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'Evaluation of circulation and heat transfer in calandria tubes of crystallisation vacuum pans'

Thesis submitted by

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August 2005

for the degree of Masters of Engineering Science in the School of Engineering James Cook University

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#### ABSTRACT

This thesis investigates the importance of circulation and heat transfer in crystallisation vacuum pans that produce raw sugar in the sugar mill. The driving force for circulation and heat transfer occurs in the calandria tubes within vacuum pans.

Numerical and CFD modelling is becoming a cost-effective and reliable way of developing vessel designs especially when there are complex physics and geometries involved, as is the case with vacuum pans. Currently, however, there are no working numerical models of vacuum pans that can be confidently used to design pans with improved circulation and boiling. If the operation of vacuum pans and specifically calandria tubes can be adequately modelled, the design of industrial vacuum pans can be improved to realise the benefits of obtaining more efficient circulation and heat transfer within the pan.

The research aims to provide data on heat transfer and circulation in factory crystallisation vacuum pans and provide data on an experimental rig simulating a single calandria tube for validation of numerical models. Factory trials were conducted to obtain data on heat transfer and circulation in factory pans. A method for measuring circulation speeds in massecuite solutions and vacuum pans was refined as part of this research. The data collected from the factory trials enabled the operating conditions for the single calandria tube boiling rig experimental trials to be determined.

The intention of the experimental rig was to simulate factory conditions to allow detailed examinations of the heat transfer process and vapour volume fraction profiles to be obtained. Natural and forced circulation conditions were investigated as both types of circulation are present in factory vacuum pans. The data gathered from these experiments were preliminary in nature as the rig did not adequately represent factory equipment.

The research highlights problems associated with the boiling of viscous fluids, such as molasses on a laboratory scale. Strategies and recommendations are provided to enable a more adequate representation of factory conditions in the experimental rig. These improvements will allow more accurate data to be obtained that can be used to develop improved models of calandria tubes and vacuum pans.

The experiments conducted on the single calandria tube detailed the physical changes and heat transfer characteristics for boiling in calandria tubes with changing material properties and heat input conditions. The experiments allowed fluid specific correlations to be obtained for heat transfer coefficients and vapour distribution during boiling in the calandria tubes. These correlations were used to develop numerical models of the boiling that occurs in calandria tubes. The numerical models provided a better understanding of the flow characteristics in the vessel and can facilitate the development of improved engineering designs.

The project shows the applicability of a pilot scale rig to provide data that can be used to improve the understanding and modelling of flow and heat transfer in the calandria tubes of crystallisation vacuum pans.

#### STATEMENT OF SOURCES

#### DECLARATION

I declare that this thesis is my own work and has not been submitted in any form for another degree or diploma at any university or other institution of tertiary education. Information derived from the published or unpublished work of others has been acknowledged in the text and a list of references is given.

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### Contents

STATEMEN	NT OF ACCESS	i
ABSTRACT		ii
STATEMEN	NT OF SOURCES	iv
ACKNOWL	EDGEMENTS	vi
LIST OF FI	GURES	X
LIST OF TA	ABLES	xii
LIST OF SY	MBOLS	xiii
1 INTRO	DUCTION	1
1.1 Cry	ystallisation vacuum pans	3
1.2 Cry	ystallisation vacuum pan design	4
1.3 CF	D modelling	6
1.4 Pro	blem statement	7
2 CIRCU	LATION AND HEAT TRANSFER MEASUREMENTS	9
2.1 Cir	culation theory	9
2.2 Cir	culation measurements	11
2.2.1	Measurement method	13
2.2.2	Measurement results	14
2.2.3	Summary	15
2.3 He	at transfer	15
2.4 Flu	id properties	17
2.4.1	Liquid density	18
2.4.2	Specific heat capacity	19
2.4.3	Enthalpy	
2.4.4	Rheological properties	
2.4.5	Thermal conductivity	23
2.4.6	Surface tension	
2.4.7	Vapour properties	
2.4.8	Boiling point elevation	25
2.4.9	Impurities	
2.5 Su	mmary	
<b>3 FACTO</b>	DRY TRIALS	

	3.1	Introduction	
	3.2	Hot film anemometers	
	3.3	Anemometer calibrations	
	3.4	Anemometer error sources	
	3.5	Overview of the factory trials	
	3.6	Sample analysis	
	3.7	Circulation results	
	3.7.	1 Measurement issues	
	3.8	Heat transfer	
	3.9	Heat transfer results	
	3.10	Summary	
4	NU	MERICAL MODELLING	55
	4.1	Introduction	
	4.2	Modelling of circulation in vacuum pans	
	4.3	Boiling in calandria tubes	
	4.4	Modelling calandria tubes	
	4.5	Empirical correlations	
	4.5.	1 Heat transfer	
	4.5.	<i>2 Vapour distribution within the calandria tube</i>	
	4.6	Summary	72
5	EX	PERIMENTAL RIG	74
5	<b>EX</b> 5 1	PERIMENTAL RIG	<b>74</b> 74
5	EX 5.1 5.2	PERIMENTAL RIG Introduction Single calandria tube boiling rig	<b>74</b> 74 74
5	EX 5.1 5.2 5.2	PERIMENTAL RIG Introduction Single calandria tube boiling rig	<b>74</b> 
5	EX 5.1 5.2 5.2. 5.2.	<b>PERIMENTAL RIG</b> Introduction         Single calandria tube boiling rig         1       Configuration 1         2       Configuration 2	74 74 74 75 76
5	EX 5.1 5.2 5.2. 5.2. 5.2.	<b>PERIMENTAL RIG</b> Introduction         Single calandria tube boiling rig         1       Configuration 1         2       Configuration 2         3       Configuration 3	74 74 74 75 76 77
5	EX 5.1 5.2 5.2 5.2 5.2 5.2	<b>PERIMENTAL RIG</b> Introduction         Single calandria tube boiling rig         1       Configuration 1         2       Configuration 2         3       Configuration 3         Instrumentation	74 74 74 75 76 77 80
5	EX 5.1 5.2 5.2 5.2 5.2 5.2 5.2	<b>PERIMENTAL RIG</b> Introduction         Single calandria tube boiling rig         1       Configuration 1         2       Configuration 2         3       Configuration 3         Instrumentation       Instrumentation errors	74 74 74 75 76 77 80 83
5	EX 5.1 5.2 5.2 5.2 5.2 5.2 5.3 5.3 5.3	<b>PERIMENTAL RIG</b> Introduction         Single calandria tube boiling rig         1       Configuration 1         2       Configuration 2         3       Configuration 3         Instrumentation       Instrumentation errors         1       Instrumentation errors	74 74 74 75 76 77 80 83 83
5	EX 5.1 5.2 5.2 5.2 5.2 5.3 5.3 5.3 5.4 5.5	<b>PERIMENTAL RIG</b> Introduction         Single calandria tube boiling rig.         1       Configuration 1         2       Configuration 2         3       Configuration 3         Instrumentation       Instrumentation         1       Instrumentation errors         Control software and instrumentation       Commissioning of rig.	74 74 74 75 76 76 77 80 83 83 84 84
5	EX 5.1 5.2 5.2 5.2 5.2 5.2 5.3 5.3 5.3 5.4 5.5 5.5	<b>PERIMENTAL RIG</b> Introduction         Single calandria tube boiling rig.         1       Configuration 1         2       Configuration 2         3       Configuration 3         Instrumentation       Instrumentation         1       Instrumentation errors         2       Control software and instrumentation         1       Densitometer positioning and calibration	74 74 74 75 75 76 77 80 83 83 84 86 86
5	EX 5.1 5.2 5.2 5.2 5.2 5.2 5.3 5.3 5.3 5.4 5.5 5.5 5.5	<b>PERIMENTAL RIG</b> Introduction         Single calandria tube boiling rig.         1       Configuration 1         2       Configuration 2         3       Configuration 3         Instrumentation       Instrumentation         1       Instrumentation errors         2       Control software and instrumentation         1       Densitometer positioning and calibration         2       Densitometer results	74 74 74 75 76 76 77 80 83 83 84 84 86 
5	EX 5.1 5.2 5.2 5.2 5.2 5.2 5.2 5.2 5.2 5.2 5.3 5.3 5.4 5.5 5.5 5.5 5.5	<b>PERIMENTAL RIG</b> Introduction         Single calandria tube boiling rig.         1       Configuration 1         2       Configuration 2         3       Configuration 3         Instrumentation       Instrumentation         1       Instrumentation errors         2       Control software and instrumentation         1       Densitometer positioning and calibration         2       Densitometer results         3       Pressure control	74 74 74 75 76 76 77 80 83 83 84 84 86 86 90 91
5	EX 5.1 5.2 5.2 5.2 5.2 5.2 5.2 5.3 5.3 5.3 5.4 5.5 5.5 5.5 5.5 5.5	<b>PERIMENTAL RIG</b> Introduction         Single calandria tube boiling rig.         1       Configuration 1         2       Configuration 2         3       Configuration 3         Instrumentation       Instrumentation         1       Instrumentation errors         Control software and instrumentation       Commissioning of rig.         1       Densitometer positioning and calibration         2       Densitometer results         3       Pressure control	74 74 74 75 76 76 77 80 83 83 84 84 86 
5	EX 5.1 5.2 5.2 5.2 5.2 5.2 5.2 5.2 5.3 5.3 5.3 5.4 5.5 5.5 5.5 5.5 5.5 5.5	<b>PERIMENTAL RIG</b> Introduction         Single calandria tube boiling rig.         1       Configuration 1         2       Configuration 2         3       Configuration 3         Instrumentation       Instrumentation         1       Instrumentation errors         2       Control software and instrumentation         1       Densitometer positioning and calibration         2       Densitometer results         3       Pressure control         4       Flow circulation control         5       Temperature effects	74 74 74 75 76 77 80 83 83 84 84 86 86 90 91 93 95
5	EX 5.1 5.2 5.2 5.2 5.2 5.2 5.2 5.3 5.3 5.3 5.4 5.5 5.5 5.5 5.5 5.5 5.5 5.5	<b>PERIMENTAL RIG</b> Introduction         Single calandria tube boiling rig.         1       Configuration 1         2       Configuration 2         3       Configuration 3         Instrumentation       Instrumentation         1       Instrumentation errors         2       Control software and instrumentation         Commissioning of rig.       Instrumenter positioning and calibration         2       Densitometer positioning and calibration         3       Pressure control         4       Flow circulation control         5       Temperature effects         6       Heat flux control	74 74 74 75 76 76 77 80 83 83 84 84 86 90 91 91 93 95 97
5	EX 5.1 5.2 5.2 5.2 5.2 5.3 5.3 5.3 5.4 5.5 5.5 5.5 5.5 5.5 5.5 5.5	<b>PERIMENTAL RIG</b> Introduction         Single calandria tube boiling rig.         1       Configuration 1         2       Configuration 2         3       Configuration 3         Instrumentation       Instrumentation         1       Instrumentation errors         2       Control software and instrumentation         1       Densitometer positioning and calibration         2       Densitometer results         3       Pressure control         4       Flow circulation control         5       Temperature effects         6       Heat flux control         Experimental work program	74 74 74 75 76 76 77 80 83 83 84 84 86 90 91 91 93 95 97 
5	EX 5.1 5.2 5.2 5.2 5.2 5.2 5.3 5.3 5.3 5.4 5.5 5.5 5.5 5.5 5.5 5.5 5.5	<b>PERIMENTAL RIG</b> Introduction         Single calandria tube boiling rig.         1       Configuration 1         2       Configuration 2         3       Configuration 3         Instrumentation       Instrumentation errors         1       Instrumentation errors         2       Control software and instrumentation         1       Densitometer positioning and calibration         2       Densitometer results         3       Pressure control         4       Flow circulation control         5       Temperature effects         6       Heat flux control         Experimental work program	74 74 74 75 76 76 77 80 83 83 84 84 86 90 91 91 93 95 97 100 100
5 6	EX 5.1 5.2 5.2 5.2 5.2 5.3 5.3 5.4 5.5 5.5 5.5 5.5 5.5 5.5 5.5	<b>PERIMENTAL RIG</b> Introduction         Single calandria tube boiling rig.         1       Configuration 1         2       Configuration 2         3       Configuration 3         Instrumentation       Instrumentation         1       Instrumentation errors         Control software and instrumentation       Commissioning of rig.         1       Densitometer positioning and calibration         2       Densitometer results         3       Pressure control         4       Flow circulation control         5       Temperature effects         6       Heat flux control         Fersimental work program	74 74 74 75 76 76 77 80 83 83 84 86 86 90 91 91 93 95 97 100 100 103

	6.2	Experimental trials	
	6.2.	1 Natural circulation	103
	6.2.	2 Forced circulation	104
	6.3	Sample analysis	
	6.4	Summary of results	
	6.5	Empirical correlations	110
	6.5.	1 Heat transfer	110
	6.5.	2 Vapour distribution	115
	6.6	Summary	117
7	MO	DELLING RESULTS	119
	7.1	Background	
	7.2	Validation against experimental data	
	7.2.	<i>1</i> Slip ratio for the determination of vapour distribution	124
	7.3	Tube performance curves	
	7.4	Summary	
8	CO	NCLUSIONS AND RECOMMENDATIONS	135
	8.1	Conclusions	
	8.2	Recommendations	
	8.2.	<i>1</i> Modification of experimental rig	
	8.2.	2 Other experimentation	
	8.2.	3 Numerical modelling	141
B	IBLIO	GRAPHY	143
A	PPENI	DIX A – Glossary of terms	
A	PPENI	DIX B – Calibration constants for the anemometer probes	
A	PPENI	DIX C – MTL8000 I/O wiring information	157
A	PPENI	DIX D – ProcessACT schematics	
A	PPENI	DIX E – Citect schematics	166
A	PPENI	DIX F – SEW Motor and Inverter wiring information	174
A	PPENI	DIX G – Summary of JCU experimental data	177
A	PPENI	DIX H – One dimensional Visual Basic tube model	

## LIST OF FIGURES

Figure 1-1	Sectioned view of a batch fixed calandria pan, from Stephens (2001).	3
Figure 1-2	Circulation pattern in a fixed calandria batch pan.	5
Figure 2-1	Circulation patterns in a vacuum pan due to eruptive boiling, from	
	Wright (1966)	.10
Figure 3-1	Diagram of Turck insertion flow sensor	.29
Figure 3-2	Schematic of calibration rig.	.32
Figure 3-3	Orientations of the anemometer tip to the cross-flow profile,	
-	adaptation from Incropera and DeWitt (1996).	.33
Figure 3-4	Socket locations for the anemometer probes and general pan	
e	dimensions (in mm) of Macknade No. 6 pan	.35
Figure 3-5	Anemometer probe housing and gland arrangement for insertion	
0	into vacuum pans	.36
Figure 3-6	Average velocity trends at socket location 'A' for various insertion	
e	depths on No. 6 pan at Macknade Mill during the A massecuite	
	strike.	.40
Figure 3-7	Average velocity trends at socket location 'B' for various insertion	
U	depths on No. 6 pan at Macknade Mill during the A massecuite	
	strike.	.41
Figure 3-8	Average velocity trends at socket location 'C' for various insertion	
C	depths on No. 6 pan at Macknade Mill during the A massecuite	
	strike.	.41
Figure 3-9	Average velocity trends at socket location 'D' for various insertion	
	depths on No. 6 pan at Macknade Mill during the A massecuite	
	strike	.42
Figure 3-10	Average velocity trends at socket location 'E' for various insertion	
-	depths on No. 6 pan at Macknade Mill during the A massecuite	
	strike	.42
Figure 3-11	Comparison of the circulation results between the 2001 and 2002	
	factory trials measured at location 'B' at an insertion depth of 300-	
	330 mm for the seed preparation step on Macknade No. 6 pan	.44
Figure 3-12	Comparison of the circulation results between the 2001 and 2002	
	factory trials measured at location 'B' at an insertion depth of 300-	
	330 mm for the A massecuite strike on Macknade No. 6 pan	.44
Figure 3-13	Effect of probe insertion depth versus probe orientation to the	
	expected main direction for massecuite flow.	45
Figure 3-14	Velocity trends of different production runs for probe 1 inserted to a	
	depth of 100 mm at location 'C' and probe 2 inserted to a depth of	

	600 mm at location 'A' for the seed preparation step on Macknade	
	No. 6 pan during trials in the 2002 season.	.46
Figure 3-15	Velocity trends of different strikes for probe 1 inserted to a depth of	
	100 mm at location 'C' and probe 2 inserted to a depth of 600 mm at	
	location 'A' for the A massecuite strike on Macknade No. 6 pan	
	during trials in the 2002 season	.47
Figure 3-16	Velocity trends of different production runs for probe 3 inserted to a	
	depth of 1000 mm at locations 'D' and 'E' for the seed preparation	
	step on Macknade No. 6 pan during trials in the 2002 season	.48
Figure 3-17	Velocity trends of different strikes for probe 3 inserted to a depth of	
	1000 mm at locations 'D' and 'E' for the A massecuite strike on	
	Macknade No. 6 pan during trials in the 2002 season.	.49
Figure 3-18	HTC values plotted against operating level for Macknade No. 6 pan	
	during trials in the 2001 season.	.51
Figure 3-19	HTC values and operating level plotted against time for Macknade	
	No. 6 pan during trials in the 2001 season.	.52
Figure 4-1	Diagram of temperatures and void fractions when boiling in a	
	vertical tube, from Rouillard (1985).	.59
Figure 4-2	Illustration of the thermal boundary layer.	.63
Figure 5-1	Schematic of the single calandria tube boiling rig at JCU.	.76
Figure 5-2	Photo of the electrical heating bands	.77
Figure 5-3	Photo of the internal gear pump	.78
Figure 5-4	Schematic of the single calandria boiling tube rig located at JCU	.79
Figure 5-5	Photo of the modified pipe work and insulated header tank	.80
Figure 5-6	Experimental calandria boiling tube instrumentation.	.82
Figure 5-7	Photo of the instrumentation installed on the single calandria boiling	
	tube rig	.82
Figure 5-8	Schematic of SCADA system hierarchy.	.85
Figure 5-9	Citect overview of boiling circuit controller.	.86
Figure 5-10	Densitometer positioning system layout.	.87
Figure 5-11	Data obtained from the densitometer.	.90
Figure 5-12	Operating pressure in the headspace for various experimental trials	.92
Figure 5-13	Operating pressure in the headspace for leak test trials.	.93
Figure 5-14	Operating level in the header tank for various experimental trials	.94
Figure 5-15	Temperature profiles along the tube length during an experimental	
	trial	.96
Figure 5-16	Temperature profiles and heat transfer data for the vapour heat	
	exchanger during an experimental trial.	.99
Figure 6-1	Heat transfer correlation for the natural circulation trials.	113
Figure 6-2	Heat transfer correlation for the forced circulation trials	114
Figure 6-3	Vapour volume fraction correlation for the experimental trials	117

Figure 7-1	Performance curve showing the pressure driving force as a function	
	of mass flow rate through the calandria tube1	28
Figure 7-2	Performance curve showing a zoomed section of figure 7-1	29
Figure 7-3	Performance curve showing the heat flux as a function of mass flow	
	rate through the calandria tube1	30
Figure 7-4	Performance curve showing the pressure driving force as a function	
	of average circulation velocity through the calandria tube1	31
Figure 7-5	Performance curve showing a zoomed section of figure 7-41	31
Figure 8-1	Suggested positioning of instrumentation for the additional factory-	
	based trials in one calandria tube of a vacuum pan1	40

## LIST OF TABLES

Table 2-1	List of velocity measurements in industrial vacuum pans12
Table 3-1	List of analyses conducted on massecuite and molasses samples
Table 3-2	Summary of sample analyses for Macknade No. 6 pan
Table 4-1	Summary of numerical modelling attempts of vacuum pan
	operation
Table 6-1	Summary of average operating conditions for the natural circulation
	trials (configurations 1 and 2)104
Table 6-2	Summary of operating conditions for the forced circulation trials
	(configuration 3)105
Table 6-3	Analyses of the sample mixtures used in the experimental boiling
	trials107
Table 6-4	Summary of the results and average operating conditions for the
	natural circulation trials (configurations 1 and 2)108
Table 6-5	Summary of the results and operating conditions for the forced
	circulation trials (configuration 3)108
Table 7-1	Comparisons between the experimental data and predicted values
	for the single calandria tube boiling trials
Table 7-2	Typical average fluid properties and operating conditions for high-
	grade massecuite strikes

## LIST OF SYMBOLS

$A_{film}$	Heat transfer area of metal film	$m^2$
$A_{HT}$	Heat transfer area	$m^2$
$A_{tube}$	Surface area of the calandria tube	m <sup>2</sup>
$A_{R}$	Entrained air constant for viscosity calculations	-
Bo	Non-dimensional Bond number	-
BPE	Boiling point elevation of the massecuite	°C
$BPE_{S}$	Boiling point elevation of the sugar solution	°C
$Bx_{liq}$	Brix of the sugar solution	%
$Bx_{mass}$	Brix of the massecuite	%
$Bx_{mol}$	Brix of the molasses	%
$C_{Y}, C_{X}, n_{K}$	King's law constants	-
$C_0$	Flow distribution parameter	-
$CC_{mass}$	Crystal content by weight of massecuite	%
$CC_{vol}$	Volume ratio of crystal to molasses in the solution	%
$C_{p,liq}$	Specific heat of the sugar solution	J.kg <sup>-1</sup> .K <sup>-1</sup>
$C_{p,mass}$	Specific heat of the liquid	J.kg <sup>-1</sup> .K <sup>-1</sup>
$C_{p,sug}$	Specific heat of the sugar	J.kg <sup>-1</sup> .K <sup>-1</sup>
$C_N$	Count rate for the process fluid in the heated tube	counts.s <sup>-1</sup>
CV	Coefficient of variation in the crystal size distribution	%
$C_W$	Count rate for a fluid with specific gravity of unity	counts.s <sup>-1</sup>
$d_{bub}$	Diameter of the bubble	m
$dP_{grav}$	Pressure loss due to elevation	N.m <sup>-2</sup>
$dP_{acc}$	Pressure loss due to acceleration	N.m <sup>-2</sup>
$dP_{frict}$	Pressure loss due to friction	N.m <sup>-2</sup>
D	Internal diameter of the heated tube	m
$DS_{\rm liq}$	Dry substance of the solution	%
$DS_{\rm mass}$	Dry substance of the massecuite	%
$DS_{\rm mol}$	Dry substance of the mother molasses	%
Ε		Volt
-	Voltage output of the anemometer	1010
$F_R$	Voltage output of the anemometer Crystal property constant for viscosity calculations	-
$F_R$ $f_f$	Voltage output of the anemometer Crystal property constant for viscosity calculations Fanning friction factor	-
$F_R$ $f_f$ $f_{liq}$	Voltage output of the anemometer Crystal property constant for viscosity calculations Fanning friction factor Fanning friction factor evaluated for the liquid velocity	- - -
$F_R$ $f_f$ $f_{liq}$ $f_{vap}$	Voltage output of the anemometer Crystal property constant for viscosity calculations Fanning friction factor Fanning friction factor evaluated for the liquid velocity Fanning friction factor evaluated for the vapour velocity	- - -

G	Mass flow rate in the tube	kg.s <sup>-1</sup>
$h_{boil}$	Boiling heat transfer coefficient	$W.m^{-2}.K^{-1}$
$h_{cond}$	Condensation heat transfer coefficient	$W.m^{-2}.K^{-1}$
$h_{conv}$	Convection heat transfer coefficient	$W.m^{-2}.K^{-1}$
$h_{FC}$	Forced convection heat transfer coefficient	$W.m^{-2}.K^{-1}$
$h_{\scriptscriptstyle NB}$	Nucleate boiling heat transfer coefficient	$W.m^{-2}.K^{-1}$
$h_{SP}$	Single phase transfer coefficient	$W.m^{-2}.K^{-1}$
$h_{TP}$	Boiling or two-phase heat transfer coefficient	$W.m^{-2}.K^{-1}$
Ι	Current in the heating element	А
Ja	Non-dimensional Jacob number	-
$k_{_{liq}}$	Thermal conductivity of the sugar solution	$W.m^{-1}.K^{-1}$
k <sub>mass</sub>	Thermal conductivity of massecuite	$W.m^{-1}.K^{-1}$
$K_{liq}$	Consistency of the liquid	$N.m^{-2}.s^{n}$
$L_{\rm xal}$	Mean crystal size	mm
$L_D$	Path length of the process fluid	m
L	Length scale for heat transfer	m
$L_T$	Length of the heated tube	m
$M_{AC}$	Mass absorption coefficient	$m^2.kg^{-1}$
$M_{CW}$	Mass flow rate of the cooling water stream	kg.s <sup>-1</sup>
$M_{leak}$	Leakage mass flow rate of air	kg.h <sup>-1</sup>
$M_{steam}$	Mass flow rate of the steam	kg.s <sup>-1</sup>
MW	Molecular weight	kg.kmol <sup>-1</sup>
n <sub>flow</sub>	Viscosity flow behaviour index	-
$N_{bub}$	Experimentally determined constant (Equation 4.22)	-
$Nu_L$	Non-dimensional Nusselt number	-
$Nu_{TP}$	Non-dimensional two-phase Nusselt number	-
p	Static pressure in the heated tube	kPa
$P_{\rm liq}$	True purity of the solution	%
$P_{\rm mass}$	True purity of the massecuite	%
$P_{\rm mol}$	True purity of the mother molasses	%
Pr	Non-dimensional Prandtl number	-
Q	Heat flux	W
$Q_{cond}$	Heat flux in the heat exchanger	W
$Q_{leak}$	Air leakage rate in the rig	m <sup>3</sup> .Pa.s <sup>-1</sup>
$Q_{liq}$	Volumetric flow rate of liquid in the tube	$m^{3}.s^{-1}$
$Q_{tube}$	Heat flow rate to the calandria tube	W
$Q_{vap}$	Volumetric flow rate of vapour in the tube	$m^3.s^{-1}$

r	Internal radius of the heated tube	m
R	Gas constant 8.314 m <sup>3</sup> .Pa.m	nol <sup>-1</sup> .K <sup>-1</sup>
Re <sub>TP</sub>	Non-dimensional two-phase Reynolds number	-
$R_m$	Metal heating element resistance	Ω
$R_{SW}$	Heating resistance from the condensing steam to the tube	$W^{-1}$ .°C
$R_{\scriptscriptstyle WM}$	Heating resistance from the tube wall to the massecuite	$W^{-1}.^{\circ}C$
S	Liquid – vapour slip ratio	-
suc <sub>liq</sub>	Sucrose content of the solution	%
$T_a$	Ambient fluid temperature	°C
T <sub>air</sub>	Temperature of the air leaking into the system	°C
T <sub>CWin</sub>	Inlet cooling water temperature	°C
$T_{CWout}$	Outlet cooling water temperature	°C
$T_{f}$	Film temperature	°C
$T_{liq}$	Temperature of the liquid	°C
$T_{mass}$	Temperature of the massecuite	°C
$T_{mol}$	Temperature of the molasses	°C
$T_{steam}$	Temperature of the condensing steam	°C
$T_{sat}$	Temperature of the saturated vapour produced by boiling	°C
T <sub>sug</sub>	Temperature of sugar	°C
$T_{wall}$	Temperature of the tube wall	°C
$u_{liq}$	Superficial liquid phase velocity	m.s <sup>-1</sup>
$\overline{u}_{liq}$	Average liquid phase velocity	m.s <sup>-1</sup>
u <sub>TP</sub>	Two-phase velocity of the liquid-vapour mixture	$m.s^{-1}$
$u_{vap}$	Superficial vapour phase velocity	$m.s^{-1}$
$\overline{u}_{vap}$	Average vapour phase velocity	$m.s^{-1}$
U	Overall heat transfer coefficient	$W.m^{-2}.K^{-1}$
$V_{fluid}$	Velocity of the fluid perpendicular to the probe	$m.s^{-1}$
$V_{liq}$	Mean velocity of the fluid entering the tube	m.s <sup>-1</sup>
$V_r$	Mean bubble rising velocity	m.s <sup>-1</sup>
x	Mixture quality	-
Z	Length along the heated tube	m

#### **Greek letters**

α	Vapour volume fraction	-
$lpha_{_{dif}}$	Thermal diffusivity	$m^2.s^{-1}$
$\partial_t$	Thermal boundary layer thickness	m
$\Delta T$	Temperature difference between the tube wall and liquid	°C

$\Delta T_{e\!f\!f}$	Effective temperature difference	Κ
γ	Shear rate	$s^{-1}$
γ <sub>corr</sub>	Corrected shear rate	$s^{-1}$
$\lambda_{_{fg}}$	Latent heat of condensation of the steam	J.kg <sup>-1</sup>
$\lambda_{_{fg},liq}$	Latent heat of the sugar solution	J.kg <sup>-1</sup>
$ ho_{_{liq}}$	Density of the liquid	kg.m <sup>-3</sup>
$ ho_{\scriptscriptstyle mass}$	Density of the massecuite	kg.m <sup>-3</sup>
$ ho_{\scriptscriptstyle mol}$	Density of the molasses	kg.m <sup>-3</sup>
$ ho_{{\it mix}}$	Density of the process fluid in the heated tube	kg.m <sup>-3</sup>
$ ho_{\scriptscriptstyle vap}$	Density of saturated water vapour	kg.m <sup>-3</sup>
$ ho_{\scriptscriptstyle xal}$	Density of the crystal	kg.m <sup>-3</sup>
$\mu_{_{liq}}$	Dynamic viscosity of the liquid	Pa.s
$\mu_{mass}$	Dynamic viscosity of the massecuite	Pa.s
$\mu_{\scriptscriptstyle mol}$	Dynamic viscosity of the mother molasses	Pa.s
$\sigma_{_{liq}}$	Surface tension of sugar solution	N.m <sup>-2</sup>
$\sigma_{\scriptscriptstyle mol}$	Surface tension of mother molasses	N.m <sup>-2</sup>
τ	True shear stress	N.m <sup>-2</sup>

#### Subscripts

liq	Liquid component of solution
vap	Vapour component of solution
mass	Massecuite
mol	Molasses
sug	Sugar