# Handwritten Signature Verification Using Complementary Statistical Models

Thesis submitted by Alan McCabe November, 2003

for the Degree of Doctor of Philosophy in the School of Information Technology at James Cook University of North Queensland.

> Supervisor: Doctor Bruce Litow

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Alan McCabe

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#### Abstract

There is considerable interest in computerised personal identification and in particular in *biometrics*, a branch of identification that deals with verifying physical or behavioural characteristics of human beings. This thesis is concerned with the development of the particular biometric of handwritten signature verification, which is superior in many ways to other biometric authentication techniques that may be reliable but are much more intrusive.

Specifically, this project involves the use of two complementary artificially intelligent systems in the form of neural networks and hidden Markov models. Five sample signatures are used to build a reference in each of the independent models and experimentation and testing is done using an extensive database of almost 4,000 genuine signatures and forgeries. The confidence levels from each model are then combined and tested on unseen signatures resulting in an equal error rate of 1.1%. Further experimentation is performed and includes analysis of different verification scenarios, error contribution and the importance of visual feedback when signing. Finally, experiments are conducted exploring the possibility of "signing" handwritten passwords, with the developed system resulting in an equal error rate of 0.7% in the worst case.

### **Major Contributions**

- A new method of signature segmentation, detailed in Appendix A, which dramatically reduces "false" segments;
- The development of successful methods for selecting effective training forgeries from a body of other users' reference signatures;
- A method for comparing signatures via string edit distance, outlined in Appendix B;
- Examination and development of methods for combining the output of neural networks and hidden Markov models;
- The introduction of several new features not previously used in on-line handwritten signature verification;
- A study on the need for a signer to have visual feedback when performing their signature.

## Contents

1	$\operatorname{Intr}$	oducti	ion 1
	1.1	Handv	vriting
	1.2	Handv	vritten Signatures
	1.3	Design	1 Overview $\ldots \ldots 6$
	1.4	Thesis	Structure
<b>2</b>	Lite	erature	Review 9
	2.1	Applic	cations of Handwritten Signature Verification $\ldots \ldots \ldots 10$
	2.2	Auton	nated Handwritten Signature Verification
		2.2.1	Dynamics of Signature Production
		2.2.2	The Basic Methodology 14
	2.3	Review	w of Earlier Work
		2.3.1	Combining Local and Global Features
3	Neu	ıral Ne	etworks 32
	3.1	The T	heory of Neural Networks
		3.1.1	Learning in Neural Networks
		3.1.2	Linear Networks
		3.1.3	Multi-Layer Perceptrons
		3.1.4	Radial Basis Functions
		3.1.5	Bayesian Networks
		3.1.6	Kohonen Self-Organising Maps
		3.1.7	Autoassociative Networks
	3.2	Applie	cations to Handwritten Signature Verification
	3.3	Previo	ous Work
	3.4	Metho	dology
		3.4.1	Pre-processing
		3.4.2	Signature Database
		3.4.3	Extracted Features

		3.4.4	Experimental Setup	90
4	Hid	den M	Iarkov Models	105
	4.1	The T	Theory of Hidden Markov Models	106
		4.1.1	Markov Models	107
		4.1.2	The Hidden Layer	109
		4.1.3	Bakis Models	117
		4.1.4	Learning in Hidden Markov Models	118
	4.2	Applie	cations to Handwritten Signature Verification	121
	4.3	Previo	ous Work	121
	4.4	Metho	odology	125
		4.4.1	Signature Segmentation	125
		4.4.2	Extracted Features	126
		4.4.3	Experimental Setup	132
<b>5</b>	Con	nbinin	g Multiple Models	137
	5.1	Previo	ous Work	138
	5.2	Metho	odology	145
		5.2.1	Experimental Setup	146
	5.3	Furthe	er Results	152
		5.3.1	Removal of "Short Signatures"	153
		5.3.2	Contribution to Overall Error	153
		5.3.3	Allowing Users Another Chance When Rejected	155
		5.3.4	Varying the Size of the Reference Set	156
		5.3.5	Zero-Effort False Acceptance Rate	
		5.3.6	The Importance of Visual Feedback When Signing	
		5.3.7	Manually Adjusted Personal Thresholds	
		5.3.8	Signing a Password	160
6	Con	clusio	n J	162
$\mathbf{A}_{j}$	ppen	dices	1	165
$\mathbf{A}$	$\mathrm{Th}\epsilon$	e Extre	emum Consistency Algorithm	165
	A.1		luction	165
	A.2		Problem Domain - Motivation	
	A.3	The A	Algorithm	168
	A.4	Succes	ssful Applications	171
		A.4.1	Direction Based Handwritten Signature Verification	172

		A.4.2	Velocity Based Handwritten Word Verification	175
		A.4.3	Physiology Research - Tracking Fluctuations in Infant	
			Face Temperature	176
	A.5	Future	e Work	. 176
	A.6	Conclu	$\dot{sion}$	. 176
Б	<b>.</b>			
В	Sigr	nature	Similarity Via Edit Distance	178

# List of Figures

1.1	A typical handwritten word, sampled at 205 points per second. Each dot in the handwriting represents the position of the pen tip for one of these samples
1.2	The various forces at work in generation of handwriting. A is the "pen pressure" exerted by the writer perpendicular to the axis of the writing instrument; B is the "point load", which is the component of pressure exerted perpendicular to the writing surface, responsible for indentations, line thickness etc.; and C is the "travel action", the pressure component exerted in two dimensions (forward/sideward for upstrokes or crossings and drag/backward for downstrokes) across the writing surface, re- sponsible for line generation. Together these forces contribute to features like velocity, acceleration, shape etc
2.1	The equal error rate is the error value at which the false accept-
2.1	ance and false rejection rates are the same
3.1	The general structure of a neuron
3.2	The sigmoid activation function
3.3	The hyperbolic activation function
3.4	The ramp activation function. $\ldots \ldots \ldots \ldots \ldots \ldots 38$
3.5	The step activation function. $\ldots$ $\ldots$ $\ldots$ $\ldots$ $39$
3.6	The sign activation function. $\ldots$ $\ldots$ $\ldots$ $\ldots$ $39$
3.7	Various feed-forward network topologies. (a) A simple two- input, one output network with no hidden layers. (b) A two- layer network with two inputs, two hidden nodes and one output node. (c) A more complicated network consisting of eight input nodes each connected to four nodes in the hidden layer and a single output node. (d) A network similar to that in (c) except
	with two hidden layers. $\ldots$ $\ldots$ $\ldots$ $\ldots$ $\ldots$ $41$

3.8	A linearly-separable feature space	45
3.9	A linear network.	46
3.10	Linear separability of Boolean functions - the axes represent the	
	input values and the dots represent the output (a solid dot is a $1$	
	and a hollow dot is a $0$ ). (a) The AND function which is linearly	
	separable. (b) The $OR$ function which is linearly separable. (c)	
	The XOR function - it is not possible to draw a single line to	
	separate the classes	46
3.11	The sampled coordinates captured from the handwritten word	
	"farley"	65
3.12	Interpolation of the sampled coordinates produces the off-line,	
	or static, image of the word	65
3.13	Contributors to the database grouped according to (a) nation-	
	alities, (b) handedness (left or right), (c) age and (d) gender	67
3.14	This is an illustration of the difficulty that a potential forger	
	has in trying to identify the pen-down ratio. The sample in (a)	
	is a genuine signature and $(b)$ is an attempted forgery based on	
	the forger having seen an off-line version of the signature (both	
	taken from the signature database used in this project). The	
	pen-down ratio for the genuine signature is $0.992$ and is $0.879$ for	
	the forgery (forgeries were typically found to have much lower	
	pen-down ratios, presumably because of the extra attention to	
	detail)	70
3.15	Horizontal length of a typical handwritten word is a simple fea-	
	ture to comprehend and calculate. The horizontal length of this	
	sample is 1,345 pixels	70
3.16	Cursivity varies widely between different authors while tending	
	to remain similar for different samples produced by the same au-	
	thor. For example consider parts $(a)$ and $(b)$ above that contain	
	words written by different authors with very different cursivity	
	values of $16.0$ and $3.6$ respectively. Part (c) is another sample	
	of the same written word as $(b)$ , by the same author, and has a	
	very similar cursivity value of 3.8	72

3.17	Cursiveness varies somewhat between authors and is a feature	
	that is highly indicative of natural handwriting style. (a) shows	
	a signature with a seemingly high cursiveness, but the actual	
	value for this is $12$ which is significantly lower than the signature	
	in $(b)$ at 125. These signatures are examples of how visual	
	inspection can be quite deceptive in estimation of cursiveness.	73
3.18	This is an illustration of how the different measures of cent-	
	ral tendency can give different midpoints for the calculation of	
	top-heaviness. The figure has three horizontal lines drawn to	
	illustrate the location of the calculated midpoint using the dif-	
	ferent central tendency measures.	74
3.19	Different handwriting samples can result in quite different curvature	;
	values. For example, (a) shows a sample in which the writing	
	is quite flat and not well-formed, resulting in a curvature value	
	of $3.96$ . Conversely (b) shows a sample with a much more pro-	
	nounced forming of the handwritten characters resulting in the	
	higher value of 5.22	75
3.20	The process of calculating the average curvature per stroke. $(a)$	
	shows the entire handwritten word and $(b)$ shows an isolated	
	view of one of the extracted strokes. $\ldots$ $\ldots$ $\ldots$ $\ldots$ $\ldots$ $\ldots$	75
3.21	Two signatures sections produced by the same author illustrat-	
	ing the consistency in the number of strokes. The crosses on	
	the handwriting represent the stroke boundaries. Both of these	
	samples have 21 strokes and as can be seen the segmentation is	
	$quite \ consistent.$	76
3.22	A typical handwriting sample with labels indicating the ascend-	
	ers, descenders, mean vertical displacement, ascender height and	
	$descender \ depth. \qquad \dots \qquad $	77
3.23	The maximum height of a signature or handwritten word is	
	defined as the distance from the top of the highest ascender to	
	the bottom of the lowest descender. The vertical line seen here	
	to the right of the writing sample is the maximum height, and	
	in this case is calculated as $1,005$ pixels. $\ldots$ $\ldots$ $\ldots$	78

	The gradient of the line between each pair of consecutive points is determined (a sample of which is shown in part (a)), and the mean of those values found - this mean is the slant of the hand- writing. Part (b) illustrates the computed slant value, drawn as a series of dotted lines laid over the handwriting sample "Long strokes" extracted from a typical handwriting sample.	79
5.25	The long stroke is represented as bolded handwriting with the remainder of the handwriting appearing as a broken line in the background.	80
3.26	Calculation of handwriting slant through regression of "long strokes". (a) shows one of the long strokes extracted from a typical handwriting sample. (b) shows a close-up view of that same stroke with the straight line being the line-of-best-fit as produced by simple linear regression. The gradient of this line is taken as the handwriting slant. (c) shows the same handwrit- ing sample used in (a) and is overlayed with a series of straight lines parallel to the calculated slant using the regression of long	
3.27	strokes	81
3.28	number of intersections)	82
3.29	best-fit	83

- 3.31 The various stages in the calculation of baseline consistency. (a) shows the original handwritten word, (b) shows the extracted minima for non-descender characters and (c) shows the line-of-best-fit calculated for these points using linear regression. The baseline consistency is then the square root of the sum of the squares of the distances between the extracted minima and the line. The baseline consistency of this handwriting sample is 25.2. 87
- 3.33 This figure illustrates "middle-heaviness", which is defined as the percentage of the bounding box of a signature that is interior to the sample itself. The bounding box is shown in the figure and all shaded pixels are points interior to (or part of) the sample. The area of the shaded pixels is then divided by the area of the bounding box to give middle-heaviness.
- 3.35 Convergence of training and verification errors. (a) In a linear network. (b) In a multi-layer perceptron with a single hidden layer.
  3.36 Error rates resulting from varying the number of hidden nodes in a MLP with one hidden layer.
  94

3.38	The performance of the optimal network structure using differ-
	ent threshold values
4.1	A Markov model of the weather
4.2	A HMM that models coin tosses using (a) 2 and (b) 3 states 111
4.3	A summary of Expectation Maximization (EM) training in hid-
	den Markov models
4.4	A 5-state left-right, or Bakis, model. This example features loop
	(for example, 1 to 1), forward $(1 \text{ to } 2)$ and skip $(1 \text{ to } 3)$ transitions.118
4.5	This figure presents a signature from the signature database.
	Using the velocity based stroke (VBS) technique for segmenta-
	tion results in 290 strokes, whereas the extremum consistency
	approach results in 217 strokes
4.6	This figure represents the horizontal length of a typical stroke.
	(a) contains the original handwritten sample with an extracted
	stroke in bold. (b) shows an expanded view of that same stroke
	with the horizontal length marked
4.7	Different strokes can result in quite different curvature values.
	For example, (a) shows a sample stroke that is quite flat, result-
	ing in a curvature value of $0.01$ . Conversely (b) shows a sample
	with a much more pronounced curve that results in the higher
	curvature value of $0.40.$
4.8	Handwriting slant calculated using stroke end-points. This is
	the same stroke as shown in Figure 4.7, depicted here as the
	series of sampled points. The solid line to the immediate right
	is the calculated slant. $\ldots \ldots 129$
4.9	An illustration of handwriting slant calculated through regres-
	sion. (a) shows the original word as a series of sampled points
	with the extracted stroke in bold and $(b)$ shows slant calculated
	via regression
4.10	$A\ graphical\ representation\ of\ the\ beginning\ and\ ending\ gradient$
	values within the stroke. $\ldots \ldots 131$
4.11	$A \ plot \ of \ the \ HSV \ results \ using \ the \ Segmental \ K-Means \ learning$
	algorithm and different threshold values. $\ldots \ldots \ldots \ldots \ldots \ldots 135$
4.12	A plot of the HSV results using the Baum-Welch learning al-
	gorithm and different threshold values
5.1	The combination of models described in previous chapters 146

5.2	The MLP structure that produced the lowest overall error rate when combining the constituent systems. Each of the weight	
		150
5.3	values $W_i$ is optimised via a learning algorithm	
		. 194
5.4	The overall error rate versus the duration threshold. Signers	
	with an average signature duration less than t seconds were re-	
	moved from consideration. As can be seen, error rates generally	
	improve as signature duration increases	. 154
5.5	A plot of individual contributions to overall error rate, sorted	
	in order of increasing contribution.	. 155
5.6	The overall error rate versus the number of reference signatures	
	used.	. 157
5.7	(a) A signature sample captured using a stylus to provide visual	
	feedback to the signer. (b) A signature sample from the same	
	author captured without the use of the stylus. $\ldots$ $\ldots$ $\ldots$	. 158
A.1	This figure represents some local minima situations which are	
	typically encountered in processing the input stream. The hori-	
	zontal axis represents increasing time and the vertical axis can	
	represent various stream types such as velocity, direction and	
	temperature. Specifically, (a) contains a valid minimum, (b)	
	contains only a single valid minimum (there are actually two	
	minima, but the second is the result of the local maximum in	
	the centre, which should be ignored in this environment) and all	
	others contain no "true" minima. An effective algorithm should	
	reflect this.	167
A.2	Situations like this are the result of the limited resolution of the	. 101
11.4	hardware used to capture a stream. The black line represents	
	the actual value of the stream and the black dots represent the	
	-	
	recorded value. Time is represented on the horizontal axis. This	
	situation typically arises when the hardware is a graphics tablet	
	which rounds the position of the pen tip to the nearest pixel,	
	but also comes up with (say) temperature observations when the	
	actual temperature is rounded to the nearest tenth of a degree	
	for recording.	. 168

A.3	A finite state machine expressing the EC algorithm. The move-
	ments between vertices (states) are defined by the comparison
	between points in the input stream and the comparisons are
	included on the edges in the diagram. Additionally there are
	actions to be performed when vertices are reached - these are
	also included in the diagram
A.4	An illustration of step and width calculation. Valid steps occur
	between time points $0$ and $1$ , $1$ and $2$ , $3$ and $4$ and $5$ and $6$ .
	Backward steps occur between time points 6 and 7, as well as
	between 9 and 10
A.5	An illustration of a large downslope with a small upslope. The
	minimum indicated by $(1)$ is more likely the result of noise than
	a genuine valley and should be ignored (that is, it is necessary
	to take the minimum of the upslope and the downslope, rather
	than the sum or average). The better minimum would be that
	indicated by (2). $\ldots$
B.1	A portion of a signature that has been segmented. The crosses
	on the diagram represent stroke start and/or end points 179
<b>B</b> .2	The start-point of each stroke is placed at the origin and the
	quadrant in which the end-point lies is recorded as the observa-
	tion. The line appearing in the figure in quadrant A represents
	a stroke extracted from a handwritten word

## List of Tables

3.1	A summary of the main database of signatures used in experi-
	$mentation. \ldots 68$
3.2	The training performance of three network structures 96
3.3	The classification accuracy of the three implemented neural net-
	work training algorithms
3.4	$The \ convergence \ speed \ of \ the \ three \ implemented \ neural \ network$
	training algorithms
3.5	The performance of the $HSV$ system using different approaches
	to obtaining negative examples
3.6	The performance of the $HSV$ system using different $MLP$ struc-
	tures. Unless otherwise stated, the structure made use of a
	single hidden layer. $\ldots$
4.1	The training performance of the two HMM training algorithms
	used in experimentation. The "Number of Epochs" is the mean
	number of epochs required for convergence to occur (with stand-
	ard deviation in brackets). The relative time compares the
	elapsed time prior to convergence
4.2	A comparison of the modelling accuracy of the Segmental K-
	Means and Baum-Welch HMM training algorithms. All signi-
	ficant HSV-related error rates are reported in this table 135
4.3	A comparison of the modelling accuracy of the Segmental K-
	Means and Baum-Welch HMM training algorithms when ten
	reference signatures are used to train the model
5.1	The results using the two different voting mechanisms to com-
J.1	bine the classifiers.
5.2	The resulting error rates using the different confidence-based
	approaches to combining the classifiers

5.3	The most successful results for each of the different model scen-
	arios used during development. $\ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots 152$
5.4	A breakdown of the error rates for various reference set sizes,
	optimised to give the lowest overall error rate
5.5	The resulting error rates using different types of forgeries in the
	"signing passwords" variant of the HSV system
A.1	Error rates using various methods of overcoming local extrema in a specific signature verification environment. If there are parameters involved in the operation (such as convolution win- dow size) then the parameters which produced the lowest overall error rates were used to generate the results