

## Optimisation of photosynthetic carbon gain and within-canopy gradients of associated foliar traits for Amazon forest trees

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**Abstract.** Vertical profiles in leaf mass per unit leaf area ( $M_A$ ), foliar  $^{13}\text{C}$  composition ( $\delta^{13}\text{C}$ ), nitrogen (N), phosphorus (P), carbon (C) and major cation concentrations were estimated for 204 rain forest trees growing in 57 sites across the Amazon Basin. Data was analysed using a multilevel modelling approach, allowing a separation of gradients within individual tree canopies (within-tree gradients) as opposed to stand level gradients occurring because of systematic differences occurring between different trees of different heights (between-tree gradients). Significant positive within-tree gradients (i.e. increasing values with increasing sampling height) were observed for  $M_A$  and  $[\text{C}]_{\text{DW}}$  (the subscript denoting on a dry weight basis) with negative within-tree gradients observed for  $\delta^{13}\text{C}$ ,  $[\text{Mg}]_{\text{DW}}$  and  $[\text{K}]_{\text{DW}}$ . No significant within-tree gradients were observed for  $[\text{N}]_{\text{DW}}$ ,  $[\text{P}]_{\text{DW}}$  or  $[\text{Ca}]_{\text{DW}}$ . The magnitudes of between-tree gradients were not significantly different to the within-tree gradients for  $M_A$ ,  $\delta^{13}\text{C}$ ,  $[\text{C}]_{\text{DW}}$ ,  $[\text{K}]_{\text{DW}}$ ,  $[\text{N}]_{\text{DW}}$ ,  $[\text{P}]_{\text{DW}}$  and  $[\text{Ca}]_{\text{DW}}$ . But for

$[\text{Mg}]_{\text{DW}}$ , although there was no systematic difference observed between trees of different heights, strongly negative within-tree gradients were found to occur.

When expressed on a leaf area basis (denoted by the subscript “A”), significant positive gradients were observed for  $[\text{N}]_A$ ,  $[\text{P}]_A$  and  $[\text{K}]_A$  both within and between trees, these being attributable to the positive intra- and between-tree gradients in  $M_A$  mentioned above. No systematic within-tree gradient was observed for either  $[\text{Ca}]_A$  or  $[\text{Mg}]_A$ , but with a significant positive gradient observed for  $[\text{Mg}]_A$  between trees (i.e. with taller trees tending to have a higher Mg per unit leaf area).

Significant differences in within-tree gradients between individuals were observed only for  $M_A$ ,  $\delta^{13}\text{C}$  and  $[\text{P}]_A$ . This was best associated with the overall average  $[\text{P}]_A$  for each tree, this also being considered to be a surrogate for a tree’s average leaf area based photosynthetic capacity,  $A_{\text{max}}$ . A new model is presented which is in agreement with the above observations. The model predicts that trees characterised by a low upper canopy  $A_{\text{max}}$  should have shallow, or even non-existent, within-canopy gradients in  $A_{\text{max}}$ , with optimal intra-canopy gradients becoming sharper as a tree’s



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upper canopy  $A_{\max}$  increases. Nevertheless, in all cases it is predicted that the optimal within-canopy gradient in  $A_{\max}$  should be substantially less than for photon irradiance. Although this is also shown to be consistent with numerous observations as illustrated by a literature survey of gradients in photosynthetic capacity for broadleaf trees, it is also in contrast to previously held notions of optimality. A new equation relating gradients in photosynthetic capacity within broadleaf tree canopies to the photosynthetic capacity of their upper canopy leaves is presented.

## 1 Introduction

It has long been observed that the light saturated photosynthetic rates of leaves located low in plant canopies can be much less than leaves receiving much more irradiance ( $Q$ ) higher up (Jarvis et al., 1976), and this has been typically attributed to gradients in foliar nitrogen contents on a leaf area basis (Field, 1983). Nitrogen is a critical component of the photosynthetic apparatus (Evans, 1989) and it has been shown that the theoretically optimal distribution of nitrogen concentration which maximizes canopy photosynthesis is that where the foliar nitrogen concentration gradient (leaf area basis) closely follows the distribution of  $Q$ , thus approaching zero when  $Q$  also does (Field, 1983; Chen et al., 1993). Nevertheless, one regular observation in tree canopies is that vertical gradients in photosynthetic capacity are much less than that associated with the optimal distribution maximising individual plant carbon gain (e.g. Hollinger, 1996; Kull and Niinemets, 1998; Meir et al., 2002; Wright et al., 2006).

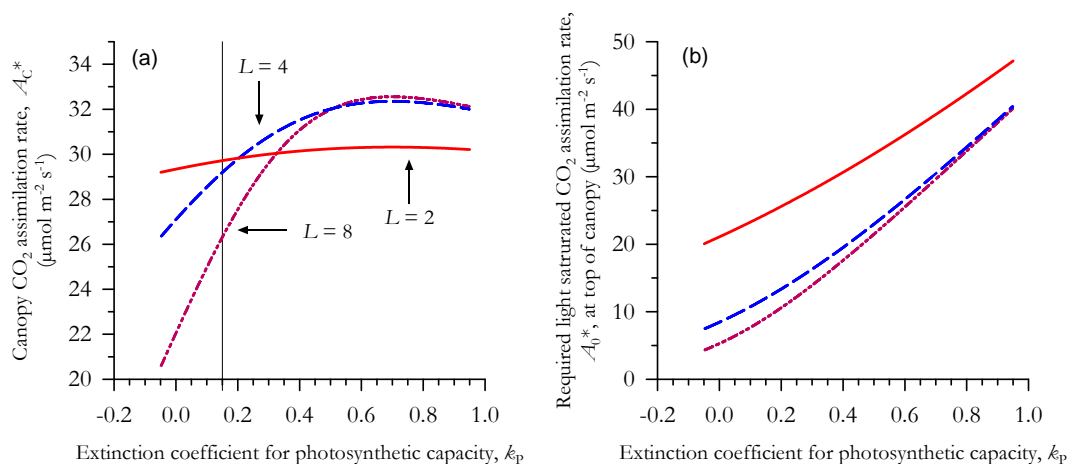
Understanding and quantifying within-canopy gradients in photosynthetically important nutrients and associated changes in plant physiological properties is also important for simulating rates of canopy photosynthesis and the associated light response (Lloyd et al., 1995; Haxeltine and Prentice, 1996; de Pury and Farquhar, 1997; Mercado et al., 2009) as well as for simulations of canopy leaf areas (themselves affecting predicted rates of photosynthetic carbon gain) in dynamic vegetation models (Sitch et al., 2003; Woodward and Loomis, 2004). Within tropical forest canopies, this variation may be expected to be especially complicated due to the very high number of species present in any one forest with an associated high tree-to-tree variation (Fyllas et al., 2009), some of which can be related to asymptotic tree height (Lloyd et al., 1995; Thomas and Bazzaz, 1999; Rijkers et al., 2000), successional status (Popma et al., 1992; Reich et al., 1995) and/or shade tolerance (Turner, 2001). Mean vertical variations in nutrient concentrations and associated physiological characteristics within tropical forests may thus be as much due to tree-to-tree variations correlated with actual or greater osmotic potentials tree height as with variations within individual trees themselves.

Nitrogen need not, of course, always be the primary limiting nutrient for photosynthesis in higher plants (Field and Mooney, 1986). This may be especially the case for tropical forest trees whose photosynthetic rates may be more closely correlated with foliar phosphorus content (Cromer et al., 1993; Raaijmakers et al., 1995; Reich et al., 1995; Lovelock et al., 1997; Domingues et al., 2010).

Associated with within-canopy gradients in photosynthetic capacity may also be gradients in foliar  $\delta^{13}\text{C}$  which, rather than reflecting a substantial recycling of  $^{13}\text{C}$  depleted carbon dioxide lower down plant canopies, probably reflects genuine vertical gradients in physiological processes for tropical forests (Lloyd et al., 1996). This could be attributable to upper canopy leaves being exposed to more severe water deficits during the day (Niinemets et al., 2004), though for conifers at least, it is also associated with variations in foliar nitrogen concentrations (leaf area basis), and by implication variations in photosynthetic capacity (Dursma and Marshall, 2006).

Although not yet studied in any great detail to date, gradients in foliar cations within plant canopies also occur. For example, Grubb and Edwards (1982) found magnesium concentrations (dry weight basis) to decrease with height for a New Guinea montane rain forest, attributing this to the central role of Mg within chlorophyll complex and the tendency for shaded leaves to have higher chlorophyll concentrations (again, expressed on a dry weight basis) than more exposed leaves higher up (Björkman et al., 1981). Gradients in other physiologically important cations might also be anticipated. For example, potassium has a critical role, not only in stomatal function, but also as an important foliar osmoticum (Leigh and Wyn-Jones, 1984), potentially being required in higher concentrations for leaves towards the top of the canopy where gas exchange rates would be expected to be higher (Carswell et al., 2000) and with the leaves there also tending to have greater osmotic potentials (Oberbauer et al., 1987).

We here analyse vertical variations in leaf properties for 204 trees sampled at a range of locations across Amazonia, attempting to quantify variations in nitrogen, phosphorus, major cations (Ca, Mg and K), carbon stable isotope composition and  $M_A$  with height. As well as analysing this observational data, we also present a new model which shows that the true “optimal” gradient in plant canopies does not necessarily mimic the gradient in  $Q$ . This model, described immediately below, is predicated on the observation that foliar leaf nutrient concentrations are to a large degree genetically constrained (Fyllas et al., 2009) and thus for any given species there is a practical limit for the maximum nutrient concentration possible. Once this is taken into account, it emerges that trees with a low overall photosynthetic potential should have a shallow (or even zero) decline in photosynthetic capacity with canopy depth, with higher photosynthetic capacity trees having sharper gradients for the optimisation of canopy photosynthesis. But with the predicted optimal gradients still



**Fig. 1.** Effect of variations in extinction coefficient for photosynthetic capacity,  $k_p$  at a range of different leaf area indices,  $L$ , for an overall canopy photosynthetic capacity ( $C_C$ ) of  $42 \mu\text{mol m}^{-2} \text{s}^{-1}$  (ground area basis) and at an incoming photon irradiance of  $2000 \mu\text{mol m}^{-2} \text{s}^{-1}$  (a) Variations in canopy  $\text{CO}_2$  assimilation rate (in the absence of any leaf respiration); (b) required  $\text{CO}_2$  assimilation rate for the uppermost canopy leaves ( $A_0^*$ ) in order to fulfill the requirements of Eq. (1).

substantially shallower than the within-canopy light profile. Data from a range of Amazon forest trees presented here suggests this to be the case, with these results also being confirmed through a global survey of vertical gradients of photosynthetic capacity within the canopies of broadleaf trees and forests.

## 2 Theoretical considerations

The model used to evaluate the optimal distribution of resources for species of a fixed maximum photosynthetic capacity is outlined in Appendix A. In short, it consists of the use of integral equations combining gradients in photosynthetically active radiation,  $Q$ , photosynthetic capacity,  $A_{\text{max}}$ , and leaf respiration,  $R$ , throughout plant canopies, also allowing for leaf respiration rates to be reduced at higher irradiances (Atkin et al., 2000). Gradients in  $Q$  and  $A_{\text{max}}$  are expressed in terms of exponential decay coefficients and are expressed as a function of canopy depth, this being defined for any point within the canopy ( $z$ ) as the cumulative leaf area index measured downwards from the canopy top. That is to say,  $z=0$  for the uppermost leaves of the canopy and  $z=L$  for the lowermost canopy leaves, with  $L$  being the canopy leaf area index.

### 2.1 Simulations with a canopy of fixed photosynthetic capacity

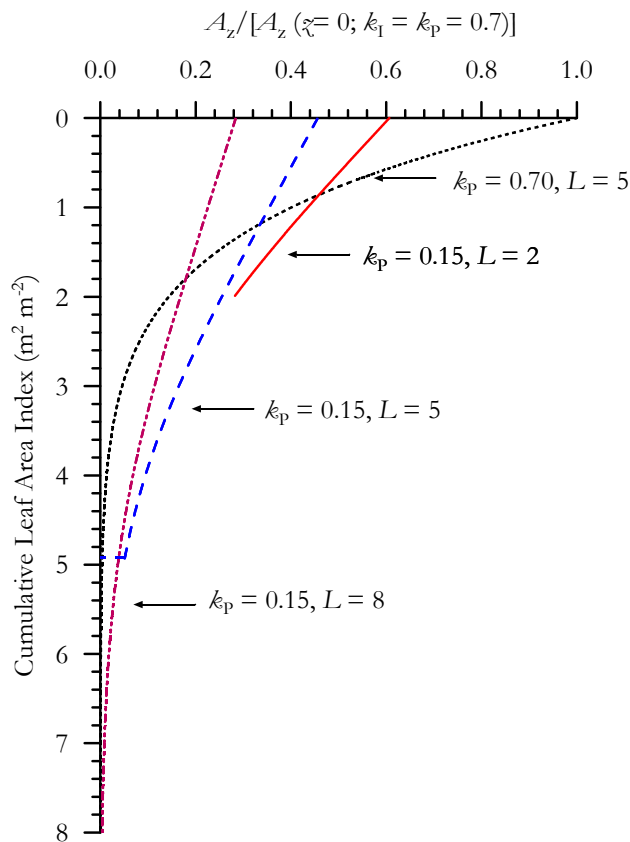
We first apply the model above to a rain forest canopy with  $L$  of either 2.0, 5.0 or 8.0, but in all cases having the same photosynthetic capacity, denoted here as  $C_C$ . To obtain a realistic estimate of the latter, we take representative observational values from data presented by Domingues et al. (2005)

for a forest near Tapajós (Para State, Brazilian Amazon) viz.  $L=5.5$ ,  $A_0^*=12.0 \mu\text{mol m}^{-2} \text{s}^{-1}$  (full sunlight) and with an extinction coefficient for photosynthetic capacity,  $k_p$ , of 0.15. Taking then a simple integral equation of the  $A_{\text{max}(z)}$  term in Eq. (A2), we obtain

$$C_C = A_0^* e^{-k_p z} \Big|_{z=0}^{z=L} = \frac{A_0^* (1 - e^{-k_p L})}{k_p}, \quad (1)$$

where  $A_0^*$  is the maximum (light saturated)  $\text{CO}_2$  assimilation rate at the top of the canopy, with the superscript “\*” indicating that we are ignoring dark respiration. This yields  $C_C=42 \mu\text{mol m}^{-2} \text{s}^{-1}$  (ground area basis).

Now, keeping this canopy photosynthetic potential constant, the first question we ask in a series of investigative simulations is how should the canopy photosynthetic rate,  $A_C^*$ , vary across a range of potential  $k_p$ ? And how is this variation in  $A_C^*$  with  $k_p$  influenced by  $L$ ? To do this we use Eqs. (A4) and (A5) as detailed in Appendix A. For these simulations, we always use a value for the light extinction within the canopy of  $k_1=0.7$  as reported for tropical forest (Wirth et al., 2001). Because  $C_C$  is held constant for all simulations, this requires that  $A_0^*$  varies as  $k_p$  changes. This is achieved via a rearrangement of Eq. (1); viz.  $A_0^*=k_p C_C / (1 - e^{-k_p L})$ . Using the above procedure, we can thus estimate how  $A_C^*$  and  $A_0^*$  should vary with  $k_p$  for a given  $L$  and this is shown in Fig. 1. Figure 1a shows that, as expected from theory (Field, 1983), the maximum  $A_C^*$  is indeed always observed when  $k_1 = k_p = 0.7$ . Also as expected, the higher the  $L$ , the greater the  $A_C^*$  at this optimum  $k_p$ . But as  $k_p$  declines (or increases) away from the optimum 0.7 value, the decline in  $A_C^*$  is much greater at higher  $L$ . So much so that at  $k_p=0.15$   $A_C^*$  actually declines with increasing  $L$ .



**Fig. 2.** Variations in the rate of photosynthesis at canopy depth  $z$  in the absence of dark respiration,  $A_z^*$ , normalised to that which would occur at the top of the canopy when the extinction coefficient for photosynthetic capacity,  $k_p$ , is equal to that for light,  $k_l$  which has in this case been set at 0.7. Values are shown for different combinations of  $k_p$  and leaf area index,  $L$ , at an incoming photon irradiance of  $2000 \mu\text{mol m}^{-2} \text{s}^{-1}$ .

Figure 1b shows the changes in  $A_0^*$  required to satisfy Eq. (1) with  $C_C$  conserved. As  $k_p$  increases then so does  $A_0^*$ . Likewise, at any given  $k_p$  then if  $A_0^*$  is lower then a higher  $L$  is required. As has already been pointed out by Pons et al. (1990) for herbaceous species and Hollinger (1994) for the New Zealand tree *Nothofagus fusca*, Fig. 1b implies that there are certain combinations of  $A_0^*$ ,  $k_p$  and  $C_C$  which may not be physiologically realistic. For example, most tropical tree species have maximum photosynthetic rates substantially less than  $20 \mu\text{mol m}^{-2} \text{s}^{-1}$  (Turner, 2001, p. 97; Domingues et al., 2010). Thus an “optimum”  $k_p$  may not be possible in the case of Fig. 1b unless  $C_C$  were substantially lower (see Eq. 1). But this would then mean that  $A_C^*$  was also correspondingly reduced (again as shown in Sect. 2.3). This contradiction is the fundamental reason why “optima”  $k_p$  as implied by Fig. 1a are not, in fact, optimal at all. That is to say, if one accepts that there is a fundamental limit to the maximum photosynthetic rate possible for any given species (see also Sect. 6.1), then the sharp “optimum”  $k_p$  required for

the gradient in photosynthetic capacity to match that of the light environment actually gives rise to a significantly lower canopy photosynthetic capacity were  $k_p$  to be substantially lower.

But why, despite higher canopy light interception, does  $A_C^*$  decline with increasing  $L$  at low  $k_p$ ? This also turns out to be critical in Sect. 2.3 in determining what is the optimum  $L$  when  $C_C$  and  $A_0^*$  are taken as fixed. The answer can be seen from Fig. 2. Here, the required gradients in  $\text{CO}_2$  assimilation rate in the absence of dark respiration ( $A^*$ ) at depth  $z$ ,  $A_z^*$ , are shown for various combinations of  $k_p$  and  $L$  with all values standardised to  $A_0^* = 1.0$  when  $k_l = k_p = 0.7$ . As would be expected from Fig. 1b, when  $k_p < 0.7$  then  $A_0^*$  is also less than this “optimal case” and as  $L$  increases the greater is the reduction in  $A_0^*$ . The vertical variation photosynthetic losses or gains associated with  $k_p \neq 0.7$  can also easily be seen by comparing the  $A_z^*$  profiles for  $k_p = 0.15$  with that for  $k_p = 0.7$ . This shows that, irrespective of  $L$ , and as would be expected, that  $A_z^*$  is lower towards the top of the canopy for lower  $k_p$ , but that this is to some degree compensated for by a greater  $A_z^*$  lower down. What can be seen from Fig. 2, however, is that the extent to which this higher  $A_z^*$  lower down in the canopy can compensate for lower  $A_z^*$  towards the top diminishes as  $L$  increases. As to why this occurs can be deduced from Fig. 1b. Because the high  $L$ /low  $k_p$  combination necessitates a low maximum photosynthetic capacity in the upper layers, much of the relatively high  $Q$  there cannot be utilised. On the other hand, a substantial proportion of the extra photosynthetic capacity lower down is more or less wasted as  $\text{CO}_2$  assimilation rates at low  $Q$  are much less dependent on  $A_{\text{max}(z)}$  (Fig. A1b). It is for this reason, as has also been noted by Hirose and Werger (1987), that the reduction in  $A_C^*$  as  $k_p$  deviates from its “optimum value” increases as  $L$  increases.

It is also worthwhile pointing out at this stage that the higher the value of  $A_0^*$  the greater the relative cost for any imbalances in the light versus photosynthetic capacity gradients at any given  $L$ . This is because any removal of photosynthetic capacity away from the top of the canopy results in a proportionally greater loss in  $A_C^*$  for high capacity as opposed to low capacity trees (see Fig. A1b).

## 2.2 What constitutes the optimal combination of $L$ and $k_p$ ?

As argued above in Sect. 2.1, due to the high  $A_0^*$  required, what is often considered the “optimum”  $k_p$  may in fact not even be physiologically possible, especially when observation based values of  $C_C$  and  $L$  are employed. Indeed, it can even be argued that for such cases the “optimality” question may have been inappropriately posed. This is because, rather than asking what the optimum profile in photosynthetic capacity should be for given values of  $L$  and  $C_C$ , one should rather be inquiring as to, given the considerable genetic and environmental limitations on  $A_0^*$  that undoubtedly

occur (e.g. Wright et al., 2004; Fyllas et al., 2009); *What is the combination of  $L$ ,  $C_C$  and  $k_P$  that serves to maximise the net carbon gain of the canopy for any given value of  $A_0^*$ ?*

Such a simulation requires that one looks at timescales greater than hours or days, and so we drive the model using a dataset collected above the 87 km tower at Tapajós (Goulden et al., 2004) consisting of about 3.8 years of net (incoming less reflected)  $Q$  averaged over hourly times steps and running from 1 July 2000–11 March 2004. Using different symbols to identify the much longer timescales we are now working at, we write

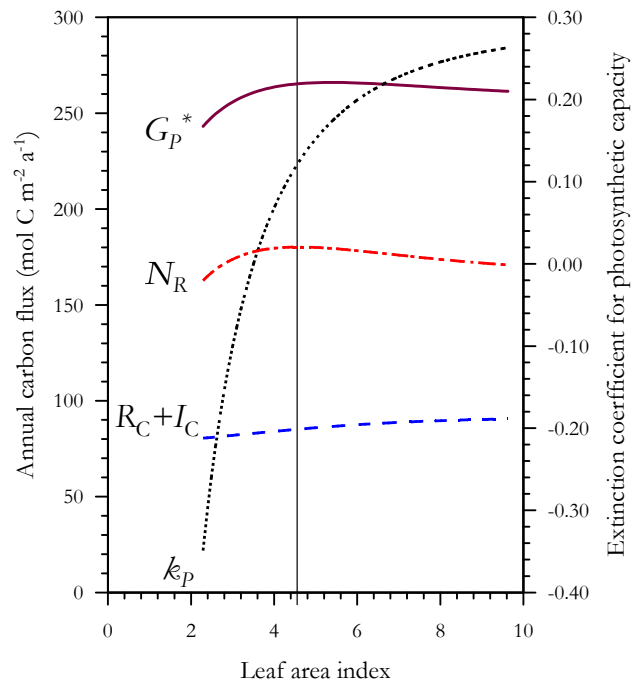
$$N_R = G_C^* - R_C - I_C, \quad (2)$$

where  $N_R$  is the net carbon gain to the canopy provided by the foliage on an annual basis, after accounting for the investment of carbon as new leaves within the plant canopy ( $I_C$ ) with  $R_C$  representing the annual respiratory losses by the canopy (estimated as detailed below) and  $G_C^*$  being the annual net carbon gain (Gross Primary Productivity) by the leaves in the absence of respiration in either the dark or the light. The latter is equivalent to  $A_C^*$ , calculated hourly, but summed over one year.

Noting also that elements such as nitrogen and phosphorus which are likely to be the key modulators of variations in  $A_{\max(z)}$  tend to stay constant on a dry weight basis with depth within the canopy and with variations on an area being due to variations in leaf mass per unit area ( $M_A$ ), see Sect. 5.2 for Amazon trees and Sect. 6.1 for a general discussion, then it follows that the decline in C investment per unit leaf area with canopy depth should approximate that of the decline in photosynthetic capacity and it then follows that we can simply express  $I_C$  as

$$I_C = I_0 e^{-k_P z} \Big|_{z=0}^{z=L} = \frac{I_0(1 - e^{-k_P L})}{k_P}. \quad (3)$$

To estimate  $I_0$  we assume an average leaf lifetime ( $\tau$ ) of one year and taking typical values of  $M_A$  and carbon content for upper canopy leaves at Tapajós (88.5 g m<sup>-2</sup> and 491 mg g<sup>-1</sup>, respectively) also accounting for construction respiration costs as in Masle et al. (1990) we obtain an estimate for  $I_0$  of 4.5 mol C m<sup>-2</sup> for an  $A_0^*$  of 12 μmol m<sup>-2</sup> s<sup>-1</sup>. Given that there is generally little correlation between photosynthetic capacity and  $M_A$  when the former is calculated on an area basis (Wright et al., 2004) we thus make  $I_0$  independent of  $A_0$  and as a simplification (also noting that it has no effect on the main conclusions of these simulations) we also make  $\tau$  independent of  $A_{\max}$  and  $I_0$  (For a further discussion of the effects of these and other assumptions, see Sect. 6.3).  $A_C^*$  is calculated as in Eq. (A4) or Eq. (A5) and integrated annually to obtain  $G_C^*$ . Based on data of Domingues et al. (2005) night time respiration ( $R_n$ ) is simply calculated as 0.08  $C_C^*$  but with daytime respiration by the leaves within the canopy dependent upon the illumination received. The extent of any decline in leaf respiration rates during the day is

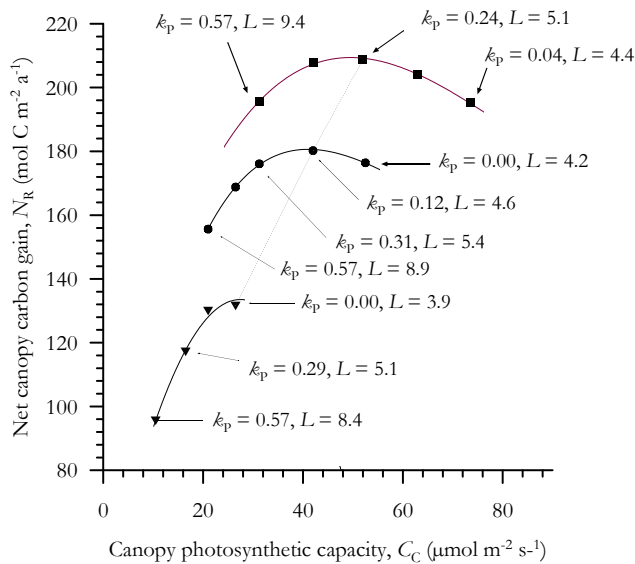


**Fig. 3.** Variations in the rate of Gross Primary production (in the absence of any leaf respiration in the light),  $G_P^*$ , the sum of leaf respiration (day and night) plus investment costs in leaf construction ( $R_C + I_C$ ) and the difference between the two, the annual net carbon gain of the canopy,  $N_R$  as defined through Eq. (2) as a function of leaf area index,  $L$ . Associated variations in the extinction coefficient for photosynthetic capacity,  $k_P$ , are also shown, with the vertical line indicating the  $L$  associated with the maximisation of  $N_R$ .

specified to be through a parameterisation of data presented by Atkin et al. (2000) as specified in Eq. (A7) or Eq. (A8) and as shown in Fig. A1b. The  $R_C$  values in Eq. (2) represent average annual sums.

Results from such a simulation are shown in Fig. 3 for our standard Tapajós conditions of  $A_0^* = 12 \mu\text{mol m}^{-2} \text{s}^{-1}$  and  $C_C = 42 \mu\text{mol m}^{-2} \text{s}^{-1}$ . To create the curves,  $k_P$  has been increased in increments starting from a value of  $-0.35$ , with each output increment calculated to be sufficient to increase  $L$  by about 0.1. This has been achieved through  $L$  being calculated via a simple rearrangement of Eq. (1).

As  $k_P$  is increased, the gradient away from the top of the canopy must by definition become sharper. And associated with this an increase in  $L$  is required; this being necessary to “hold” the same  $C_C$  within a greater leaf area. Figure 3 shows that associated with this increase in  $k_P$  and  $L$  is first an increase in  $G_C^*$  associated with an increase in light interception. Nevertheless, as  $L$  increases above a value of  $\sim 5.4$  in this simulation,  $G_C^*$  begins to decline. This is because the aggravating effects of higher  $L$  on  $k_P/k_1$  imbalances as demonstrated in the previous Section (Fig. 2) outweigh the increasingly diminishing advantage of increased light interception.



**Fig. 4.** Relationship between net canopy carbon gain (as defined by Eq. 2) and canopy photosynthetic capacity according to the model presented in Appendix A and Sect. 2. Curves shown are for different photosynthetic capacities,  $A_0^*$ , at the top of the canopy; ▼:  $A_0^*=6 \mu\text{mol m}^{-2} \text{s}^{-1}$ ; ●:  $A_0^*=12 \mu\text{mol m}^{-2} \text{s}^{-1}$ ; ■:  $A_0^*=18 \mu\text{mol m}^{-2} \text{s}^{-1}$ .

Although both  $I_C$  and night-time  $R_C$  do not change with the concurrent variations in  $k_p$  and  $L$ , daytime respiration increases. This is because associated with higher  $L$  are more and more leaves at very low light levels where the inhibition of daytime respiration is considerably reduced (Fig. A1a). Thus, the net carbon gain of the canopy,  $N_C$ , peaks at intermediate  $k_p$  and  $L$ : the optimum values from this simulation being 0.123 and 4.5, respectively. These values compare surprisingly favourably with what is actually observed for the Tapajós forest ( $k_p \sim 0.15$ ) as discussed above with  $L=5.1 \pm 0.5$  (Aragão et al., 2005). This may, however, be especially fortuitous because, as is discussed in Appendix B, there are good reasons to think that both  $L$  and  $k_p$  should actually be a little higher than the simple estimates predicted here. We also note that an estimate for  $G_C^*$  of  $262 \text{ mol C m}^{-2} \text{ a}^{-1}$  obtained from eddy covariance and other measurements at the Tapajós tower (Hutyra et al., 2007) is in remarkably good agreement with our model based estimate of  $G_C^*$  of  $265 \text{ mol C m}^{-2} \text{ a}^{-1}$  at  $L=4.5$ .

It is also worth noting that although  $k_p < 0.0$  (i.e. photosynthetic capacities increasing with canopy depth) is both mathematically and physiologically possible, it is also at odds with one central tenant of the approach here (viz. that  $A_0^*$  is a maximum physiologically constrained value). Thus, although included in Fig. 2 for illustrative purposes, in the simulations which follow we limit our interpretations to cases where  $k_p \geq 0.0$ .

### 2.3 What constitutes the optimal combination of $A_0^*$ and $C_C$ ?

In Sect. 2.2, we took our best estimate of the integrated canopy photosynthetic capacity for the Tapajós forest ( $A_0^*=12 \mu\text{mol m}^{-2} \text{s}^{-1}$  and  $C_C=42 \mu\text{mol m}^{-2} \text{s}^{-1}$ ) and found that, although effects of variations in  $L$  and  $k_p$  on  $G_C^*$ ,  $R_C$  and  $N_R$  were relatively modest, our model optimum  $N_R$  had associated with it values of  $G_C^*$ ,  $L$  and  $k_p$  that were surprisingly close to those actually observed. But what happens with other combinations of  $A_0^*$  and  $C_C$ ? To the extent that foliar nutrient concentrations are related to variations in leaf photosynthesis (Domingues et al., 2005, 2010; Mercado et al., 2009),  $A_0^*$  should reflect some combination of genetic and environmental influences (Fyllas et al., 2009). On the other hand, it might be reasonable to expect that the potential  $C_C$  for a given species would be more strongly influenced by edaphic conditions and/or climate than by genotype – this being mediated through variations in  $L$  and/or  $k_p$ .

To help answer this question, Fig. 4 shows the results of simulations where we have kept the model formulation and driving  $Q$  exactly as for Sect. 2.2, but investigating now how  $N_R$  varies for three different photosynthetic capacities at the top of the canopy, viz  $A_0^*=6 \mu\text{mol m}^{-2} \text{s}^{-1}$ ,  $12 \mu\text{mol m}^{-2} \text{s}^{-1}$  and  $18 \mu\text{mol m}^{-2} \text{s}^{-1}$  and for a variety of  $C_C$ , the range of which examined depends on the  $A_0^*$  investigated. This selection has occurred because a high  $A_0^*/C_C$  ratio leads to unreasonably high  $L$ . Conversely a low  $A_0^*/C_C$  leads to  $k_p < 0.0$ . In all cases, the symbol plotted reflects the value at the optimum  $N_R$  as determined from simulations such as shown in Fig. 3. Associated  $k_p$  and  $L$  are also shown for selected points.

This shows that, as might be anticipated, as  $C_C$  increases from the lowest values, then so does  $N_R$ . Associated with these increasing  $N_R$  are reductions in the optimal  $k_p$ . This allows a higher  $C_C$  to be more evenly distributed over a smaller  $L$ . Importantly, the lower  $L$  reduces overall respiratory losses. This is especially the case for high photosynthetic capacity leaves at the bottom of high  $C_C$  canopies. Yet, there is also a clear maximum for each  $A_0^*$ , beyond which  $N_R$  declines. This maximum occurs because the enhancement in  $G_C^*$  with higher  $C_C$  shows a shallower increment than the losses associated with  $R_C$ , including those at night. In short, above a certain point, little of the extra photosynthetic capacity can be put to good use. Though it still costs the tree in terms of respiratory carbon losses.

Not surprisingly, the  $C_C$  at which this point occurs increases with  $A_0^*$ ; this being associated with a higher  $L$  and a higher  $k_p$ . For  $A_0^*=6 \mu\text{mol m}^{-2} \text{s}^{-1}$  the optimal prediction is no gradient in photosynthetic capacity at all. This is because such a tree should maximise its annual carbon gain by compressing as much photosynthetic potential into as small a leaf area as possible. As  $A_0^*$  increases the predicted “optimal”  $k_p$  also increases as a partitioning of resources, more

in-line with the light distribution, assume relatively more importance. This also being associated with a higher  $L$ . But in no case is the predicted  $k_P$  even close to that of the light extinction coefficient ( $k_L=0.7$  in all simulations). Thus, our simulations here suggest that if physiological constraints on the maximum photosynthetic rate possible for upper-canopy leaves are taken into account along with the mutual dependencies of  $L$  and  $C_C$  and respiratory losses on  $k_P$ , then within canopy profiles of  $k_P$  should always be substantially less than  $k_L$ . This is because a low  $k_P$  gives a greater overall canopy photosynthetic capacity and thus a higher overall potential rate of carbon gain.

## 2.4 Model validation

For the remainder of this paper, we focus on gradients in key foliar properties such as leaf mass per unit area and foliar nitrogen and phosphorus concentrations within Amazon forest canopies. Taken together these three functional traits account for much of the variability in the photosynthetic rates of tropical trees (Domingues et al., 2010) thus providing good surrogates for variations in  $A_{\max(z)}$  (Sect. 5.3). Within the Discussion (Sect. 6.2), the extent to which the model accounts for variations observed for broadleaf tree  $k_P$  as a whole is also considered through a literature survey. Although variations in  $L$  are not explicitly considered in this data analysis, how model estimates of  $L$  and  $k_P$  may be modified by a consideration of evolutionarily stable versus instantaneous solutions (Anten, 2005) is considered in Appendix B.

## 3 Materials and methods

Of a total of 1508 trees sampled in 65 permanent plots in Brazil, Bolivia, Colombia, Ecuador, Peru and Venezuela between January 2002 and April 2005 for foliar nutrients and other properties (Fyllas et al., 2009; Patiño et al., 2009), 204 had also been sampled at three canopy heights for foliar nutrient composition, carbon and nitrogen isotope ratios and leaf mass per unit area ( $M_A$ ). Locations, vegetation and basic soil and climatological characteristics of the sample material plots are given in Patiño et al. (2009) and Quesada et al. (2010).

### 3.1 Leaf sampling

Twelve to 40 trees per plot had been chosen at random for collection of upper canopy leaves. A professional tree climber usually climbed three to eight trees in different points of the plot. From each climbed tree, branches of 1 to 2 m length from the exposed crown of two to four nearby trees were also usually harvested. For randomly selected trees (generally three trees per plot) branches were additionally collected from the middle (sunny-shaded) and from the lower canopy (shaded) portion of the canopy. Sampling was

achieved by severing a branch (usually ca. 4 cm in diameter) from the tree, this being subsequently allowed to fall to ground. From each branch a sub-sample was made, generally distal to the area of twig used by Patiño et al. (2009) for wood density analysis. One A4 sized plastic zip-bag of leaves of a range of possible different ages (but excluding obviously juvenile or senescent leaves) was then filled and sealed, kept as cool and shaded as possible, and then transported to the laboratory or field station the same evening as the day of collection.

### 3.2 Tree and canopy height determinations

The heights of both the lowest branch and canopy of sample trees were determined using a clinometer (Model PM5/360 PC, Suunto, Turku, Finland) with “middle canopy” leaves assumed to have been at the average crown height; calculated as the arithmetic mean of the upper and lower crown dimensions.

### 3.3 Leaf mass per unit area ( $M_A$ )

Sub-samples of 10–20 leaves were taken for the leaves collected from each tree/measurement height combination and imaged using a locally purchased document scanner attached to a Laptop or PC. The scanned images were then saved as image files with leaf area and other associated characteristics of each image subsequently analysed using *Win Folia Basic 2001a* (Regent Instruments, Quebec, QC, Canada). Scanning was usually done on the evening of collection, but when for logistical reasons this was not possible, leaves were stored in a cool, dry, and shaded place in tightly sealed plastic bags for a maximum of two days to avoid desiccation and any associated reduction of the leaf area.

Once scanned, leaves were air dried in the field or when an oven was available they were dried at 70°C for about 24 h or with a microwave oven in 5 min steps until death was considered to have been achieved. Once transported to the analysis laboratory leaves were redried at 70°C for about 24 h and their dry mass determined after being allowed to cool in a dessicator.

### 3.4 Sample preparation and analysis locations

Samples from Bolivia, Peru, Ecuador, Colombia and Venezuela were analysed in the Central Analytical and Stable Isotope Facilities at the Max-Planck Institute for Biogeochemistry (MPI-BGC) in Jena, Germany. Samples from the Brazilian sites were analysed for cations and phosphorus at the Instituto Nacional de Pesquisas da Amazônia (INPA) in Manaus and for carbon and nitrogen in the laboratory of the Empresa Brasileira de Pesquisa Agropecuária (EMBRAPA), also in Manaus. In both laboratories leaf sample not used for  $M_A$  determinations was dried as described above with a sub-sample of about 20 g DW then taken, for which the main

vein of all leaves was removed and the sub-sample subsequently ground. Sub-samples of ground material were also analysed for  $^{13}\text{C}/^{12}\text{C}$  ratios (Sect. 3.7), the Brazilian analyses being undertaken at the Centro de Energia Nuclear na Agricultura (CENA) in Piracicaba.

### 3.5 Carbon and nitrogen determinations

In both laboratories, analyses for C and N were carried out using 15–30 mg of finely ground plant material using a “Vario EL” elemental analyser (Elementar Analysensysteme, Hanau, Germany). Inter-laboratory consistency was maintained via the regular use of the same CRM 101 spruce needle (Community Bureau of Reference, BCR, Brussels, Belgium) and SRM 1573a tomato leaf (National Institute of Standards of Technology, Gaithersburg, MD, USA) standards in both laboratories. Within the Manaus laboratory, laboratory consistency with Jena values was also checked from time to time by the comparison of ground rain forest tree foliar material of various C and N concentrations previously analysed in Jena.

### 3.6 Cation and phosphorus determinations

In the Jena laboratory about 100 mg of sample material was first submitted to a microwave-assisted high pressure digestion (Multiwave, Anton Paar, Graz, Austria) after addition of 3 ml of 65%  $\text{HNO}_3$ . Maximum reaction temperature was 230 °C with maximum pressures of 25–30 bar. To check for possible contamination of reagents and vessels, a blank was run with each series of standard reference materials or samples. After digestion, blank solutions and samples (reference materials and plant samples) were transferred to 50 ml glass vessels which were filled to the mark with ultrapure water (Millipore, Eschborn, Germany) and analysed by ICP-OES (Model Optima 3300 DV, Perkin Elmer, Norwalk, CT, USA) with a 40 MHz, free-running RF-Generator and an array detector allowing for the simultaneous determination of the elements using wavelengths as given in Boumans (1987) and DIN EN ISO 11885 (1998). In the Manaus laboratory, concentrations of P, K, Ca and Mg were determined after digestion with a nitric/perchloric acid mixture as described in detail by Malavolta et al. (1989). Concentrations of K, Ca and Mg in the extracts were subsequently determined using an Atomic Absorption Spectrophotometer (Model 1100b, Perkin Elmer, Norwalk, CT, USA) as prescribed by Anderson and Ingram (1993). Phosphorus was determined by colorimetry (Olsen and Sommers, 1982) using a UV visible spectrophotometer (Model 1240, Shimadzu, Kyoto, Japan). As for the Jena laboratory, to check for possible contamination of reagents and vessels, a blank was run with each series of standard reference materials or samples. Inter-calibration between the two laboratories was achieved by the use of the same external and internal standards as for C and N (Sect. 3.5).

### 3.7 Carbon isotope determinations

In the Jena laboratory,  $^{13}\text{C}/^{12}\text{C}$  isotopes were measured as described in Werner and Brand (2001). In short: within the same sequence of analyses, bulk tissue samples, laboratory reference materials (including quality control standards) and blanks were combusted quantitatively using an NA 1110 elemental analyser equipped with an AS 128 autosampler (CE Instruments, Rodano, Italy) attached to a Delta-C isotope ratio mass spectrometer (Thermo-Finnigan MAT, Bremen, Germany) using a ConFlo III interface (Werner et al., 1999). In the CENA laboratory, Brazilian samples were analysed as described in Ometto et al. (2006). In brief, 1–2 mg of sample was combusted in an elemental analyser (CE Instruments, Rodano, Italy) coupled to an isotopic ratio mass spectrometer (IRMS Delta Plus, Thermo-Finnigan MAT, San Jose CA, USA) operating in continuous flow mode.

Inter-calibration exercises between MPI-BGC and CENA using secondary standards and other plant material showed small but significant and systematic differences between the two laboratories ( $r^2=0.99$ ). These have been corrected for here with results from the CENA laboratory adjusted to provide full isotope scale equivalence with the MPI-BGC results.

## 4 Statistical analysis

As we were interested in vertical variations in foliar characteristics with individual trees and variations in these characteristics between individual trees as a function of canopy height (and not so much concerned with plot-to-plot variations – these are considered in Fyllas et al., 2009) we used multilevel modelling techniques (Snijders and Bosker, 1999) treating both tree-to-tree variation (within a plot) and variations in overall mean values (between plots) as random (residual) effects. The Basin-wide average within- and between-tree gradients was thus determined according to

$$\Theta_{\ell\text{tp}} = \beta_{0\text{tp}} + \beta_1 h_{\ell\text{tp}} + \beta_2 h_c + R_{\ell\text{pt}}, \quad (4)$$

where  $\Theta_{\ell\text{tp}}$  can be taken to represent any physiological parameter of interest (measured on leaf “ $\ell$ ” within tree “ $t$ ” located within plot “ $p$ ”),  $\beta_{0\text{tp}}$  is an intercept term which, as indicated by its nomenclature, is allowed to vary both between trees and between individual plots,  $\beta_1$  is a coefficient that describes how  $\Theta$  varies with the height at which it was sampled (common to all leaves, trees and plots),  $\beta_2$  is an additional coefficient describing how  $\Theta_{\ell\text{tp}}$  varies with mean tree canopy height,  $h_c$ , and  $R_{\ell\text{tp}}$  is a residual term.

The tree and plot dependent intercepts can be split into an average intercept and group dependent deviations. Firstly we write

$$\beta_{0\text{tp}} = \delta_{00\text{p}} + U_{0\text{tp}}, \quad (5)$$

where  $\delta_{00\text{p}}$  is the average intercept for the trees sampled within each plot and  $U_{0\text{tp}}$  is a random variable controlling



for the effects of variations between trees (i.e. with a unique value for each tree within each plot). Likewise, we also write

$$\delta_{00p} = \gamma_{000} + V_{00p}, \quad (6)$$

where  $\gamma_{000}$  is the average intercept for the entire dataset and  $V_{00p}$  is a random variable controlling for the effects of variations between each plot (i.e. with a unique value for each plot). Using a general notation then, we can combine Eqs. (4–6) to yield

$$\Theta_{ltp} = \gamma_{000} + \gamma_{100}h_{lt} + \gamma_{010}h_c + V_{00p} + U_{0tp} + R_{ltp}, \quad (7)$$

where  $\gamma_{100}$  describes how variations in  $\Theta$  between leaves within a tree vary with canopy height (with the same value for all trees within all plots) and  $\gamma_{010}$  is a between-tree regression coefficient that describes how  $\Theta$  varies with the overall (mean) canopy height for each tree (with the same value applying to all trees within all plots). For the  $V_{00p}$  and  $U_{0tp}$ , just as is the case for the  $R_{ltp}$ , it is assumed they are drawn from normally distributed populations and the population variance of the lower level residuals ( $R_{ltp}$ ) is likewise assumed to be constant across trees. Note that within each plot the mean value of  $U_{0tp} \equiv 0$  and likewise the weighted mean value of  $V_{00p} \equiv 0$  for the dataset as a whole. As is the normal case in any regression model, for each tree the mean  $R_{ltp} \equiv 0$ .

Equation (7) is a “three-level random intercept model” with leaves (level 1) nested within trees (level 2) which are themselves nested within plots (level 3). Associated with the three residual terms there is variability at all three levels and we denote the associated variances as

$$\text{var}(R_{ltp}) = \sigma^2, \text{var}(U_{0tp}) = \tau^2, \text{var}(V_{00p}) = \phi^2. \quad (8)$$

The total variance between all leaves is  $\sigma^2 + \tau^2 + \phi^2$  and the population variance between trees is  $\tau^2 + \phi^2$ .

Equation (7) is flexible in that the within-tree regression coefficient is allowed to differ from the between-tree regression coefficient. In analogy with the two-level model derivation in Chap. 4 of Snijders and Bosker (1999) and considering the terms within a given tree, these terms can be re-ordered as

$$\Theta_{ltp} = (\gamma_{000} + \gamma_{010}h_c + U_{0tp} + V_{00p}) + \gamma_{100}h_{ltp} + R_{ltp}. \quad (9)$$

The random part between the parenthesis is the intercept for this tree and the regression coefficient for variation of  $\Theta$  with height within trees is  $\gamma_{100}$ . The systematic (non-random) part is the within-tree regression line

$$\Theta_{ltp} = (\gamma_{000} + \gamma_{010}h_c) + \gamma_{100}h_{ltp}. \quad (10)$$

On the other hand, considering only the relationship between the average value of  $\Theta$  within a canopy and the average canopy height,  $h_c$ , then Eq. (9) becomes

$$\Theta_{.tp} = \gamma_{000} + \gamma_{010}h_c + \gamma_{100}h_c + V_{00p} + U_{0tp}, \quad (11)$$

and the systematic part of the model can then be written as

$$\Theta_{.tp} = \gamma_{000} + (\gamma_{010} + \gamma_{100})h_c. \quad (12)$$

This shows that the between-tree regression coefficient in the random intercept model is  $\gamma_{010} + \gamma_{100}$ . Thus, when the relationship between any parameter  $\Theta$  and height is different for between-tree as opposed to within-tree variation in the analysis which follows then this means  $\gamma_{010}$  is significantly different from zero. Where this is not the case, any variation in  $\Theta$  with height is of a statistically similar magnitude irrespective of whether or not the source of variation is sampling at different heights within the one tree or comparing the average values for trees of different heights.

All analyses were undertaken with the *MLwinN* software package (Rabash et al., 2004). Heights were centered according to the mean tree height for the dataset (19.8 m) so the intercept estimates ( $\gamma_{000}$ ) given represent the estimated value of each  $\Theta$  at that height.

## 5 Results

### 5.1 Sources of variation

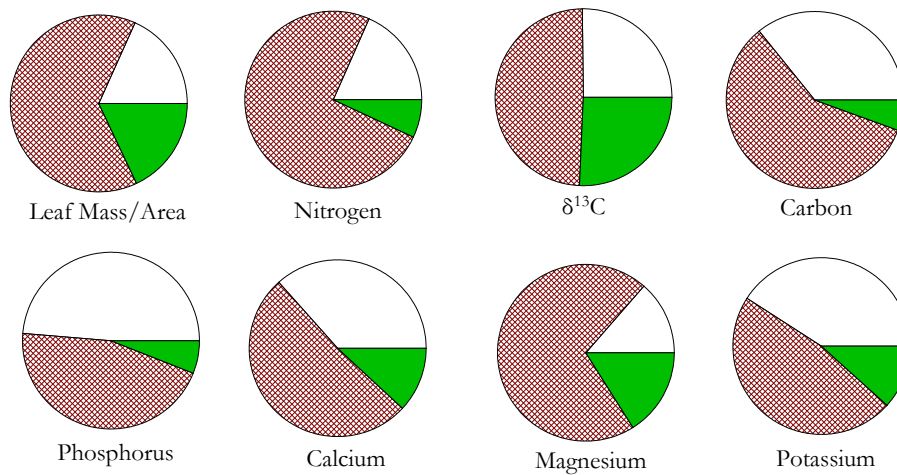
In order to examine the inherent sources of variability in the dataset, we first fitted a “null model” to untransformed data according to

$$\Theta_{ltp} = \gamma_{000} + V_{00p} + U_{0tp} + R_{ltp}. \quad (13)$$

From this model and Eq. (8) the contribution of variations within and between trees and plots to the overall variance within the dataset can be simply apportioned and the results are shown in Fig. 5. This shows that, without exception (using the subscript “DW” to denote concentrations are here being expressed on a dry-weight basis), the variability observed in the eight  $\Theta$  examined *viz.*  $M_A$  and  $\delta^{13}C$ ,  $[N]_{DW}$ ,  $[P]_{DW}$ ,  $[C]_{DW}$ ,  $[Ca]_{DW}$ ,  $[K]_{DW}$  and  $[Mg]_{DW}$  was greater between trees than the variance associated with the sampling of the three different heights within trees. Moreover, with the notable exception of  $[P]_{DW}$ , the between-plot variance was also generally less than the within-plot variance, the latter being associated with tree-to-tree variations within individual plots.

### 5.2 Vertical profiles

The underlying raw data giving rise to Table 1 and used in the subsequent multilevel analysis is shown in Fig. 6, with a different colour coding for the different regions. This “Jackson Pollock Plot” shows that, although there is considerable variability in the data, certain patterns exist. For example, on average there is a trend for an increase in  $M_A$  with increasing height and the opposite is the case for  $\delta^{13}C$ . On the other hand, generally speaking, concentrations in  $[N]_{DW}$  and  $[P]_{DW}$  are quite consistent within a given tree, although there are of course exceptions, especially at higher concentrations. Foliar carbon varies substantially between trees, and close examination shows that although usually very consistent within a given tree, there is often a slight tendency



**Fig. 5.** Partitioning of the observed variance in the dataset according to Eq. (13). Green = variability with height within individual trees; purple hatches; variability between trees within individual plots; white = variability between plots.

for  $[C]_{DW}$  to increase with height. Variations in  $[Mg]_{DW}$  were similar to  $[Ca]_{DW}$  and  $[K]_{DW}$  with no strong trend with height readily apparent.

From Fig. 6 it can be seen that there is considerable heteroscedasticity in the data with the variance of the dependent variables tending to increase with their absolute value but not with the value of the independent (height) variable. This was the case for all  $\Theta$  except maybe  $[C]_{DW}$  and  $\delta^{13}C$ . Moreover, an examination of residual variances showed marked departures from normality, even when plot-to-plot differences in overall mean values were taken into account. We therefore transformed all data (taking the absolute value of  $\delta^{13}C$ ) prior to analysis, fitting the equation

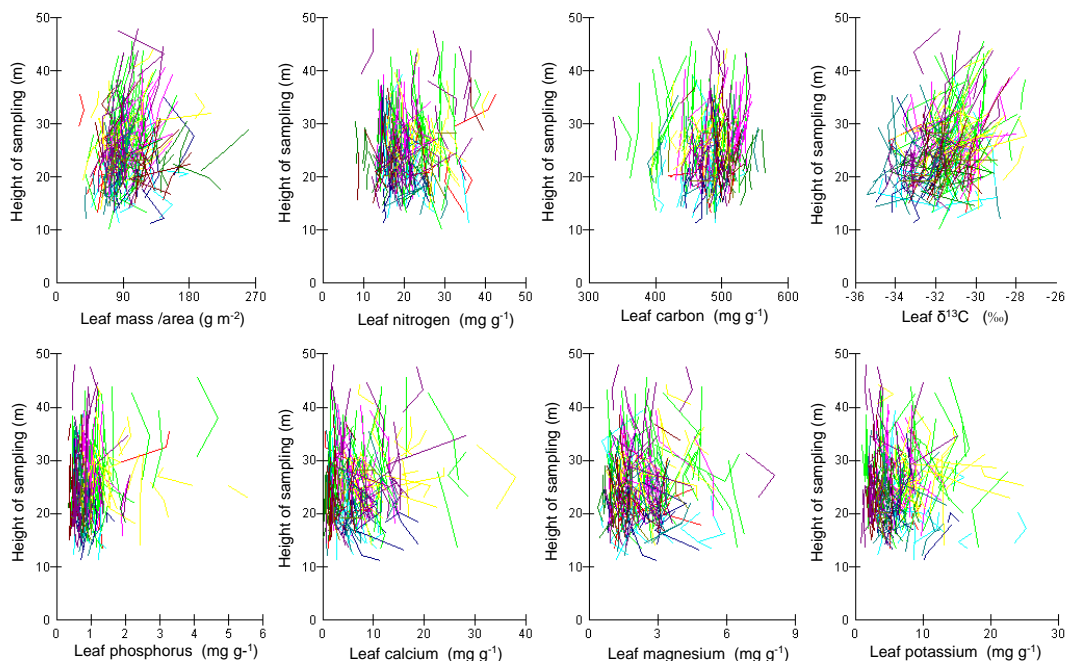
$$\log_e(\Theta_{\ell_{tp}}) = \gamma_{000} + \gamma_{100}h_{\ell_t} + \gamma_{010}h_c + V_{00p} + U_{0tp} + R_{\ell_{tp}}. \quad (14)$$

Noting that due to the logarithmic transform of the  $\Theta_{\ell_{tp}}$  terms, the height coefficients in Eq. (14) ( $\gamma_{10}$  and  $\gamma_{01}$ ) now refer to the proportional changes in the  $\Theta_{\ell_{tp}}$  with  $h_{\ell_t}$  and  $h_c$  per metre respectively, results are listed in Table 1. Here the null hypothesis that a certain regression parameter ( $\gamma_h$ ) is zero (i.e.  $H_0: \gamma_h=0$ ) can be tested according to a two tailed  $t$ -test,  $T$ , ( $\gamma_h$ )= $\hat{\gamma}_h/[S.E.(\hat{\gamma}_h)]$ , the so called *Wald test*. This indicates (as shown in bold font) that within tree canopy gradients were significantly different to zero only for  $M_A$ ,  $[C]_{DW}$ ,  $\delta^{13}C$  and  $[Mg]_{DW}$ . From Eq. (12), the parameter  $\gamma_{010}$  can be taken to reflect the difference between the within-tree and between-tree slopes and a separate Wald test can be used to determine if the overall coefficient for the between-tree coefficient ( $\gamma_{100} + \gamma_{010}$ ) is significantly different from zero (Snijders and Bosker, 1999). From such an analysis we conclude

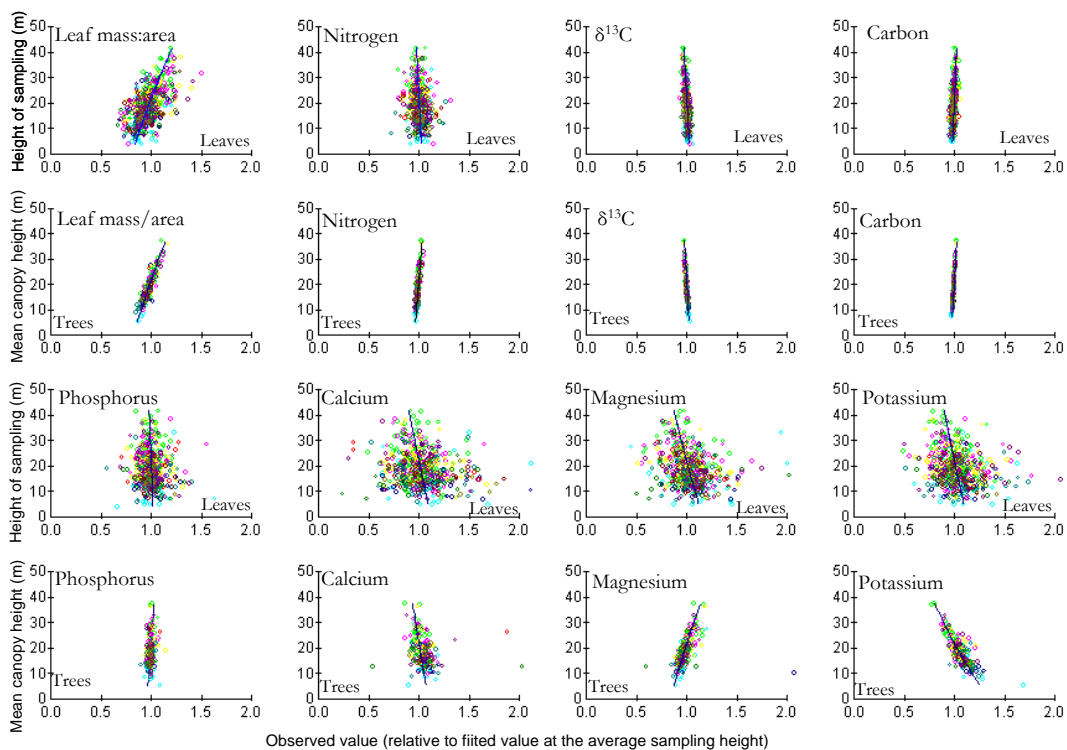
1. The between-tree coefficient for  $M_A$  is not significantly different to the within tree coefficient ( $P \leq 0.05$ ). Both are significantly different to zero ( $P \leq 0.05$ ) with  $M_A$  increasing with increasing height.

2. There is no detectable within-tree gradient for  $[N]_{DW}$ ,  $[P]_{DW}$  or  $[Ca]_{DW}$ . Nor is there any significant overall tendency for mean canopy  $[N]_{DW}$  or  $[P]_{DW}$  concentrations to increase with mean tree canopy height ( $P \geq 0.10$ ).
3. Foliar  $|\delta^{13}C|$  decreases with height irrespective of whether the source of variation is within-tree or between-tree. That is to say, taller trees have less negative  $\delta^{13}C$  than shorter trees and higher leaves also tend to have less negative  $\delta^{13}C$  than those lower down within the same tree. The gradients with height are similar for both sources of variation and are both significantly different from zero ( $P \leq 0.05$ ).
4. There is a significant tendency for  $[C]_{DW}$  to increase with height within an individual tree, and also for taller trees to have a higher foliar C content ( $P \leq 0.05$ ).
5. Although there is a significant tendency for  $[Mg]_{DW}$  to decrease with increasing height within a given tree ( $P \leq 0.05$ ), no such pattern is observed for the variation in  $[Mg]_{DW}$  between trees with  $(\gamma_{100} + \gamma_{010})/[S.E.(\hat{\gamma}_{h_c})]$   $T_{0.10}$ . Potassium also shows a significant tendency to decrease with increasing height within a given tree ( $P \leq 0.05$ ). Contrary to magnesium, this effect persists, or is perhaps even amplified when tree-to-tree variation is additionally considered.

Figure 7 shows the fitted slopes and the data, in all cases normalised to the fitted value for each tree at the average sampling height of 19.8 m. Here a comparison of the plots for within-tree and between-tree variation show the generally similar increases for  $M_A$  with height and decreases in  $\delta^{13}C$  and  $[C]_{DW}$  with height, irrespective of the source of variation. On the other hand, the much steeper gradient for  $[K]_{DW}$



**Fig. 6.** Vertical gradients in leaf mass per unit area,  $[N]_{DW}$ , leaf  $[C]_{DW}$ ,  $\delta^{13}C$ ,  $[P]_{DW}$ ,  $[Ca]_{DW}$ ,  $[Mg]_{DW}$  and  $[K]_{DW}$  for 204 trees sampled across Amazonia. Different colours refer to different regions.



**Fig. 7.** Observed values and fitted lines for within-tree gradients (“Leaves”) and tree-to-tree gradients (“Trees”) for leaf mass per unit area,  $[N]_{DW}$ ,  $[C]_{DW}$ ,  $\delta^{13}C$ ,  $[P]_{DW}$ ,  $[Ca]_{DW}$ ,  $[Mg]_{DW}$  and  $[K]_{DW}$  for 204 trees sampled across Amazonia. Different colours refer to different regions.

**Table 1.** Estimated intercept and coefficients according to Eq. (14) for leaf mass per unit area, leaf [N], leaf [C], leaf  $\delta^{13}\text{C}$ , leaf [P], leaf [Ca], leaf [Mg] and leaf [K] all expressed on a leaf dry weight basis. Significant values ( $P \leq 0.05$ ) are shown in bold.

	Log <sub>e</sub> [Leaf mass/area] (g m <sup>-2</sup> )		Log <sub>e</sub> [Nitrogen] (mg g <sup>-1</sup> )		Log <sub>e</sub>   $\delta^{13}\text{C}$   (‰)		Log <sub>e</sub> [Carbon] (mg g <sup>-1</sup> )	
Fixed effect	Coefficient	S. E.	Coefficient	S. E.	Coefficient	S. E.	Coefficient	S. E.
$\gamma_{000}$ = Intercept	4.560	0.0270	3.004	0.0267	3.673	0.0032	6.185	0.0077
$\gamma_{100}$ = Coefficient of $h$	<b>0.00981</b>	<b>0.00123</b>	-0.00121	0.00081	<b>-0.00151</b>	<b>0.00019</b>	<b>0.00114</b>	<b>0.00018</b>
$\gamma_{010}$ = Coefficient of ( $h_C-h$ )	0.00104	0.00354	0.00332	0.00329	0.00013	0.00048	0.00036	0.00082
Random Effect	Parameter	S. E.	Parameter	S. E.	Parameter	S. E.	Parameter	S. E.
$\varphi_0^2$ = between plot variance	0.01693	0.00689	0.01783	0.00689	0.00026	0.00009	0.00201	0.00058
$\tau_0^2$ = between-tree variance	0.06047	0.00757	0.05876	0.00711	0.00747	0.00010	0.00334	0.00041
$\sigma_0^2$ = within tree variance	0.01382	0.00099	0.00611	0.00044	0.00033	0.00002	0.00028	0.00003
	Log <sub>e</sub> [Phosphorus] (mg g <sup>-1</sup> )		Log <sub>e</sub> [Calcium] (mg g <sup>-1</sup> )		Log <sub>e</sub> [Magnesium] (mg g <sup>-1</sup> )		Log <sub>e</sub> [Potassium] (mg g <sup>-1</sup> )	
Fixed effect	Coefficient	S. E.	Coefficient	S. E.	Coefficient	S. E.	Coefficient	S. E.
$\gamma_{000}$ = Intercept	-0.1244	0.0508	1.532	0.098	0.6991	0.0485	1.646	0.070
$\gamma_{100}$ = Coefficient of $h$	-0.00107	0.00130	-0.00520	0.00320	<b>-0.00684</b>	<b>0.00218</b>	<b>-0.00538</b>	<b>0.00220</b>
$\gamma_{010}$ = Coefficient of ( $h_C-h$ )	0.00206	0.00460	0.00106	0.00937	<b>0.01490</b>	<b>0.00642</b>	-0.00853	0.00604
Random Effect	Parameter	S. E.	Parameter	S. E.	Parameter	S. E.	Parameter	S. E.
$\varphi_0^2$ = between plot variance	0.10919	0.02691	0.41396	0.09744	0.05785	0.02232	0.22444	0.04989
$\tau_0^2$ = between-tree variance	0.09322	0.01150	0.30900	0.04009	0.18150	0.02292	0.12120	0.01604
$\sigma_0^2$ = within tree variance	0.01519	0.00109	0.09229	0.00663	0.04282	0.00307	0.04371	0.00314

when between-tree variations are considered is also apparent as is a strong contrast in directions for  $[\text{Mg}]_{\text{DW}}$ . Taller trees tend to have slightly higher  $[\text{Mg}]_{\text{DW}}$ , but within individual trees  $[\text{Mg}]_{\text{DW}}$  declines with increasing height. Though not significant, the trends for slightly decreased  $[\text{N}]_{\text{DW}}$  and  $[\text{P}]_{\text{DW}}$  with height in individual tree canopies can also clearly be seen. Note that because all values are normalised to that of the fitted value at the average sampling height, the tree-to-tree variations appear in this graph to be much less than for the actual data themselves (see Fig. 6).

### 5.3 Area based profiles

Vertical variations in foliar nitrogen and/or phosphorus concentrations within plant canopies can be expected to substantially affect photosynthetic rates which are normally expressed per unit leaf area (Carswell et al., 2000; Domingues et al., 2005; Mercado et al., 2009; Domingues et al., 2010). It was thus also of interest to examine vertical gradients within and between trees also expressing nutrients on a leaf area basis (Table 2) – this simply being calculated as the product of the nutrient concentration (DW basis) and  $M_A$ , and with area based concentrations here identified by an “A” subscript. When done, this shows similar and significant within-tree positive gradients to exist for both  $[\text{N}]_A$  and  $[\text{P}]_A$ . The between-tree gradients are in both cases about 50% steeper than the within-tree gradients, but this difference is

not statistically significant. The negative gradient in  $[\text{C}]_A$  as on a DW basis is maintained, as is the positive gradient for  $[\text{K}]_A$ , though in the case of  $[\text{K}]_A$  the between-tree gradient is no longer statistically stronger than observed within individual trees. The pattern for magnesium is also very different on leaf-area versus dry-weight basis. The negative DW gradient (lower values higher up in the canopy) is counterbalanced by the positive gradient in  $M_A$  meaning that within individual tree canopies no gradient in  $[\text{Mg}]_A$  exists. On the other hand, the positive between-tree gradient in magnesium is amplified when expressed on an area basis, with taller trees having significantly higher  $[\text{Mg}]_A$  than their shorter counterparts.

Gradients for  $[\text{N}]_A$  and  $[\text{P}]_A$  are shown in Fig. 8, again with each tree having its value normalised to the fitted value at the average sampling height of 19.8 m. This illustrates the similar overall patterns observed for  $[\text{N}]_A$  and  $[\text{P}]_A$ , a result that is not surprising as a comparison of Fig. 8 with Fig. 7 in conjunction with Tables 1 and 2 shows that almost all the variation observed in  $[\text{N}]_A$  and  $[\text{P}]_A$ ; both within and between trees, is due to the increase in  $M_A$  with height with  $[\text{N}]_{\text{DW}}$  and  $[\text{P}]_{\text{DW}}$  staying more or less constant within a given tree and also showing no systematic variation with  $h_C$  when different trees within the one stand are compared.

**Table 2.** Estimated intercept and coefficients according to Eq. (14) for leaf [N], leaf [C], leaf [P], leaf [Ca], leaf [Mg] and leaf [K], all expressed on a leaf area basis. Significant values ( $P \leq 0.05$ ) are shown in bold.

	Log <sub>e</sub> [Nitrogen] (mg m <sup>-2</sup> )		Log <sub>e</sub> [Carbon] (mg m <sup>-2</sup> )		Log <sub>e</sub> [Phosphorus] (mg m <sup>-2</sup> )	
Fixed effects	Coefficient	S. E.	Coefficient	S. E.	Coefficient	S. E.
$\gamma_{000}$ = Intercept	7.572	0.021	10.75	0.011	4.448	0.0475
$\gamma_{100}$ = Coefficient of $h$	<b>0.00873</b>	<b>0.00136</b>	<b>-0.01112</b>	<b>0.00135</b>	<b>0.00893</b>	<b>0.00167</b>
$\gamma_{010}$ = Coefficient of $(h_C - h)$	0.00372	0.00351	0.00066	0.00426	0.00465	0.00398
Random Effects	Parameter	S. E.	Parameter	S. E.	Parameter	S. E.
$\varphi_0^2$ = between plot variance	0.00215	0.00463	0.02856	0.01155	0.09834	0.02210
$\tau_0^2$ = between-tree variance	0.05775	0.00773	0.06670	0.00850	0.05822	0.00782
$\sigma_0^2$ = within tree variance	0.01642	0.00135	0.01521	0.00119	0.02460	0.00226
	Log <sub>e</sub> [Calcium] (mg m <sup>-2</sup> )		Log <sub>e</sub> [Magnesium] (mg m <sup>-2</sup> )		Log <sub>e</sub> [Potassium] (mg m <sup>-2</sup> )	
Fixed effects	Coefficient	S. E.	Coefficient	S. E.	Coefficient	S. E.
$\gamma_{000}$ = Intercept	6.126	0.0979	5.268	0.0498	6.232	0.07187
$\gamma_{100}$ = Coefficient of $h$	0.00372	0.00234	0.00264	0.00244	<b>0.004425</b>	<b>0.00223</b>
$\gamma_{010}$ = Coefficient of $(h_C - h)$	-0.00156	0.00654	<b>0.01712</b>	<b>0.00700</b>	-0.00155	0.00654
Random Effects	Parameter	S. E.	Parameter	S. E.	Parameter	S. E.
$\varphi_0^2$ = between plot variance	0.3553	0.0915	0.05574	0.02276	0.3553	0.09146
$\tau_0^2$ = between-tree variance	0.3867	0.0538	0.18610	0.02458	0.3867	0.05381
$\sigma_0^2$ = within-tree variance	0.1072	0.0072	0.05135	0.00388	0.1072	0.00721

#### 5.4 Do tree-to-tree variations in within-canopy gradients exist?

The analysis so far has assumed that for all  $\Theta$  the within-tree gradients are the same for all plots and trees, but that different plots and the trees within them may assume different overall nutrient concentrations (a “random intercept model”) But, especially in light of the model results of Sect. 2 which suggest that trees with the highest photosynthetic capacity should have the highest within canopy extinction coefficients, it was also of interest to determine if gradients observed differed between trees, and if so, in a systematic way. Given the “noise” apparent in Fig. 6, this was obviously not an easy question to answer, but it was attempted by taking  $\beta_{1tp} = \gamma_{100}h_{\ell tp} + U_{1tp}h_{\ell tp}$  (see Eq. 4), this then adding an additional random term to Eq. (7) viz.,

$$\Theta_{\ell tp} = \gamma_{000} + \gamma_{100}h_{\ell tp} + \gamma_{010}h_c + V_{00p} + U_{0tp} + U_{1tp}h_{\ell tp} + R_{\ell tp}. \quad (15)$$

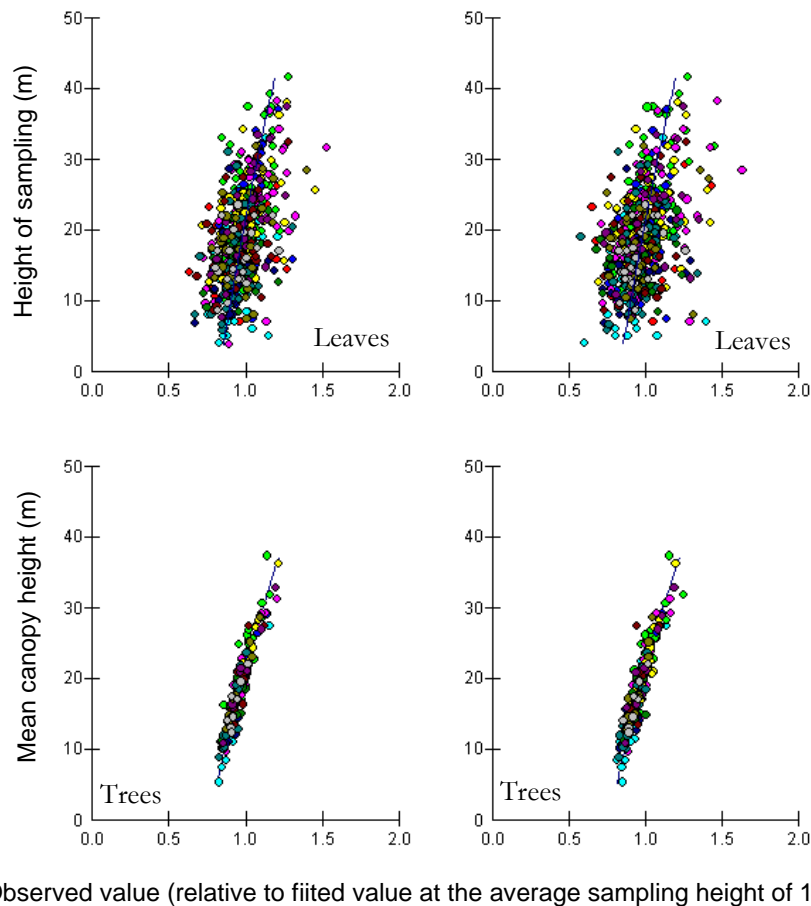
The additional term allows different trees to have different within-canopy gradients – a so called “random slope model” (Snijders and Bosker, 1999) with a  $\chi^2$  test then employable to see if the model fit has been improved. And indeed, when this was attempted, it was found that significant tree-to-tree variations in within canopy gradients were observed ( $P \leq 0.05$ ), but only for  $M_A$ ,  $|\delta^{13}C|$  and  $P_A$ . Moreover, as is shown in Fig. 9 these variations in slopes (or “extinction

coefficients”) were not random, but inter-related and correlated with the mean  $M_A$ ,  $|\delta^{13}C|$  and  $[P]_A$  of the trees concerned. In particular, tree-to-tree variation in all three of the above parameters were well correlated with mean canopy  $[P]_A$ , this being the average of all three measurements taken on each tree, and denoted here as  $\langle [P]_A \rangle$ . The very similar patterns for the gradients in  $M_A$  and  $[P]_A$  with  $\langle [P]_A \rangle$  suggests that most of the between-tree variability in within canopy gradients in  $[P]_A$  was due to variations in  $M_A$  rather than  $[P]_{DW}$ . The strong decline in  $|\delta^{13}C|$  with increasing  $\langle [P]_A \rangle$  is also of note, suggesting that variations in photosynthetic  $^{13}C$  discrimination within tropical tree canopies are intricately linked with plant metabolic processes.

## 6 Discussion

### 6.1 Gradients in nitrogen, phosphorus and photosynthetic capacity

That plants can acclimate to different irradiances at chloroplast, leaf and canopy level has long been appreciated (Monsi and Saeki, 1953; Boardman, 1977; Björkman, 1981) and a key focus of recent years has been understanding the way plants that allocate their resources throughout their canopies, with one main emphasis being the extent to which observed distributions serve to maximise photosynthetic carbon gain (Niinemets, 2007). It was Field (1983) who first proposed



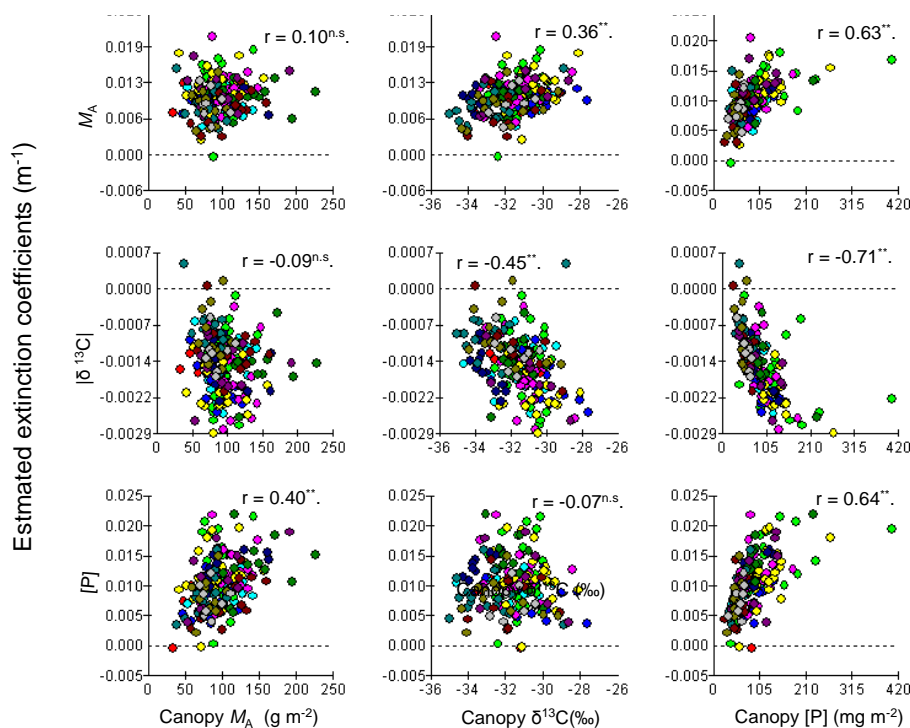
**Fig. 8.** Vertical gradients in leaf [N], and leaf [P] expressed on a leaf area basis. Different colours refer to different regions.

that plant photosynthetic carbon gain would be optimized if key physiological resources required for photosynthesis (in his case nitrogen) were allocated in direct proportion to the average  $Q$  received. Especially when considered in conjunction with the mathematical simplicities that ensue (Farquhar, 1989) this idea of “optimization” is conceptually attractive, even being incorporated into some canopy gas exchange models (Lloyd et al., 1995; Sands, 1995; Sellers et al., 1996). But it is also now clear that although the decline in photosynthetically important elements such as nitrogen and phosphorus within plant canopies can be considerable, and sometimes even impressive, this decline is never to the same extent that it matches the reduction in  $Q$  (De Jong and Doyle, 1985; Carswell et al., 1980; Meir et al., 2002; Anten, 2005; Wright et al., 2006; see also supplementary information: <http://www.biogeosciences.net/7/1833/2010/bg-7-1833-2010-supplement.pdf>).

As to why this should be so has proved somewhat of an enigma, it being generally accepted that natural selection should have resulted in plants optimising their resource strategies. Various hypotheses have been proposed to account for this apparent “non-optimality”. These include

that plants do not grow as isolated individuals but rather in competition with others (Anten, 2005), that it might be related to direct versus diffuse radiative transfer (Buckley et al., 2002; Alton and North, 2007) or not all nitrogen being related to photosynthesis (Hikosaka, 2005); that there may be optimisation of N to light gradients within leaves as well as canopies (Terashima et al., 2005); that the required very high nitrogen concentrations at the top of the canopy may place leaves at strong risk of herbivory (Stockhoff, 1994); that there may be considerable costs of retranslocating nutrients within the plant (Field, 1983; Wright et al., 2006), that plants may over invest in Rubisco in order to cope with temporal variabilities in their environment (Warren et al., 2000) and, especially as gradients in nutrients and photosynthetic capacity are generally driven by gradients in  $M_A$  rather than by variations in dry-weight nutrient concentrations (Reich et al., 1998; Ellsworth and Reich, 1993; Evans and Poorter, 2001), that there may be a practical lower limit to the minimum  $M_A$  and hence  $N_A$  that any species can achieve (Meir et al., 2002).

Although with some affinity with the latter suggestion, and the observation of both Pons et al. (1989) and



**Fig. 9.** Relationship between within canopy gradients in leaf mass per unit area ( $M_A$ ), foliar  $\delta^{13}\text{C}$  and leaf phosphorus concentrations (area basis) and the overall mean  $M_A$ ,  $\delta^{13}\text{C}$  and  $[P]_A$  in the same tree. Also shown are Spearman's rank correlation coefficients and their level of significance (\*;  $P < 0.05$ ; \*\*,  $P < 0.01$ ). Different colours refer to different regions.

Hollinger (1996) that there may be practical limits to  $A_{\text{max}}$  for any given species, the answer we present to this long standing apparent discrepancy differs somewhat to other suggestions made to date. That is to say, we believe the optimality question has actually been incorrectly posed. And we suggest from our simulations and results presented in Sect. 2 that once correctly posed, it turns out gradients of photosynthetic resources within plant canopies are, in fact, close to optimal.

For example, in some cases it has simply been assumed that the problem is simply one of allocating resources for a canopy of a given leaf area index and photosynthetic capacity (as observed). But when this is done (e.g. dePury and Farquhar, 1997) what emerges are unrealistically high nutrient concentrations being required at the top of the canopy, inconsistent with the physiological tradeoffs that clearly exist in terms of leaf structure and function (Wright et al., 2004). This is similar to the point of Meir et al. (2002) already mentioned above, that there is probably also a realistic lower limit to the  $M_A$  and nutrient content that any species can attain.

It is now well established that different species have characteristically different values of fundamentally linked physiological properties such as  $M_A$ ,  $[N]_{\text{DW}}$  and  $[P]_{\text{DW}}$ . For example Fyllas et al. (2009) showed that much of the considerable variability in these properties occurring

within individual sample plots (Fig. 5) is a consequence of species-to-species variations, this being closely linked to other aspects of their physiological strategy including leaf lifespans (Wright et al., 2004) and hydraulic characteristics (Santiago et al., 2004; Meinzer et al., 2008). Such species dependent differences in key foliar physiological properties are also linked to practical morphological and anatomical constraints such as variations in leaf and palisade layer thickness and exposure of mesophyll surface area to the intercellular airspaces (Kenzo et al., 2006). That is not to say, of course, that both within-species variability and the modulation of key physiological traits by the environment does not occur. Both clearly do (Specht and Turner, 2006; Fyllas et al., 2009). Nevertheless, that an individual species can only vary in such functional traits to a limited extent and with this being much less than the observed global range (and thus with finite species overlap occurring) is fundamental to current theories of functional plant ecology (e.g. Reich et al., 2003; McGill et al., 2006). It therefore seems reasonable to argue that the question of optimisation within plant canopies should also be viewed within the constraints of these known physiological boundary conditions such as the maximum (species dependent) photosynthetic potential of the leaves at the top of the canopy. In some cases, the practical minimum value achievable at the bottom of the canopy may also be important, this

perhaps being structural (as suggested by Meir et al., 2002), or alternatively being a consequence of the need for all leaves to maintain a positive carbon balance once mature (Turgeon, 2006), as discussed in Appendix B.

One simple way to view the argument and its consequences is through following the individual lines shown in Fig. 4. If  $A_0^*$  is kept constant, then a plant with an “optimal” distribution of its photosynthetic resources (high  $k_P$ ) unavoidably has less total photosynthetic resource available to it than one that does not (low  $k_P$ ). Thus, it is actually to a plant’s advantage to have a shallow gradient in photosynthetic resources as this allows it to have a greater overall photosynthetic capacity ( $C_C$ ) and hence a higher net rate of carbon gain,  $N_R$ . As discussed in Appendix B, it turns out there are several complexities which end up influencing the minimum  $k_P$  and maximum  $N_R$  which should occur, but nevertheless, the theory and model as presented here do lead to the (intuitive) prediction that plants with a low overall photosynthetic capacity should have shallower gradients in their photosynthetic resources than those with higher photosynthetic capacities. This can be inferred, for example, if we accept that phosphorus has a role in the photosynthetic process for tropical trees (Raaimakers et al., 1995; Lloyd et al., 2001; Domingues et al., 2010), from the relationship between  $\langle [P]_A \rangle$  and the gradients shown in Fig. 9.

As is evidenced from Fig. 8 these tree-to-tree variations in the gradients of  $M_A$  and  $[P]_A$  are also accompanied by correlated variations in  $\delta^{13}C$ . This suggests that for such trees compensating gradients in stomatal conductances do not necessarily occur (Rajendrudu and Naidu, 1997; Miyazawa et al., 2004) with leaves further down within the canopy having relatively higher ratios of intercellular to ambient  $CO_2$  concentrations ( $c_i/c_a$ ). Thus any gradient in overall photosynthetic rates may actually be less than that which would be inferred on the basis of nutrients (or photosynthetic capacity) alone. One reason for higher  $c_i/c_a$  for leaves lower down in tropical forest canopies may be the significantly lower leaf-to-air vapour pressure deficits which typically occur there (Shuttleworth, 1989). However, this does not readily explain why tree-to-tree variations in the magnitude of the gradient in  $\delta^{13}C$  are so closely linked to variations in the gradients in  $M_A$  and  $[P]_A$  (Fig. 9). This has been observed before for conifer trees by Duursma and Marshall (2006) and may be attributable to taller trees with higher than average high  $M_A$  and  $[P]_A$  tending to occur in more exposed conditions and thus experiencing a greater likelihood of their upper canopy leaves being exposed to more severe water deficits during times of high insolation than those lower down (Niinemets et al., 2004). Consistent with this explanation is the less negative overall  $\delta^{13}C$  for those trees with the sharpest gradients (Fig. 9).

The relationship of Fig. 9 is, interestingly, also consistent with greater differences between sun and shade leaves in  $M_A$  and many other leaf characteristics (including  $P_A$ ) for gap-dependent species (as opposed to obligate-gap species or

gap-independent species) as observed by Popma et al. (1992) for a tropical forest in Mexico. They found that gap-dependent species also had higher  $\langle [N]_A \rangle$  and  $\langle [P]_A \rangle$  than the other two species groups.

As well as increasing with height within trees,  $M_A$  also tended to be greater for taller trees within the same stand with  $[N]_{DW}$  and  $[P]_{DW}$  also showing similar patterns within and between different trees, *viz.* no significant gradient at all (Table 1, Fig. 7). Consequently, as was the case for within-tree variation, taller trees also tended to have higher  $[N]_A$  and  $[P]_A$  (Fig. 8). This has been reported before for  $[N]_A$  and  $M_A$  in dipterocarp forests in Malaysia (Thomas and Bazzaz, 1999; Kenzo et al., 2006) with a tendency for taller trees to have a greater  $M_A$  being an apparently general phenomenon (Poorter et al., 2009). This phenomenon will be dealt with in more detail in an accompanying paper utilising a much larger additional data set of individual trees for which only upper-canopy leaves had been sampled. But suffice to say, it emerges that simple scaling relationships such as between  $M_A$  and  $[N]_{DW}$  or  $[P]_{DW}$  (Fyllas et al., 2009) are markedly improved when tree height is also considered as a covariable (S. Patiño et al., unpublished results).

## 6.2 Extrapolation to the stand level

As shown in Fig. 5, even when considering a study such as this encompassing sites across a wide range of soil substrates and climates within the Amazon Basin, the variability in nutrient concentrations,  $M_A$ , and  $\delta^{13}C$  observed was mostly attributable to differences between trees within individual stands (plots). This is as opposed to being associated with the height of sampling within individual trees or even due to the trees being situated in different plots (see also the random error variances as listed in Table 1). This high within-plot heterogeneity has been noted before for tropical forest  $[N]_{DW}$  and  $[P]_{DW}$  (Townsend et al., 2008) and is attributable to the typically high species diversity of most of the plots sampled combined with the presence of substantial within- and between-species variations in nutrient concentrations (Fyllas et al., 2009). Combined with the typical complexities of tropical forest phyto-structure (e.g. Kellner et al., 2009) this then makes it virtually impossible to take relationships such as shown in Fig. 9 and somehow scale them up to estimate some sort of averaged stand level gradient. This is because one would not only need to know the relative abundances of the different trees with different characteristic nutrient concentrations, but also their individual height, canopy dimensions and the leaf area density distributions within their canopies.

But being able to predict such gradients is of critical importance, not only in the modelling of tropical forest carbon acquisition (Mercado et al., 2009), but also for simulations of terrestrial carbon exchange in general (Mercado et al., 2007).

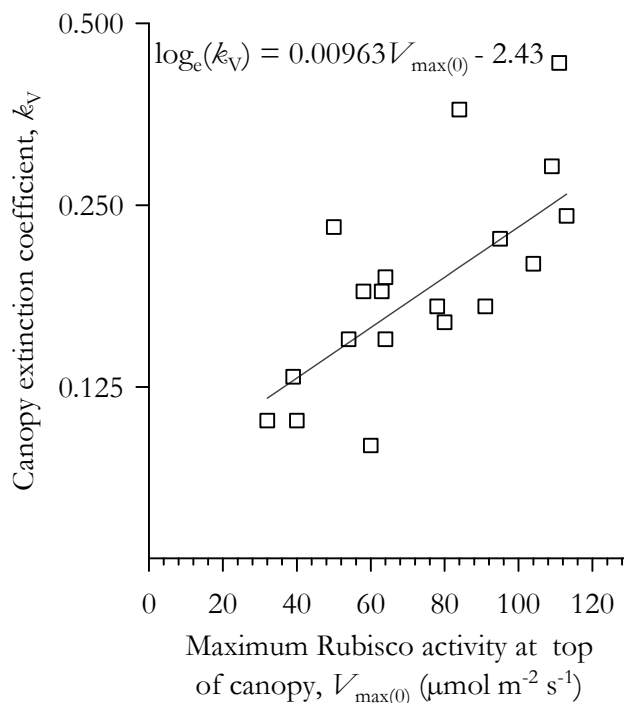
In most studies attempting to simulate  $G_P$ , gradients in photosynthetic capacity are typically expressed in terms of



the cumulative  $L$  down from the top of the canopy (Hirose and Wegner, 1987; de Pury and Farquhar, 1995; Mercado et al., 2009) as is also the case for our simulations here in Sect. 2. In search of a general equation and also to further confirm one fundamental thesis here – that the magnitude of vertical gradients in photosynthetic capacity (expressed as an extinction coefficient) should scale with photosynthetic capacity (Sect. 2.3) – we have thus surveyed the literature, and attempted to estimate a form of  $k_P$  as in Eq. (A2) for as many broadleaf forests and/or trees as possible. As most terrestrial carbon exchange models utilise the activity of ribulose-1,5-bisphosphate carboxylase/oxygenase (Rubisco) for the uppermost leaves  $V_{\max(0)}$ , as a critical input variable (e.g. Sellers et al., 1996) we have therefore attempted to also estimate this value from the same studies as is described in the Supplementary Information: <http://www.biogeosciences.net/7/1833/2010/bg-7-1833-2010-supplement.pdf>. In all, 18 profiles were identified and, when taken together, show a relationship between the within canopy extinction coefficient for Rubisco ( $k_V$ , per unit  $L$ ) and  $V_{\max(0)}$  that is surprisingly good (Fig. 10) with a very strong positive relationship between  $V_{\max(0)}$  and  $k_V$  observed. This was despite the many assumptions required (see Supplementary Information: <http://www.biogeosciences.net/7/1833/2010/bg-7-1833-2010-supplement.pdf>) with associated uncertainties in the true values, and for which it should also be noted we have used a robust rank-based regression procedure (Terpstra and McKean, 2005) to avoid any overinfluence of outliers on the fitted line.

Especially as the range of  $k_V$  is virtually identical to that simulated for  $k_P$  in Fig. 4 this gives us increased confidence in the validity of the approach taken in Sect. 2 and, perhaps along with data from other vegetation types such as conifers and monocots, also suggests a way forward in terms of modelling photosynthesis at larger scales. According to the modelling study (Sect. 2) generally shallow gradients in photosynthetic capacity but with  $k_V$  increasing with upper leaf  $V_{\max}$  can be interpreted as reflecting a likely optimisation of canopy carbon gain potential across a wide range of species with different photosynthetic capacities and geographic locations.

We also believe that previous schemes based on “big-leaf assumptions” also equating to optimality such as for Sellers et al. (1996), Haxeltine and Prentice (1996) and, of course, as also advocated by Lloyd et al. (1995), should probably now be abandoned. Indeed, it is interesting to note that, although a separate consideration of direct versus diffuse radiation may lead to improved model fits for canopy gas exchange models (e.g. Mercado et al., 2006), much of the effect attributed to the improved description of canopy light regime in the sun/shade model of de Pury and Farquhar (1997) was actually a consequence of their sun/shade model and multi-layer model calculation using a  $k_V$  of ca. 0.3 rather than a value of more like 0.7 which is what a big-leaf model actually assumes (J. Lloyd, unpublished results). It may also be



**Fig. 10.** Relationship between within canopy gradients in activity of ribulose-1,5, bisphosphate carboxylase/oxygenase, Rubisco, and maximum Rubisco activity in upper-canopy leaves for a range of broadleaf forests and/or trees taken from a literature review. Details of the individual studies and means of calculation are given in the Supplementary information. Note the logarithmic scale for  $k_V$ . Due to uncertainties in the estimates of both the independent and dependent variables from this literature survey (see Supplementary information), the fitted line has been obtained using a high breakpoint rank regression technique (Chang et al., 1999) and is significant at  $P < 0.01$ .

useful to note that that study and several others (e.g. Hirose and Werger, 1987) have used a slightly different parameterisation of Eq. (A1) where the exponent is normalised by  $L$ . The two different mathematical forms give rise to very different results when  $L$  is allowed to vary. The latter form effectively changes the gradients in photosynthetic capacity throughout the entire plant canopy with any variation in  $L$ .

### 6.3 Model and data uncertainties

Although the model described in Appendix A and utilised analytically in Sect. 2 does seem to be able to simulate  $L$ ,  $G_P$  and  $k_P$  for Amazon forests, as well as making the general prediction that within-canopy gradients should increase as does upper canopy photosynthetic capacity (Figs. 9 and 10), it should be emphasised that the model presented is more conceptual than quantitative. For example, it does not take into account effects of direct versus diffuse radiation (Buckley et al., 2002) and considers the forest canopy to consist only of one generic phenotype. This overlooks

the clear intra- and inter-species variations in photosynthetic characteristics and associated leaf traits that clearly occur, especially for tropical forest canopies (Domingues et al., 2005; Fyllas et al., 2009), along with substantial within and between-tree variations in leaf angle and size (Kitajima et al., 2005; Posada et al., 2009) which should also give rise to attendant variations in  $k_I$ .

The model simulations also involve some simplistic assumptions regarding leaf lifetimes and associated annual construction costs of the photosynthetic machinery (Sect. 2.2). It ignores, for example, that shaded leaves lower down in the canopy may have much longer lifetimes than their sun-exposed counterparts (Lowman, 1992; Tong and Ng, 2008). We have also assumed an average leaf lifetime of one year, independent of  $M_A$  or  $A_{\max}$ . Nevertheless, as mentioned already (Sect. 2.2), leaf lifetimes tend to correlate very poorly with  $A_{\max}$  when the latter is expressed on a leaf area basis. And indeed, for Amazon forest trees, soil fertility seems to be able to strongly influence  $[P]_{DW}$  without affecting  $M_A$  to any large degree (Fyllas et al., 2009). This suggests that the structural component of leaf longevity may be unlinked to concurrent changes in photosynthetic capacity when soil fertility is the primary source of variation – at least for tropical forest trees

Similarly, the carbon costs of nutrient acquisition which may be considerable (Lynch and Ho, 2005) have not been included in the calculations of Sect. 2.3. Effectively, if they were to be included (associated with variations in  $C_C$ ), the optima in Fig. 4 would be shifted slightly to the left, with a less dramatic increase in  $N_R$  as  $C_C$  increases at low values, but with a more rapid decline at supra-optimal  $C_C$ .

Although not critical for the overall conclusions of the model, there are several assumptions regarding leaf respiratory costs which also involve uncertainties. For example, we have simply assumed that for all leaves  $R_{(z)}=0.08A_{\max(z)}$ , even though this fraction has been reported to decline to some extent with depth within the canopy for tropical trees (Cavaleri et al., 2008). A slightly lower than modelled  $R_{(z)}$  lower down within the canopy would effectively serve to make both the modelled optimal  $N_R$  and  $k_P$  to occur at slightly higher  $L$  in simulations such as shown in Fig. 3. Also important in this respect is that the model in Sect. 2 allows for significantly reduced leaf respiration rates in light at all but the lowest  $Q$  (Fig. A1a). The precise mechanism(s) and magnitude of this effect remain highly uncertain at the current time (Hurry et al., 2005). For the model described in Sect. 2, less inhibition at high  $Q$  than modelled would serve to reduce overall  $N_R$  and also make  $R_C$  less sensitive to changes in  $L$  as long as  $C_C$  remains constant, and thus with a slightly higher optimal  $L$  and  $k_P$  being simulated for any given  $C_C$ , but also with a lower  $N_R$ .

One further consideration is that variations in the construction and maintenance costs of foliar supporting tissues (twigs, branches and boles) have not been accounted for when allowing  $L$  to vary. Poorter et al. (2006) found crown

area increasing more strongly with tree height than crown length. They interpreted this as suggesting that crown area expansion is the more efficient way to increase the number of apical meristems and leaf area, so as to occupy space, over-shade neighbors, and reduce self-shading. Nevertheless, the nature of this relationship varies with tree developmental stage (Poorter et al., 2003, 2006) and, indeed, it does not necessarily follow that higher  $L$  trees need to be taller. This is because leaf area density within tropical tree crowns can also vary widely (Ashton, 1978) and thus a deep crown does not necessarily imply a high number of leaf layers. Moreover, taller trees also tend to have a lower bole wood density, as well as low density and weak branches, short branches, high resource costs per unit branch length, and low resource costs per unit stem length (Stark et al., 2006). Taken together, the above considerations suggest that the carbon construction costs of supporting tissue may not vary to any great degree (or systematically) with  $L$  and that their omission from the calculations of Sect. 2 is unlikely to have caused any significant error in the simulations or affected the basic conclusions reached.

The calculations undertaken for Fig. 10 (Sect. 6.2) as detailed in the Supplementary information: <http://www.biogeosciences.net/7/1833/2010/bg-7-1833-2010-supplement.pdf> have in many cases also required assumptions in the derivations of  $V_{\max(0)}$  and/or  $k_V$ . For example in the study of Ellsworth and Reich (1993) we have had to make assumptions about  $c_i$ , in order to estimate  $V_{\max(0)}$ , also assuming it did not vary with canopy height. Also, as many studies have reported  $Q_z/Q_0$  (see Eq. A2) rather than cumulative leaf area index, it was often necessary to make assumptions about  $k_I$ , for example as in Meir et al. (2002) – this being taken as uniform throughout the canopy, although it may also be the case that leaf angles, and hence  $k_I$ , may vary with canopy depth (Posada et al., 2009). The required assumptions for each study are listed in the right hand column of Table S1 (Supplementary Information: <http://www.biogeosciences.net/7/1833/2010/bg-7-1833-2010-supplement.pdf>), and it is because of the considerable uncertainties involved with the estimates of both  $V_{\max(0)}$  and/or  $k_V$  that we have used a robust high breakpoint rank regression technique (Chang et al., 1999) to estimate the slope and its significance for the relationship shown in Fig. 10.

#### 6.4 Gradients in carbon and cation concentrations

Gradients with height were observed in plant carbon concentrations, both within and between trees. Small within canopy gradients in  $[C]_{DW}$  have been reported before by Poorter et al. (2006) who accounted for lower construction costs of low irradiance leaves in terms of lower levels of soluble phenolics. Studying upper-canopy leaves from across the Amazon Basin, Fyllas et al. (2009) also observed significant variations in foliar carbon content, relating this to variations in  $M_A$

and the extent of investment in constitutive defenses. Consistent with this and the observed positive vertical gradient in  $[C]_{DW}$  both between and within trees is the tendency for leaves higher up rain forest canopies to have greater levels of carbon based defense compounds (Lowman and Box, 1983; Downum et al., 2001; Dominy et al., 2003), this perhaps being associated with higher abundances of herbivores such as insects and other arthropods also occurring there (Sutton, 1989; Kato et al., 1995; Koike et al., 1998; Basset et al., 2001).

The decrease in  $[Mg]_{DW}$  with height within individual trees (Table 1, Fig. 7) seems similar to that reported by Grubb and Edwards (1982) comparing saplings and mature trees within a New Guinea montane rain forest. They attributed this to the central role of Mg within the chlorophyll (Chl) complex (Shaul, 2002) with increased  $[Chl]_{DW}$  for shaded leaves being a well documented phenomenon (Boardman, 1977; Björkman, 1981) – as generally seems to be also the case for tropical forest trees (Rozendaal et al., 2006). The within-tree Mg gradient was not, however, significant when expressed on a leaf area basis, despite both  $[N]_A$  and  $[P]_A$  declining with increasing canopy depth. Particularly for N, this is consistent with the idea that in shaded conditions a large portion of N is invested in chlorophyll for light capture, leading to high Chl:N ratios. On the other hand, for light exposed leaves a large proportion of N is invested in Rubisco with commensurate lower Chl:N ratios (Poorter et al., 2000; Evans and Poorter, 2001). By contrast  $[Mg]_A$  did increase with height along with  $[N]_A$  and  $[P]_A$  when between-tree differences in tree height were the source of vertical variation (Table 2). Nevertheless, when comparing different rain forest trees  $[Chl]_A$  seems to be independent of light environment or tree height (Rijkers et al., 2000). Probably then, this increase in  $[Mg]_A$  with tree height relates to its other physiological functions, for example in the process of thylakoid acidification (Pottosin and Schönkmecht, 1996), as an activator of several photosynthetic enzymes including Rubisco (Gardemann et al., 1986; Portis, 1992) and as a ATP-cofactor required for phloem loading of sugars (Shaul, 1992). All these physiological functions would be expected to need to be proceeding at higher rates in taller trees with higher  $[N]_A$  and  $[P]_A$ . This is because such trees would also most likely have higher photosynthetic rates by virtue of greater  $A_0^*$  (associated with higher  $[N]_A$  and  $[P]_A$ : Domingues et al., 2010) as well as a greater probability of high light interception compared to trees occurring lower down the canopy stratum.

Potassium showed a different pattern to magnesium, with a decline in  $[K]_{DW}$  with increasing height, both within- and between-trees (Table 2, Fig. 8). As potassium plays a key role in the maintenance of leaf osmotic potentials as well as being critical for stomatal function (Leigh and Wyn Jones, 1984; Lebaudy et al., 2008) this may appear counter-intuitive as, other things being equal, leaves higher up in the canopy should have both higher gas exchange rates (Carswell et al., 2000; Kenzo et al., 2006; Niinemets, 2007) and more

negative osmotic potentials (Myers et al., 1987; Oberbauer et al., 1997; Niinemets et al., 1999; Niinemets and Valladares, 2004). Nevertheless, soluble carbohydrate concentrations are usually high for sun exposed leaves (Lichtenthaler et al., 1991; Gleason and Ares, 2004) with these sugars making a critical contribution to the required more negative osmotic potentials for the leaves higher up the canopy stratum (Niinemets and Valladares, 2004), perhaps also replacing potassium in this role to some extent (Leigh and Wyn Jones, 1984). It is also the case that leaf densities tend to be higher for high  $M_A$  leaves (e.g. Kenzo et al., 2006), mostly likely due to greater cell wall thicknesses (Syvertsen et al., 1995) and that associated with these high leaf densities are lower water contents (at saturation) per unit dry weight for high  $M_A$  leaves (Prior et al., 2004; Poorter et al. 2009) as well as a greater relative apoplastic water content (Oberbauer et al., 1987). Taken together, these observations mean that mesophyll protoplasmic volumes per unit dry weight should be substantially less for high  $M_A$  upper canopy leaves and thus any potassium present being relatively more effective as an osmoticum per unit foliar dry-weight.

## 7 Conclusions

This paper provides a new explanation as to why gradients in photosynthetic capacity within plant canopies are almost inevitably shallower than that of the light environment. This occurring despite the fact that simple optimization theory suggests that maximum plant carbon gain should be achieved when both gradients are identical. The argument is predicated on the observation, as already noted by others, that there is a practical limit to the maximum photosynthetic capacity a leaf can attain. The analysis here extends this notion through numerical simulation – showing that species with a high intrinsic maximum photosynthetic capacity should have sharper gradients than those with a lower  $CO_2$  assimilation potential. This prediction is verified in two ways. First, it is shown for Amazon trees that variations in the magnitude of intra-canopy variations in phosphorus, a likely good surrogate for photosynthetic capacity, increase with the overall average concentrations of phosphorus (leaf area basis) for individual trees. Secondly, across a wide range of broad leaf trees from various environments, it is also shown that the magnitude of estimated gradients in the activity of Rubisco within plant canopies tends to be greater for those trees with the highest Rubisco activity in their upper canopy leaves. In contrast to previous notions, it is found that in all cases the optimal within-tree gradient in photosynthetic capacity should be less than that of the vertical light profile. The model presented also calculates the leaf area index associated with these optimal gradients in photosynthetic capacity, with predictions surprisingly close to those actually observed.

As has been reported for other forest canopy types, gradients in physiologically relevant nutrients such as N and P

are more or less non-existent for Amazon forests when expressed on a dry weight basis, with lower concentrations on a leaf area basis lower down in the canopy associated with a decline in leaf mass per unit leaf area. As is also the case for  $\delta^{13}\text{C}$ , and foliar carbon content, within-tree and between-tree gradients are, on average, similar.

Gradients in other physiologically relevant nutrients such as Mg and K are also reported. By contrast with the other foliar properties examined, variations in the magnitude of profiles within- and between-trees exist for Mg. Possible explanations for these observed gradients in cations as well as for the observed vertical variations in foliar carbon content and  $\delta^{13}\text{C}$  are discussed.

## Appendix A

### Gradients of photosynthetic capacity in plant canopies

We first start with a general equation describing the light dependence of photosynthesis, this being a rectangular hyperbola, viz:

$$A_z = \frac{A_{\max(z)}\phi Q_z}{A_{\max(z)} + \phi Q_z} - R_z, \quad (\text{A1})$$

where  $A_z$  represents the net  $\text{CO}_2$  assimilation rate of a leaf at some point,  $z$ , within the canopy,  $A_{\max(z)}$  is the maximum net  $\text{CO}_2$  assimilation rate of the leaf in question (at light saturation),  $\phi$  is the quantum yield,  $Q_z$  is the photon irradiance at the leaf surface and  $R_z$  is the rate of respiration by the leaf. Equation (A1) is of a slightly different form to that of a rectangular hyperbola usually presented (Causton and Dale, 1990), allowing a constant  $\phi$  (independent of  $A_{\max(z)}$ ). From both empirical and functional points of view better equations exist, for example the monomolecular (Causton and Dale, 1990) or hyperbolic minimum functions (Farquhar et al., 1980). But unfortunately, both equations lead to intransigent integrals when applied in the approach shown below (see also Buckley and Farquhar, 2004).

We first ignore respiration, allowing both  $A_{\max}$  and  $Q$  to decline exponentially through the canopy according to

$$A_{\max(z)} = A_0^* e^{-k_p z}; \quad Q_z = Q_0 e^{-k_l z}, \quad (\text{A2})$$

where  $Q_0$  is the incident photon irradiance at the top of the canopy,  $A_0^*$  is the maximum (light saturated) photosynthetic rate of the leaves at the top of the canopy in the absence of respiration,  $k_p$  is an ‘‘extinction’’ coefficient describing the decline in photosynthetic capacity,  $k_l$  is an ‘‘extinction’’ coefficient describing the decline in photon irradiance, both extinction coefficients being expressed as a function of the cumulative leaf area index as measured downwards from the top of the canopy. A combination of Eq. (A1) and (A2) when

integrated downwards through a canopy of leaf area index  $L$  is

$$A_C^* = \int_0^L \frac{A_0^* e^{-k_p z} \phi Q_0 e^{-k_l z}}{A_0^* e^{-k_p z} + \phi Q_0 e^{-k_l z}} dz, \quad (\text{A3})$$

where  $A_C^*$  is the photosynthetic rate of the canopy, ignoring any respiration in the light. An analytical solution to Eq. (A3) exists, being

$$A_C^* = \frac{A_0(k_l - k_p)e^{-k_l z} {}_2F_1[a, b, c, \zeta]}{k_p} \Big|_{z=0}^{z=L}. \quad (\text{A4})$$

Here  ${}_2F_1[a, b, c, \zeta]$  is Gauss’s hypergeometric function (Abramowitz and Stegun, 1972) with  $a=k_p/(k_p-k_l)$ ,  $b=1$ ,  $c=(2k_p-k_l)/(k_l-k_p)$  and  $\zeta=-A_0 e^{(k_l-k_p)z}/(\phi Q_0)$ . Gauss’s hypergeometric function can be estimated numerically, for example using the algorithm of Forrey (1997). When  $k_p=k_l$  then Eq. (A4) is undefined, but calculation is still possible as for this special case

$$A_C^* = \frac{-A_0^* \phi Q_0 e^{-k_l z}}{k_l(A_0^* + \phi Q_0)} \Big|_{z=0}^{z=L} = \frac{A_0^* \phi Q_0 (1 - e^{-k_l L})}{k_l(A_0^* + \phi Q_0)}. \quad (\text{A5})$$

Note that Eq. (A5) is very similar in form to Eq. (A1) with the term  $(1 - e^{-k_l L})/k_l$  representing the co-ordinated decline of both light and photosynthetic capacity down the canopy.

A respiration term can be now be added to Eq. (A4) or Eq. (A5). We first take the result of Atkin et al. (2000) who showed for *Eucalyptus pauciflora* that at 30 °C the rate of respiration in the light first rapidly declines with irradiance, then subsequently increases at a much slower rate. From their data, we fitted a curve of the form

$$R_z = R_{d(z)} \left( 1 - \frac{\alpha Q_z}{\beta + Q_z} + \gamma Q_z \right), \quad (\text{A6})$$

where  $R_d$  is the (maximum) rate of foliar respiration in the dark, and with  $\alpha$ ,  $\beta$  and  $\gamma$  being fitted constants with values of 0.9575, 29.85  $\mu\text{mol m}^{-2} \text{s}^{-1}$  and  $5.114 \times 10^{-5} \mu\text{mol quanta}^{-1} \text{CO}_2$ , respectively ( $r^2=0.999$ ). This is shown in Fig. A1a.

Numerous studies have shown that leaf respiration rates in the dark tend to scale with variations in photosynthetic capacity, this also being the case for tropical forests (Domingues et al., 2005). We can therefore express  $R_d$  as a constant fraction,  $f$ , of  $A_{\max}$ , a typical value of which is 0.08, although this fraction may decline to some extent with depth within the canopy (Cavaleri et al., 2008). Light response curves for a range of  $A_{\max(z)}$  and with  $f=0.08$  are shown in Fig. 1b, viz. Eq. A1 combined with Eq. (A6) and with  $R_{d(z)}=0.08 A_{\max(z)}$ .

Light response curves for a range of  $A_{\max(z)}$  combined with Eq. A2 gives

$$R_C = \frac{f A_0 e^{-(k_p-k_l)z} \{ Q_0 \alpha k_p - (k_p+k_l) \beta e^{k_l z} + \gamma_2 Q_0 k_p - 2 F_1[a, b, c, \zeta] \}}{\beta k_p / (k_p - k_l)} \Big|_{z=0}^{z=L} \quad (\text{A7})$$

with  $a=1$ ,  $b=(k_P-k_I)/k_P$ ,  $c=k_P/k_I$  and  $\zeta=-\beta e^{-k_I z}/Q_0$ . As for Eq. (A4), we can also express Eq. (A6) in an alternative and simpler form for the special case of  $k_P=k_I$  viz

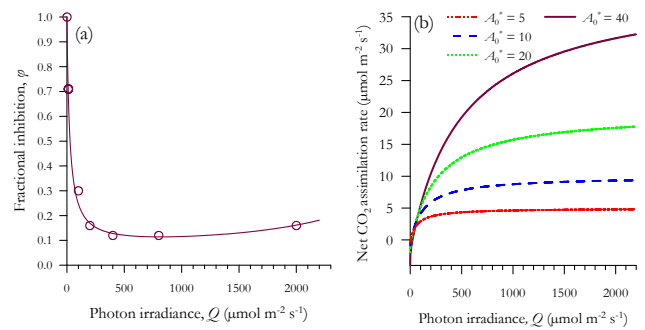
$$R_C = f A_0^* \left( \frac{(\alpha - 1)e^{-k_I z}}{k_I} - \frac{Q_0 \gamma e^{-2 k_I z}}{2 k_I} - \frac{\alpha \beta \log_e[\beta + Q_0 e^{-k_I z}]}{Q_0 k_I} \right) \Big|_{z=0}^{z=L} \quad (\text{A8})$$

In all simulations presented here, Eq. (A7) has been subtracted from Eq. (A4) (or Eq. A8 subtracted from Eq. A5) to give a net CO<sub>2</sub> assimilation rate,  $A_C=A_C^*-R_C$  with the hypergeometric functions solved using the algorithm of Forrey (1997). When applying this algorithm it was found, however, that as  $k_P \rightarrow k_I$  sometimes the numerical solution did not converge, especially at low light where  $\zeta$  could be strongly negative and  $a$  and  $c$  took on large values for the hypergeometric function in Eq. (A4). For such cases, we therefore substituted a representation of a continued equation form of the hypergeometric function which for most of the offending combinations of  $a$ ,  $b$  and  $z$  did allow a stable solution to be obtained. Here we used the general approach of Lenz (1976) as modified by Thompson and Barnett (1986).

## Appendix B

### Evolutionarily stable versus instantaneous model solutions

From Sect. 2.3, estimates of within canopy gradients in photosynthetic capacity and leaf area index are intimately inter-related, and indeed the earliest models of canopy structure and function (Monsi and Saeki, 1953) were based on the idea that the optimal leaf area index of a canopy would be that where the lowest leaves existed at the light compensation point where daily leaf photosynthesis was just cancelled out by respiration (see also Hirose, 2005). Nevertheless, as pointed out by Anten (2002, 2005) such a calculation assumes that the optimum for an individual is not affected by the characteristics of its neighbours, being “simple optimization” in the sense of Parker and Maynard Smith (1990). That is to say, the calculations in Sect. 2.3 overlook the fact that by increasing its  $L$  above the estimated “optimum” value, a plant may also gain in its chances of survival and increase its long term growth rate by shading its neighbour(s) within the same canopy stratum as well as its potential competitors below. Looking at Fig. 4 then, one might conclude that for any given  $A_0^*$ , the “evolutionarily stable” optimal solution with a higher  $L$  might, in fact, be somewhat to the left of the identified optimal value and with a slightly lower  $N_R$  and  $C_C$ . Alternatively, whilst still maintaining the same  $C_C$ , a tree might simply increase  $L$  through an increase in  $k_P$ , as for example in Fig. 3.



**Fig. A1.** Key features of the model. **(a)** Inhibition of leaf respiration in the light (Eq. A6); **(b)** Predicted variations net CO<sub>2</sub> assimilation rates for a range of leaf photosynthetic capacities (expressed as a maximum CO<sub>2</sub> assimilation rate in the absence of dark respiration,  $A_0^*$ , with units of  $\mu\text{mol m}^{-2} \text{s}^{-1}$ ) including an allowance for inhibition of leaf respiration in the light according to Eq. (A1) with  $R_z$  from Eq. (A6) and with  $\phi=0.008 \text{ mol CO}_2 \text{ mol}^{-1} \text{ quanta}$ ).

But what might be the magnitude of this effect? As pointed out by Anten (2002) this evolutionarily optimal  $L$  would be that where the relative losses in  $N_R$  incurred in reducing the photosynthetic gain of one’s competitors was not balanced by the relative gain in increasing their losses. In a mathematical sense then, the optimal “evolutionarily stable”  $L$  would be one where

$$\frac{dN_R}{dL} \geq - \frac{dN_C}{dL}, \quad (\text{B1})$$

with  $N_C$  representing the net carbon gain of the competitors. Computing the right-hand term is difficult for such a heterogeneous system as a tropical forest, but we have made a simple, albeit crude, attempt of the likely effect assuming the  $L$  of any tree affects the photosynthetic gain of only those trees in lower strata within the same canopy without any direct competition between different trees sharing the same canopy layer. We assume that the affected understorey trees have a relatively low photosynthetic capacity of  $A_0^*=5 \mu\text{mol m}^{-2} \text{s}^{-1}$  with  $L=1.0$  and with  $k_P=0.15$ . We emphasise that this is only a very rough estimate, designed merely to give an indication of the likely importance of the effect, also noting that it overlooks the importance of leaf production and vertical positioning as well as the dynamics of leaf production in relation to the optimisation of  $L$  (Hikosaka, 2003; Boonman et al., 2006).

Estimates of the upper tree “evolutionarily stable”  $L$  so calculated from Eq. (4) (denoted  $L^*$ ) are given in Table B1 for selected combinations of  $A_0^*$  and  $C_C$ . Also listed are estimates of  $L$  from the “individual optimization case” (Fig. 4) and a third estimate where the original Monsi and Saeki (1953) criterion is considered; viz. the  $L$  where the leaf at the bottom of the canopy has its photosynthetic carbon gain exactly balanced by its respiratory losses. In our case this “compensation point” represents the average photosynthesis and respiration rates over the 3.5 year period at Tapajós forest (see Sect. 2.2), and is denoted by  $L^*$ .

**Table B1.** Different potential “optimal” values of leaf area index and associated decay coefficients for photosynthetic capacity through the canopy,  $k_P$  (in brackets) for various combinations of total canopy photosynthetic capacity,  $C_C$  expressed in  $\mu\text{mol m}^{-2}$  (ground area)  $\text{s}^{-1}$ , and photosynthetic capacity for leaves at the top of the canopy in the absence of dark respiration,  $A_0^*$ , expressed in  $\mu\text{mol m}^{-2}$  (leaf area)  $\text{s}^{-1}$ . Three values are given (in order); that where the photosynthetic productivity is maximised as in Fig. 4: i.e. with no consideration of “evolutionarily stable” strategies or the need for the light compensation point, for the lowest leaves to be greater than zero;  $L$ : that where the “evolutionarily stable” leaf area index has been estimated as in Eq. (B1);  $L^\circ$ : and that where the long term light compensation point is equal to zero (i.e. photosynthesis is exactly balanced respiration for the lowest leaves of the canopy over a 3.5 year period;  $L^*$ ). NR = “Not Reached” which means this point occurred above the maximum tested leaf area index of 10.0; ND = “Not Determined”, usually because the value of  $k_P$  required to fulfill these simulations was  $<0.0$  (see text). Values in bold suggest the most likely values (see text) and lightly shaded cells correspond to the “optimal” solutions as shown in Fig. 4.

	Model	$C_C=15.75$	$C_C=21.0$	$C_C=31.5$	$C_C=42.0$	$C_C=52.5$	$C_C=63.0$
$A_0^*=6$	$L$	5.1(0.29)	4.3 (0.10)	ND	ND	ND	ND
	$L^\circ$	NR	<b>7.2 (0.23)</b>	ND	ND	ND	ND
	$L^*$	NR	7.4 (0.24)	ND	ND	ND	ND
$A_0^*=12$	$L$	NR	8.9 (0.57)	5.4 (0.31)	4.6 (0.12)	4.2 (0.00)	ND
	$L^\circ$	NR	NR	8.4 (0.36)	6.7 (0.22)	5.9 (0.10)	ND
	$L^*$	NR	NR	<b>7.9 (0.36)</b>	<b>5.5 (0.18)</b>	<b>4.5 (0.01)</b>	ND
$A_0^*=18$	$L$	NR	NR	9.4 (0.57)	6.2 (0.39)	5.1 (0.24)	4.7 (0.14)
	$L^\circ$	NR	NR	NR	9.0 (0.42)	7.4 (0.30)	6.6 (0.22)
	$L^*$	NR	NR	NR	<b>8.0 (0.41)</b>	<b>5.5 (0.26)</b>	<b>4.5 (0.12)</b>

Table B1 shows that the estimated “evolutionarily stable”  $L^\circ$  can be as much as  $3 \text{ m}^2 \text{ m}^{-2}$  greater than that calculated from Fig. 4 which is not that surprising given the only very slight reductions in  $N_R$  that occur when  $L$  increases above its optimum value (Fig. 3). Note, however, that  $L^*$  is often less than  $L^\circ$ , and for the highest  $A_0^*/C_C$  combinations, actually less than  $L$  as inferred from Fig. 4. As noted in the Sect. 6.1 this is of some consequence, because although it is conceptually possible for a leaf at the bottom of a canopy to have a net negative carbon balance and still be a net benefit to the plant (its costs to the plant in terms of being a net sink for carbohydrates being more than offset by its contribution in helping to shade a competitor), it seems this is not a physiologically viable possibility. This is because during leaf maturation, major physiological changes in phloem structure and physiology occur, meaning that it is impossible for adult leaves to act as net sinks of carbohydrates sourced from the rest of the plant (Turgeon, 2006), even if it were somehow in the plant’s interest for them to do so. For trees with high  $A_0^*$ , this effect occurs at much lower  $L$  (due to relatively higher respiratory costs). This means that, despite the model as presented here initially predicting higher  $L$  with higher  $A_0^*$ , the ability for lower  $A_0^*$  trees to sustain leaves at low light levels might allow them to maintain a higher  $L$  than their faster growing counterparts (Sterck et al., 2001; Kitajima et al., 2005).

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