 149 that depletes as it approaches  $c_2$ :

 $k_2 = \frac{\ln(\Delta c_2) - \ln(\Delta c_1)}{t_2 - t_1}$ 

 $A_2 = e^{\ln\left(\Delta c_1\right) - k_2 t_1}$ 

150

152 Equation 6:

153 [Figure 4]

Estimating the very early uptake kinetics requires an approximation when there are no intermediate 154 155 points before the peak activity measurement. This is typical when only one image is available during the first day of administration. One approach is to infer the uptake pharmacokinetics based on a generic 156 157 rate constant, k<sub>1</sub>. For long half-life therapeutic isotopes, the majority of the time-integrated activity 158 calculation is dictated by the late-phase retention. That is, if the physical half-life is several days or 159 longer, only select tissues with significant initial uptake followed by rapid and sustained clearance could 160 be appreciably impacted by the use of a generic uptake parameter. The notable exception is choosing 161 a very small  $k_1$  parameter representing very rapid uptake. In this case, the presented algorithm may yield a curve that escalates dramatically at times close to t=0 due to the nature of solving the line-of-fit 162 for the fast clearance phase. With <sup>177</sup>Lu, a half-time of approximately 30 minutes,  $k_1$ =-1.3, has been 163

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shown to offer reasonable agreement with other curve-fitting integrals over a range of different tissue types<sup>14,19</sup>. An analysis of the influence of the generic rate parameter on time-integrated activity is provided in Supplementary Table 1 showing that over a range of half-times from 20 to 90 minutes, the effect is in the order of ±2% except in bladder and heart (blood pool). Finally, the amplitude,  $A_1$ , of the uptake phase is set such that concentration value passes through zero at *t*=0. Here the term  $A_1$ becomes the negative of the sum of  $A_2$  and  $A_3$ .

170 In this manner, it is possible to analytically solve a three-phase exponential that very closely passes 171 through three measured time points. This piecewise method, or a slightly modified version, can be 172 applied wherever declining slope is detected between values of  $c_2$  and  $c_3$ ; that is, whenever some 173 clearance is detected in the late phase of imaging as would be typical of most tracers and tissue types. 174 The sequence of computations is depicted in the flowchart shown by Supplementary Figure 6 with this 175 common case designated by bold labels.

176 With the solved time-activity curve, it is then possible to integrate the decay-corrected curve from  $t_{0 \rightarrow inf}$ 177 including the physical half-life of the isotope in the form:

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 $\tilde{A} = \frac{A_1}{(\frac{ln2}{t_{1/2}} + k_1)} + \frac{A_2}{(\frac{ln2}{t_{1/2}} + k_2)} + \frac{A_3}{(\frac{ln2}{t_{1/2}} + k_3)}$ 

179 Equation 7:

180 Where  $\tilde{A}$  is the time-integrated activity or total number of disintegrations in the region described by the 181 time-activity curve,  $t_{1/2}$  is the physical half-life of the therapeutic isotope, and the parameters  $A_{1-3}$  and 182  $k_{1-3}$  are the fitting values described previously.

183 A detailed explanation of conditional methods to derive curves for irregular, or slowly-accumulating data 184 is provided in the supplementary material (Supplementary Figures 1-3). This involves methods to 185 classify the shape of the curve to apply algorithmic steps suited to that pharmacokinetic type. In some 186 instances, such as when activity decreases from  $c_1$  to  $c_2$  and increases again at  $c_3$  the algorithm will 187 interpolate an intermediate location to analytically define a curve that balances the necessary error 188 between measurements with a behaviour that is similar to least-squares optimisation. It is worth noting 189 that for these cases, the convention is taken to define a curve that as often as possible passes directly 190 through the final measurement time-typically the most important for long half-life isotopes-and 191 subsequently mitigate the error for the line-of-fit that passes through or near the preceding times. Flow 192 charts to illustrate the conditional sequence of processing are given in Supplementary Figures 4-6.

The multi-exponential algorithm was tested in clinical application in a representative cohort of 10 patients receiving <sup>177</sup>Lu-DOTA-Octreotate. Cases were followed-up by serial post-treatment quantitative SPECT imaging at timelines of 4, 24, & 72 hours. Pharmacokinetics were then computed at the voxel level with the proposed tri-exponential algorithm. For comparison to two reference methodologies, timeintegrated activity was estimated by piecewise linear approximation between image times followed by a single exponential phase determined by the effective half-life over the final two image acquisitions<sup>20</sup>.

199 In voxels where the detected clearance rate was slower than the physical half-life of <sup>177</sup>Lu, clearance 200 was instead based on physical decay. Secondly, the iterative fitting technique described by Sarrut et 201 al., the Voxel-based Multimodal method (VoMM), was implemented with Python libraries<sup>12,21</sup>. In that 202 method, iterative optimization is performed for each voxel according to four different single- or multi-203 exponential models and the most accurate line-of-fit with a penalty for model complexity is chosen. The 204 resulting time-integrated activity concentration for each technique was compared both at the voxel level 205 and based on a single curve derived from the mean activity in each volume-of-interest. For tumor and 206 a selection of relevant tissues (kidney, spleen, liver, bladder, marrow, etc) time-integrated activity was assessed. Additionally the mean absolute error as weighted for voxel activity in predicted curves with 207 208 the tri-exponential algorithm and VoMM method was investigated for each imaging time point. The 209 median of all cases with each technique is summarized.

210 Results:

This work presents a computationally efficient methodology to solve highly unconstrained curve fitting 211 212 in a predictable manner. The authors have previously demonstrated that this algorithm yields 213 comparable regional dosimetry when applied independently across regional voxels to whole-organ 214 methods employed with OLINDA coupled with a traditional iterative curve solver<sup>14,19</sup>. In comparison to alternative voxel methods including trapezoidal interpolation followed by a single exponential and the 215 216 previously published VoMM iterative technique, closest agreement between methods was observed in 217 long-retaining tissues. Time-integrated activity in high-uptake organs (kidney, liver, spleen)-those considered at-risk in <sup>177</sup>Lu-Ocreotate therapy—was on average within 10% for all curve fitting methods 218 219 evaluated at the voxel level. Results for the 10 patient cohort are summarised in Table 1 and an 220 evaluation of median voxel-wise fitting error at each of the three imaging time points is reported for the 221 tri-exponential and VoMM techniques in Table 2. The three methods were observed to be in closer 222 agreement when pharmacokinetics were computed at the organ- rather than voxel-level where the tri-223 exponential algorithm was within 5% of the VoMM technique for all regions except for bladder, intestines 224 and pancreas. Of the three, the proposed tri-exponential algorithm most closely reproduces the whole 225 organ time integrated activity result when calculated from independent voxel curves with the lowest 226 variation observed for 8 of the 15 regions including tumor, marrow, liver, and left kidney.

227 In comparison to a trapezoidal interpolation followed by single-exponential model, the multi-exponential 228 model was typically 3.5% lower in terms of estimated integral decays with most organs in the range of 229 -1 to -8%. Much of the area under the curve for these therapies is dictated by the late phase retention 230 which should be similar in most cases with single- and tri-exponential evaluations. A significant 231 difference in dose to bladder is reported with all three methods which may be attributed to the relative 232 variation in uptake between images on the first day of therapy and those acquired at 24 hours and beyond. Where tissues displaying this form of clearance are relevant for assessing potential toxicity, it 233 234 is advisable to collect finer temporal sampling in the first day post-administration.

The scripted implementation of the fitting algorithm using Python computes at a rate of approximately 5,000 voxels per second with clinical image data<sup>14,22</sup>. Applying a condition to ignore background

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voxels-those with very low activity values-dose volumes for a multi-bed SPECT series at 3.0mm 237 238 cubic spatial resolution can be computed in less than five minutes. Processing times were comparable 239 to trapezoidal and single-exponential model. The iterative VoMM method was considerably more 240 computationally intensive, previously reported at 800 voxels per second<sup>12</sup>, however the python-based 241 implementation would not be practical to apply across the full image space and voxel-wise fitting was 242 restricted to labelled subregions. Image-based pharmacokinetics processing is often coupled with nonrigid image registration to tightly fuse the serial time points across the image volume<sup>23</sup>. That step will 243 244 typically be equally or more computationally intensive than the pharmacokinetics process described in this work and as such this method of pharmacokinetic interpolation should not be considered a 245 246 significant bottleneck to clinical workflows. As a complete image-based dosimetry tool, the algorithm 247 has been employed in a variety of clinical studies for both therapeutic and diagnostic dose evaluation 248 which have been used to inform patient management<sup>24-27</sup>.

249 [Table 1]



250 The overall residual error was observed to be comparable between iteratively optimized and tri-251 exponential algorithms, however, the VoMM method was shown to be most accurate at the early image 252 phase with increasing error at later time points. This is to be anticipated as the observed activity-and potential to influence sum of squared error-carries less weight for the optimization task. In contrast, 253 254 the proposed tri-exponential algorithm is designed to fit directly through the 2<sup>nd</sup> and 3<sup>rd</sup> measurements 255 wherever the shape of the curve would sensibly permit. This may necessarily come at the sacrifice of 256 accuracy in the very early phases; for example, in bowel which can be slow to accumulate <sup>177</sup>Lu-257 Octreotate over several days.

258 [Table 2]

259 Discussion:

260 This work aims to describe an automated, reproducible and efficient methodology for solving a large 261 volume of time-activity curves with application to nuclear medicine dosimetry. The choice of three-phase exponential model affords the flexibility to characterise periods of tracer uptake as well as mixtures of 262 263 slow- and fast-clearance. By considering the sequence of operations, it is possible to address model 264 over-complexity: solving the most important phase at the outset and applying additional phases as 265 necessary with decreasing influence on the time integral. The resulting algorithm is designed to yield comparable estimates of time-integrated activity to traditional methods including linear piecewise 266 interpolation or constrained least-squares optimisation. Additionally as a pure exponential model, it is 267 268 straightforward to apply isotope decay corrections and integral calculations. Many of the standard kinetic coefficients selected in the present implementation are chosen empirically as a practical solution 269 270 for use in <sup>177</sup>Lu-DOTA-octreotate dosimetry and with imaging times routinely used in clinical practice. 271 The conditional methods have been shown to reliably approximate time-integrated activity estimates 272 from other curve-fitting techniques when compared both at the voxel and organ level.

It has been consistently reported that delayed image acquisitions are most important to accurately 273 274 estimate dosimetry in <sup>177</sup>Lu therapies even for complex pharmacokinetic models<sup>28,29</sup>. The algorithm in 275 this work is designed to yield curves which pass through the final acquisition time and, where 276 appropriate, will directly determine late phase clearance based on the line of slope between the second 277 and third image acquisitions. This is in contrast to most iterative least-squares solvers which, in the 278 ordinary case, will be weighted toward uptake when activity is largest, typically at the earliest time point 279 and may be at the expense of accurately characterizing time-integrated activity. This can be improved 280 upon by modifying the objective function to bias the weighting of certain measurements either explicitly or through additional iterative operations <sup>30</sup>, but this presents a different set of challenges if the aim is 281 282 to implement as a general purpose tool to efficiently run in the image space. Balancing patient 283 convenience with quantitative accuracy and ease of use is a motivation for improved algorithms for 284 clinical dosimetry.

There are intrinsic limitations to fitting a six-variable equation to three measured data points; or 285 286 effectively four if directed through zero at the origin and generic uptake rates are considered. Even with 287 well-conditioned data, the combination of clearance half-times and fractions may be modified to yield 288 an infinite number of solutions which pass through the measurement values. This is constrained if each 289 phase of the multi-exponential term depletes to very near zero as it transitions from one measurement 290 to the next. Subsequently, the shape of the curve is influenced by the selection of image times as the 291 inflection between phases 2 and 3 will necessarily occur at the second measurement time. If the time 292 points are not chosen sensibly, or there are inconsistencies in the image times between patients within 293 a cohort, systematic bias could result. This, however, is a challenge for any pharmacokinetic 294 assessment methodology and it is worthwhile to restate the importance of judicious selection of 295 measurements with consideration of the pharmacokinetics and physical half-life of any radiopharmaceutical. Of specific note, when using short half-life isotopes or imaging in the first two 296 297 hours of administration, it is advisable to experiment with the standard uptake rate coefficient,  $k_1$ , which may be modified (and likely reduced) to reliably model the underlying physiology. As with the selection 298 299 of uptake half-time, the use of conditional assumptions may warrant special consideration for the pharmacokinetics of individual tracers with <sup>124</sup>, <sup>131</sup> and <sup>90</sup>Y being of particular interest in the context of 300 301 current therapeutic radionuclides. Additionally, with increasing focus on the potential for theranostic isotope pairs such as <sup>86</sup>Y/<sup>90</sup>Y, <sup>44</sup>Sc/<sup>47</sup>Sc, or <sup>64</sup>Cu/<sup>67</sup>Cu which permit delayed, high-resolution imaging 302 and treatment with an equivalent molecular species, the ability to assess pharmacokinetics in the image 303 304 space is particularly relevant.

In this report, a working version of the algorithm is distributed as open-source software, which may be employed directly or improved upon by contributing researchers. Because the algorithm runs with a set of conditional statements and a sequence for solving for exponential slope between two points, it is possible to implement in software that handles basic conditional and mathematical operations. For demonstration or use as a region-based dosimetry tool, the algorithm has been incorporated into an interactive spreadsheet, which is available in the supplementary material supporting this article or at the primary author's Github repository<sup>31</sup>.

### 312 Conclusions:

This report presents a generalizable algorithm to derive time-activity curves from limited temporal measurement data. The methodology relies on separating the curve-fitting challenge into piecewise phases similarly to a residual stripping technique. Conditional statements allow the process to be applied in a predictable manner that achieves a sensible compromise in error for voxels which may be subject to noise or inconsistent co-registration. The technique is computationally efficient allowing use for routine image-based dosimetry. A complete version of the algorithm is provided as open-source computer code for developers of nuclear medicine analysis software.

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333 Conflicts-of-interest:

334 The authors have no conflicts to disclose

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- 336 Citations:
- Fanti S, Minozzi S, Antoch G, et al. Consensus on molecular imaging and theranostics in
   prostate cancer. *The Lancet Oncology*. 2018;19(12):e696-e708.
- Kwekkeboom DJ, Krenning EP, Lebtahi R, et al. ENETS consensus guidelines for the standards
   of care in neuroendocrine tumors: peptide receptor radionuclide therapy with radiolabeled
   somatostatin analogs. *Neuroendocrinology*. 2009;90(2):220-226.
- Bolch WE, Bouchet LG, Robertson JS, et al. MIRD pamphlet no. 17: the dosimetry of
   nonuniform activity distributions—radionuclide S values at the voxel level. *Journal of Nuclear Medicine*. 1999;40(1):11S-36S.

Lanconelli N, Pacilio M, Meo SL, et al. A free database of radionuclide voxel S values for the
 dosimetry of nonuniform activity distributions. *Physics in Medicine & Biology.* 2012;57(2):517.

- Dieudonné A, Hobbs RF, Bolch WE, Sgouros G, Gardin I. Fine-resolution voxel S values for
   constructing absorbed dose distributions at variable voxel size. *Journal of nuclear medicine*.
   2010;51(10):1600-1607.
- Pacilio M, Lanconelli N, Lo Meo S, et al. Differences among Monte Carlo codes in the
   calculations of voxel values for radionuclide targeted therapy and analysis of their impact on
   absorbed dose evaluations. *Medical physics.* 2009;36(5):1543-1552.
- Jackson PA, Hickson K. Integration of GATE Monte Carlo-based radionuclide dosimetry as a
   practical on-line clinical tool. Paper presented at: 2017 Geant4 User Workshop2017;
   University of Wollongong, Wollongong, Australia.
- Pacilio M, Amato E, Lanconelli N, et al. Differences in 3D dose distributions due to calculation
   method of voxel S-values and the influence of image blurring in SPECT. *Physics in Medicine & Biology*. 2015;60(5):1945.
- Sgouros G, Frey E, Wahl R, He B, Prideaux A, Hobbs R. Three-dimensional imaging-based
   radiobiological dosimetry. Paper presented at: Seminars in nuclear medicine2008.
- 10. Dewaraja YK, Frey EC, Sgouros G, et al. MIRD pamphlet no. 23: quantitative SPECT for patient specific 3-dimensional dosimetry in internal radionuclide therapy. *Journal of Nuclear Medicine*. 2012;53(8):1310-1325.
- Ljungberg M, Celler A, Konijnenberg MW, Eckerman KF, Dewaraja YK, Sjögreen-Gleisner K.
   MIRD pamphlet no. 26: joint EANM/MIRD guidelines for quantitative 177Lu SPECT applied for
   dosimetry of radiopharmaceutical therapy. *Journal of nuclear medicine*. 2016;57(1):151-162.
- 367 12. Sarrut D, Halty A, Badel JN, Ferrer L, Bardiès M. Voxel-based multimodel fitting method for
   368 modeling time activity curves in SPECT images. *Medical physics*. 2017;44(12):6280-6288.
- 369 13. Kletting P, Schimmel S, Kestler H, et al. Molecular radiotherapy: The NUKFIT software for
   370 calculating the time-integrated activity coefficient. *Medical physics.* 2013;40(10):102504.
- Jackson PA, Beauregard JM, Hofman MS, Kron T, Hogg A, Hicks RJ. An automated voxelized
   dosimetry tool for radionuclide therapy based on serial quantitative SPECT/CT imaging.
   *Medical physics.* 2013;40(11).
- Violet J, Jackson P, Ferdinandus J, et al. Dosimetry of 177Lu-PSMA-617 in Metastatic
   Castration Resistant Prostate Cancer: Correlations Between Pretherapeutic Imaging and
   Whole-Body Tumor Dosimetry with Treatment Outcomes. *Journal of Nuclear Medicine*.
   2019;60(4):517-523.

- 378 16. Kirkup L, Sutherland J. Curve stripping and nonlinear fitting of polyexponential functions to
  379 data using a microcomputer. *Computers in Physics.* 1988;2(6):64-68.
- Siegel JA, Thomas SR, Stubbs JB, et al. MIRD pamphlet no. 16: techniques for quantitative
   radiopharmaceutical biodistribution data acquisition and analysis for use in human radiation
   dose estimates. *Journal of Nuclear Medicine*. 1999;40(2):37S-61S.
- Stabin M, Xu XG. Basic principles in the radiation dosimetry of nuclear medicine. Paper
   presented at: Seminars in nuclear medicine2014.
- 385 19. Stabin MG, Sparks RB, Crowe E. OLINDA/EXM: the second-generation personal computer
  386 software for internal dose assessment in nuclear medicine. *Journal of nuclear medicine*.
  387 2005;46(6):1023-1027.
- Grassi E, Fioroni F, Ferri V, et al. Quantitative comparison between the commercial software
   STRATOS<sup>®</sup> by Philips and a homemade software for voxel-dosimetry in radiopeptide therapy.
   *Physica Medica*. 2015;31(1):72-79.
- Virtanen P, Gommers R, Oliphant TE, et al. SciPy 1.0: fundamental algorithms for scientific
   computing in Python. *Nature Methods.* 2020:1-12.
- Van Der Walt S, Colbert SC, Varoquaux G. The NumPy array: a structure for efficient numerical
  computation. *Computing in Science & Engineering*. 2011;13(2):22.
- Klein S, Staring M, Murphy K, Viergever MA, Pluim JP. Elastix: a toolbox for intensity-based
   medical image registration. *IEEE transactions on medical imaging*. 2010;29(1):196-205.
- Willowson KP, Ryu H, Jackson P, Singh A, Eslick E, Bailey DL. A comparison of 2D and 3D kidney
   absorbed dose measures in patients receiving 177Lu-DOTATATE. *Asia Oceania Journal of Nuclear Medicine and Biology*. 2018;6(2):113.
- Hicks RJ, Jackson P, Kong G, et al. First-in-human trial of 64Cu-SARTATE PET imaging of patients
   with neuroendocrine tumours demonstrates high tumor uptake and retention, potentially
   allowing prospective dosimetry for peptide receptor radionuclide therapy. *Journal of Nuclear Medicine.* 2018:jnumed. 118.217745.
- 404 26. Pattison DA, Solomon B, Hicks RJ. A new theranostic paradigm for advanced thyroid cancer.
  405 *Journal of Nuclear Medicine*. 2016;57(10):1493-1494.
- Kong G, Callahan J, Hofman MS, et al. High clinical and morphologic response using 90 Y-DOTA octreotate sequenced with 177 Lu-DOTA-octreotate induction peptide receptor
   chemoradionuclide therapy (PRCRT) for bulky neuroendocrine tumours. *European journal of nuclear medicine and molecular imaging*. 2017;44(3):476-489.

- 410 28. Hänscheid H, Lapa C, Buck AK, Lassmann M, Werner RA. Absorbed dose estimates from a
  411 single measurement one to three days after the administration of 177Lu-DOTATATE/-TOC.
  412 *Nuklearmedizin.* 2017;56(06):219-224.
- 413 29. Madsen MT, Menda Y, O'Dorisio TM, O'Dorisio MS. Single time point dose estimate for
  414 exponential clearance. *Medical physics.* 2018;45(5):2318-2324.
- 415 30. Muzic Jr RF, Christian BT. Evaluation of objective functions for estimation of kinetic
  416 parameters. *Medical physics.* 2006;33(2):342-353.
- 41731.JacksonPA.Github-TriExponential-Solver.2019;418https://github.com/jacksonmedphysics/TriExponential-Solver.
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- 420

421 Supplementary Material:

422 Handling of irregular data:

423 When performing operations across many thousands of voxels that may be prone to noise or image alignment errors, there are likely to be challenging locations that warrant special consideration to yield 424 425 curves and integrals which represent fair approximations of the underlying data. In instances where the 426 highest activity is detected at  $t_{3}$ , a reasonable convention is to assume that only physical decay occurs 427 at time points beyond<sup>20</sup>; or for simplicity that there is very slight pharmacological clearance such that 428 the effective half-time is determined by the physical half-life of the isotope as illustrated in 429 Supplementary Figure 1. In the proposed method, setting  $k_3$  to a value near zero yields an equivalent 430 computation when applied to decay-corrected data. The coefficient  $A_3$  may be solved according to Equation 4. There may be no need to fit multiple uptake phases in this instance ( $A_2=0$ ). Instead, the 431 432 method from Equation 6 is used to solve for a single uptake phase that reaches a maximum as it nears 433  $c_3$ . There is scope to moderate the uptake kinetics based on the measured data points  $c_1$  and  $c_2$ , as illustrated in the flow chart shown by Supplementary Figure 5. Nevertheless, the area under the curve 434 435 for long half-life isotopes will be primarily dictated by the amplitude of uptake at measurement  $c_3$ . In 436 other instances, this type of curve may be physiologically appropriate.

437 [Supplementary Figure 1]

The most apparent case where the data requires correction from the outset is when the trajectory of uptake or clearance changes multiple times across the measurement points. This may occur when a region initially displays a large activity concentration that appears to decrease at the time of the second image and subsequently increases again at the third. In image-based dosimetry, these instances are often artefactual; produced due to noise or small misalignments near the margin of high-uptake tissues such as kidneys and spleen. Here, the aim is to mitigate potential errors and yield a curve that approximates the behaviour of a least-squares fitting routine. In this methodology, the convention is taken that the final time point is most important to determine the time integral. The values of the first
two points are moderated such that it is possible to apply a curve solving methodology which balances
error with respect to the early phase(s) as shown in Supplementary Figure 2.

### 448 [Supplementary Figure 2]

Solving exponential slope between values that transition to very near zero can be problematic. This 449 450 tends to occur for voxels in low-uptake regions where small changes in absolute activity concentration 451 represents very large relative differences if one of the values is near zero. Although this type of 452 measurement is largely influenced by scanner sensitivity in background regions and reconstructed 453 noise, using those rate kinetics parameters leaves the potential to infer extremely high uptake in the 454 very early time window and, as such, overestimate time-integrated activity. As a practical fix, the relative 455 uptake can be initially compared across time-points and adjusted if necessary—in this case  $c_3$  is 456 modified to 10% of the value at  $c_2$  as shown in the preconditioning flow-chart, Supplementary Figure 457 4-to yield a more sensible curve and estimate of integral decays.

Additionally, computation of two threshold  $c_2$  values are used to define the limits for the slope between 458 459 the values of  $c_1$  and  $c_3$ . The first,  $c_{2,\text{plateau}}$ , is used to test whether activity increases between time points 460 2 and 3. If the activity at  $c_1$  is also very low, as may occur in some tissues that slowly accumulate tracer such as bowel in <sup>177</sup>Lu-PMSA therapy, no correction would be warranted. In other cases where activity 461 462 initially declines from  $c_1$  to  $c_2$  only to increase again at the final measurement such as shown in 463 Supplementary Figure 2, it is logical to assume that some element of the measurement is artefactual. 464 Shifting the value of  $c_2$  up to the plateau point where the exponential fit between  $c_2$  and  $c_3$  achieves 465 minimal biological clearance; or effectively only physical decay from  $t_2$  and passing through the 466 measurement  $c_3$ . With this parameter solved, it is then possible to apply the piecewise methodology to 467 solve the remaining phases that may appropriately to pass through  $c_1$ .

468 [Supplementary Figure 3]

469 When the concentration at  $c_2$  appears as less than a linear interpolation between time points  $c_1$  and  $c_3$ 

(illustrated in Supplementary Figure 3), a solution is to compute a value that falls on that line,  $c_{2,linear}$ ,

that may replace the original value if increasing slope is required to approximate the curve up to the

final imaging time. The resulting curve is illustrated in Supplementary Figure 3 and the implementation

into the algorithmic workflow can be traced in Supplementary Figure 5 and Supplementary Figure 6.

- 474 [Supplementary Figure 4]
- 475 [Supplementary Figure 5]
- 476 [Supplementary Figure 6]
- 477
- 478 Selection of Generic Uptake Rate Parameter  $(k_1)$ :

479 For the common condition where fast- and slow-clearance components are observed it is sensible to 480 implement a generic uptake rate in order to prevent unrealistically large activity extrapolations in the 481 times between t=0 and the first measurement. By setting the amplitude parameter  $A_1$  equal to the 482 negative sum of the  $A_2$  and  $A_3$  coefficients, the curve will necessarily pass through the origin at the 483 time of administration and a generic  $k_1$  coefficient should be applied which allows uptake to complete 484 prior to the first measurement (typically in the first several hours) but mitigates the potential for large area under the curve in the initial moments post-administration. In this instance, an empirically chosen 485  $k_1$  value of -1.3 (approximately 30 minutes half-time) appears to provide a reasonable approximation 486 487 for a variety of tissue types. The results of experiments with other rate parameters for half-times of 488 20, 60, and 90 minutes are provided in Supplementary Table 1 and yield time-integrated activity values 489 within 2% in all instances, except in tissues with a particularly large component of early-phase 490 clearance such as urinary bladder and heart (blood pool).

491 [Supplementary Table 1]

492

493 Figure Captions:

Figure 1: Decay-correcting initial measured data before fitting ensures algorithm does not fit increasing pharmacological concentration beyond final imaging time point. This is accounted for when calculating time-integrated activity and easily permits estimates from diagnostic/therapeutic isotope pairs such as <sup>124</sup>/<sup>131</sup>I.

Figure 2 - Illustration of typical time-activity curve comprised of three exponential phases that has been solved to pass through measured data points. Plots of the component exponential curves, one uptake and two clearance, are shown as dashed lines. The sum of phases 2 & 3 and all phases are shown as shown as solid green and solid blue, respectively. Note that phase 1 and phase 2 effectively deplete as the curve nears measurement time points 1 & 2.

Figure 3 - Standard (left) and logarithmic (right) plots of method to solve late-phase clearance based
on exponential slope between measurement time points 2 and 3.

Figure 4 - Method to solve phase 2, first clearance phase, based on the difference in the curve
described by Figure 2 and the measured activity at time point 1. Standard (left) and logarithmic (right)
plots are shown to illustrate piecewise nature of the individual curve phases.

508 Supplementary Figure 1: Time-activity curve approximated for data with greatest uptake measured at 509 the final time point  $c_3$ . Physical decay is assumed beyond and a single uptake phase may be used to

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approximate the kinetics between t=0 and  $c_3$ . Dotted line represents the late-phase retention beyond c<sub>3</sub>. On right plot, separate phases are plotted individually; uptake phase shown as dashed line. The resulting time-activity curve is shown as solid line against measured values on left.

513 Supplementary Figure 2: Example of serial activity measurements requiring conditional adjustment to 514 solve analytical time-activity curve. This may occur due to image alignment issues or noise and is 515 unlikely to represent true physiology. Here the activity declines at  $c_2$  and increases again at  $c_3$ . This 516 may be detected by conditional statement and the measurement  $c_2$  is adjusted to match the slope for 517 very near physical clearance between time-points  $c_2$  and  $c_3$ . The piecewise solving process may then 518 proceed as normal.

Supplementary Figure 3: A second pattern of measurement that may be detected by conditional statement. By first shifting the measured activity at  $c_2$  to the linear interpolation between  $c_1$  and  $c_3$ , solving with the piecewise algorithm approximates the behaviour of a least-squares optimiser, yielding a curve that is a compromise of early measured data.

523 Supplementary Figure 4: Initial preconditioning of values with very low measurements relative to the 524 second time point. These tend to occur in low-uptake regions or where there are errors in image 525 alignment and this may prevent calculation of very large exponential decay slopes.

Supplementary Figure 5: Calculation of comparison values c<sub>2,plateau</sub> and c<sub>2, linear</sub> which may be employed
 to handle unrealistic cases (eg. high-low-high uptake).

528 Supplementary Figure 6 - Primary flow-chart for solving time-activity curve as a two- or three-phase 529 exponential decay curve. Note: the common case with one uptake phase and two separate clearance

530 components is denoted in bold.

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Table 1 - Estimated time-integrated activity for representative cohort of <sup>177</sup>Lu-DOTA-Octreotate therapies as computed using proposed tri-exponential algorithm, Voxel-based Multimodal, and simplified piecewise with single late-phase exponential methods. Results are provided based on curves computed at the voxel level (mean of all curves) and additionally based on a single curve for each organ using the mean activity concentration at each timepoint.

	Mean Time-					
	Integrated					
	Activity					
	Concentration					
	(MBa*b/ml)					
	Vexel Level			1		
	voxer Lever:			whole Organ:		
	Tri-exponential	VoMM	Trapezoid +	Tri-exponential	<u>VoMM</u>	Trapezoid +
			Single			Single
			Exponential			Exponential
Marrow	2.78	2.52	2.95	2.78	2.86	2.88
Muscle	1.21	1.22	1.28	1.03	1.06	1.05
Lung	1.01	1.04	1.11	0.95	0.96	1.04
Heart	1.62	1.71	1.76	1.54	1.62	1.64
Stomach	14.92	13.86	15.57	14.03	13.51	14.39
Small	3.51	3.32	3.65	2.93	2.97	2.93
Bowel						
Liver	27.46	24.96	27.98	26.53	26.74	26.08
Pancreas	17.53	15.04	18.64	18.02	16.20	19.18
Spleen	56.26	52.05	57.64	53.43	53.82	52.54
Right	39.27	35.96	40.16	36.97	37.51	36.86
Kidney						
-						
Left	35.88	32.61	36.38	33.99	34.88	33.98
Kidnev						
Bladder	20.23	25.33	34.65	18.99	24.81	33.13
Lower	10.92	7.40	10.85	10.41	7.79	10.28
Large						
Intestine						
Intestine						
Upper	5.35	4.96	5.14	4.83	4.22	4.55
Largo						
intestine						
Tumer	207.02	200 70	245.00	220.06	247.05	251.05
rumor	321.03	290.79	343.99	330.20	347.20	551.05
1		1	1		1	

Table 2 - Median Voxel Level error as relative percentage at each of the three imaging time points. Note that the iterative solving method (VoMM) is biased toward reducing error at early images as when activity and associated calculation of residual error would be greatest. The proposed tri-exponential algorithm prioritizes accuracy for the second and third measurements with consideration of the late phase influence on the estimated time integral.

	4b		24h		72h	
	411		2411		7211	
	<u>Tri-</u>		<u>Tri-</u>		<u>Tri-</u>	
<u>Region</u>	<u>exponential</u>	<u>VoMM</u>	<u>exponential</u>	<u>VoMM</u>	<u>exponential</u>	VoMM
Marrow	5.0%	1.4%	10.3%	7.4%	0.0%	12.2%
Muscle	3.8%	0.5%	8.2%	3.9%	0.0%	11.7%
Lung	8.4%	0.1%	5.7%	1.2%	0.0%	9.3%
Heart	5.5%	0.1%	4.9%	1.1%	0.0%	9.2%
Stomach	8.5%	4.7%	6.3%	7.2%	0.2%	7.1%
Small Bowel	12.5%	1.9%	7.6%	7.5%	0.2%	14.8%
Liver	3.2%	0.4%	1.9%	1.4%	0.1%	2.5%
Pancreas	5.7%	4.5%	12.1%	7.2%	0.1%	7.9%
Spleen	4.2%	1.1%	2.8%	3.4%	0.1%	6.2%
Right Kidney	4.3%	0.5%	1.3%	2.3%	0.1%	13.8%
Left Kidney	4.2%	0.6%	1.6%	2.7%	0.0%	14.6%
Bladder	7.2%	0.0%	1.9%	0.6%	0.0%	51.2%
Lower Large Intestine	77.0%	13.7%	3.6%	13.4%	0.1%	10.0%
Upper Large Intestine	21.4%	5.9%	2.2%	8.0%	0.2%	16.7%
Tumor	15.9%	4.7%	8.5%	7.3%	0.3%	15.2%

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